Dielectric Study of the Molecular Mobility and the Isothermal Crystallization Kinetics of an Amorphous Pharmaceutical Drug Substance

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ABSTRACT: During the development of new pharmaceutical products based on drug substances in their amorphous form, the molecular mobility of an amorphous active ingredient was characterized in detail within a very broad time–temperature range. The relation between the isothermal crystallization kinetics and the dynamics of this amorphous substance was investigated. First, dynamic dielectric spectroscopy (DDS) and the thermostimulated current (TSC) techniques were used to analyze the molecular mobility of the amorphous drug substance over a wide frequency and temperature range (the drug substance is referred to as SSR in this text and was chosen as a model glass-forming system). Two relaxation processes, corresponding to different molecular motions, were identified. The $\beta_a$-relaxation process, associated with intramolecular oscillation of small dipolar groups, followed Arrhenius temperature behavior over the entire time–temperature domain that was studied. However, the main $\alpha_a$-relaxation process, assigned to the dielectric manifestation of the dynamic glass transition of the amorphous phase, was described by Vogel–Fulcher–Tammann (VFT) and Arrhenius behavior above and below the glass transition temperature ($T_g$) respectively. The physical meaning of these complex dynamics is explained in the context of the Adam and Gibbs (AG) model, by the temperature dependence of the size of cooperatively rearranging regions (CRR) that govern the time scale of delocalized molecular motions. The distinction between the molecular mobility and the structural relaxation of amorphous systems below $T_g$ is discussed. This work shows that the complementary nature of both DDS and TSC techniques is essential to directly analyze the intramolecular and molecular motions of disordered phases over a wide time–temperature range above and below the $T_g$. Second, real-time dielectric measurements were carried out to determine the isothermal crystallization kinetics of the SSR amorphous drug. Whatever the crystalline form obtained over time in the crystallization process, the decrease of the dielectric response of amorphous phase, which is characteristic of the isothermal crystallization, was studied to monitor the time dependence of the degree of crystallinity. The characteristic crystallization time, derived from Kohlrausch–Williams–Watt (KWW)–Avrami analyses performed at different temperatures, followed an Arrhenius temperature dependence. Behaviors specific to the molecular mobility of the amorphous drug substance were compared with the characteristic crystallization time. It was concluded
that the crystal growth process of the SSR drug seems to be controlled by the intramolecular motions involving the $\beta_a$-relaxation mode and not by the molecular motions responsible for the $\alpha_a$-relaxation mode in the range of temperatures $> T_g$. Subsequent studies will focus on the crystallization process of the SSR drug in the glassy state ($T < T_g$). © 2004 Wiley-Liss, Inc. and the American Pharmacists Association J Pharm Sci 93:218–233, 2004

**Keywords:** amorphous; dynamic dielectric spectroscopy; ThermoStimulated Current; mobility; crystallization; relaxation time; glass transition

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**INTRODUCTION**

The aqueous solubility of new pharmaceutical drug substances is increasingly becoming a concern. If these new drugs have good permeability across the intestinal barrier, then their bioavailability can be improved by promoting the dissolution rate in the gastrointestinal tract. Several different strategies have been adopted to accelerate the dissolution of poorly soluble drugs because the oral route remains the most utilized way to administer a medication. The use of liquid and solid solutions, micronization, and cyclodextrin or other additives are some examples of approaches taken to improve bioavailability. Another possible strategy is to exploit the advantage offered by amorphous phases of a very high free energy state. The latter is characterized by important free volume, which will promote the accessibility of foreign molecules like water and, consequently, the kinetics of dissolution. However, because the molecules in amorphous phases have more free energy, they are more susceptible to chemical reactions leading to impurity formation (toxicity). Equally important is their potential to undergo a crystallization process over time that would potentially impact the bioavailability, which is not pharmaceutically acceptable.

Consequently, the use of amorphous phases has been the subject of very intensive investigations, and this domain, which is already well developed in the study of the physics of solids (especially in the polymer physics area), has moved into the pharmaceutical realm.¹⁻⁵ These studies have shown, at least qualitatively, that the molecular mobility of the amorphous phase is responsible for chemical¹,⁶⁻⁸ and physical instabilities.¹⁻⁹⁻¹² The physicochemical instabilities of amorphous drugs will remain a great problem until the molecular mobility is well characterized and understood.

The main objective of this study was to investigate the correlation between the molecular mobility of a pure amorphous drug and the kinetics of its isothermal crystallization, which is a major drawback (as already described). In particular, in this work we have attempted to determine which molecular motions are involved in the crystallization process (nucleation, crystal growth).

To reach this goal, the molecular mobility of amorphous drug was detected and analyzed by dynamic dielectric spectroscopy (DDS) and the ThermoStimulated Current technique (TSC), which will be henceforth be collectively referred to as dielectric spectroscopy (DS). Among all techniques currently used to study the dynamics of amorphous phases, such as solid-state nuclear magnetic resonance (NMR), quasi-elastic light scattering (QELS), quasi-elastic neutron scattering (QENS), fluorescence depolarization (FD), differential scanning calorimetry (DSC), dynamic mechanical analysis (DMA), and thermostimulated creep (TSCr), DS was chosen because of its very high sensitivity and its wide accessible frequency range of molecular solicitation. These properties allow detection of motions that have a relaxation time of $10^4 – 10^9 \text{s}$ over a wide temperature range ($-160–300^\circ \text{C}$).¹⁴⁻¹⁷ The main interest in DS is its ability to directly characterize the time scale of intramolecular and molecular motions both above and below the glass transition temperature ($T_g$) of amorphous phases.¹⁵,¹⁶,¹⁸ The DSC method is often described in the literature for determination of the molecular mobility of amorphous phase below $T_g$ by tentatively relating the molecular mobility to the structural relaxation of disordered phases in ageing experiments.¹⁹,²⁰ However, the dielectric techniques directly probe the molecular motions by stimulating the different electrical dipolar groups, with a suitable applied electrical field, thereby allowing a clear differentiation between localized relaxing entities involved in secondary relaxation and the larger sized species involved in the dynamic glass-to-liquid transition.

The crystallization process of amorphous samples has been extensively studied, but most studies reported in the literature are based on analyses performed by optical microscopy under
cross polarizers, X-ray powder diffraction (XRPD), or DSC.\textsuperscript{21–23} All these techniques measure the crystal formation from the detection of the specific responses of the crystal (e.g., light polarization, diffraction, and heat of fusion). To determine the kinetics of isothermal crystallization, an original method comprising real-time dielectric measurements was preferred in this work. With this method, the isothermal crystallization of the amorphous sample is monitored \textit{in situ} in the dielectric cell as time elapses, without any temperature change during the entire experiment. In this case, the diminishing dielectric response of the amorphous part is recorded as the increase in degree of sample crystallinity with time.

Analyses of relations between the molecular mobility and the isothermal crystallization kinetics were carried out on a poorly soluble development pharmaceutical drug from the Sanofi-Synthelabo Research Department. This compound, obtained in an amorphous phase and as two different crystalline forms (A and B) that are enantiotropically related, is considered a good model for the study of the propensity of a complex glass-forming system to crystallize over time.

**EXPERIMENTAL**

**Methods**

**Differential Scanning Calorimetry (DSC)**

DSC measurements were carried out with a TA instrument 2920 apparatus, using non-hermetically sealed pans. Thermograms were recorded at a heating rate of 10°C/min from 20 to 180°C, under a dry nitrogen gas purge at a flow rate of 50 mL/min. High purity indium was used for temperature and enthalpy calibration. The glass and the melting transition temperatures were determined as the midpoint of the heat capacity increment and as the onset temperature of the endothermic peak, respectively.

**X-ray Powder Diffraction (XRPD)**

The XRPD patterns of solid samples were determined at ambient temperature with a Siemens D500TT X-ray powder diffractometer at 40 kV and 25 mA, with CuKα radiation. Counts were measured with a scintillation counter from 4 to 40° in the 2θ diffraction angle range, with an angle rate of change of 1°/min (step size = 0.030°; residence time = 2 s).

**Dynamic Dielectric Spectroscopy (DDS)**

Complex dielectric permittivity ($\varepsilon^* = \varepsilon' - i\varepsilon''$) and dielectric loss factor ($\tan \delta = \varepsilon''/\varepsilon'$) measurements were performed with a Novocontrol (BDS4000) Broadband Dielectric Spectrometer based on an Alpha analyzer. The sample was placed into a dielectric cell especially designed for the analysis of powder and low molecular weight systems exhibiting significant flow at high temperatures. The cell is composed of two electrodes, which are able to follow the geometrical change of a sample, and a Teflon\textsuperscript{®} ring, which keeps the sample between electrodes at high temperatures. The dielectric cell was placed into a cryostat, and the temperature was controlled with an accuracy of $\pm 0.1$°C by a cold nitrogen gas stream that was heated by a Quatro temperature controller.

To determine the molecular mobility, the dielectric measurements were carried out isothermally from −160 to 150°C in steps of 5°C, in the $10^{-1}$–$10^6$ Hz frequency range. Concerning the isothermal crystallization analyses, \textit{in situ} real-time dielectric measurements were carried out at a given temperature at successive time intervals. For each crystallization temperature, a specific frequency range was selected so that the time of the frequency sweep was short enough to avoid an evolution of the structure of sample. For example, at 120°C, the selected frequency range was between $10^2$ and $10^5$ Hz so that the corresponding acquisition time of each DDS spectrum was $<1$ min.

**ThermoStimulated Current (TSC)**

TSC experiments were carried out with a Thermold\textsuperscript{®} TSC/RMA 9000 instrument. Drug was placed, as for DDS, in a sample cell especially designed for dielectric analyses of powders. Before the experiments were initiated, a secondary vacuum was applied to the sample cell located in the TSC cryostat and subsequently flushed with dry helium. To obtain TSC spectra, the sample was polarized by a static electrical field ($E_{p} = 950$ V/mm) at the polarization temperature ($T_p$) for an amount of time ($t_p$) that was long enough for the sample to reach the equilibrium polarization. This polarization stage allows the orientation, towards the direction of the field, of dipolar species that are mobile at this temperature. The sample was then quenched to a temperature $T_0 \ll T_p$, which enabled the polarization to be retained. At $T_0$, the field was switched off, and the sample was short-circuited for a defined amount of time ($t_{cc} = 2$ min) to remove fast relaxing space charges.
and to stabilize the sample temperature. The depolarization current \(I(T)\) was then recorded with a very sensitive electrometer (resolution of \(10^{-16}\) A) as the temperature increased at a constant heating rate of \(7^\circ C/min\) from \(T_0\) to a final temperature \(T_f\) that was \(>T_p\). The variation of the depolarization current versus temperature corresponds to the global TSC spectrum.

**Materials**

**Crystalline Forms of the Drug Substance (SSR)**

The drug substance, labeled SSR hereafter, was obtained from Sanofi-Synthelabo Research. This low molecular weight system has been shown to exist in two crystalline forms that are referred to as A and B. Both crystalline forms have low solubility in classical solvents and a good permeation through biomembranes (class 2 in the BCS classification). Consequently, the SSR drug substance represents a good candidate to study for the development of new formulations based on an amorphous drug. Thermograms recorded for the A and B crystalline forms (Fig. 1) display melting transitions characterized by onset temperatures of 146 and 156°C, respectively, and by melting enthalpies of 70 and 58 J \(g^{-1}\), respectively. From these parameters, and from the study of the A and B crystallization in solution at different temperatures, the system was found to be enantiotropic. \(^{24}\) The solid–solid transition temperature was estimated from thermodynamic values \(^{25}\) as \(\sim T_{ss} = 103^\circ C\), and the A crystalline form was found to be more stable at temperatures \(<T_{ss}\).

**Amorphous Form of SSR**

The amorphous form of SSR was prepared by melting the A crystalline form of SSR at 180°C for 10 min and then quench cooling the resulting melt in liquid nitrogen. The obtained amorphous film was then ground and stored at 5°C/0% relative humidity (over P\(_2\)O\(_5\)), despite the substance being hydrophobic. No chemical degradation was observed for the drug substance obtained as amorphous phase by this specific thermal treatment, as determined by high-performance liquid chromatography (HPLC) analyses. The DSC thermogram recorded for the amorphous SSR is shown in Figure 1. The glass transition at \(T_g = 76^\circ C\) was the single event observed on the thermogram; neither crystallization nor melting transition was noted at high temperature on the thermogram recorded at a heating rate of 10°C/min.

**RESULTS**

**Molecular Mobility of the Amorphous Form of SSR Dynamic Dielectric Spectroscopy**

The dielectric properties of amorphous SSR were recorded isothermally in the \(10^{-1}–10^6\) Hz frequency range for temperatures between \(-160\) and \(-130^\circ C\) (steps of \(5^\circ C\)). The loss factor \([\tan(\delta) = \varepsilon''/\varepsilon']\) is shown on a logarithmic scale as a function of frequency and temperature in Figure 2. Three

![Figure 1](image1.png)

**Figure 1.** DSC thermograms recorded for SSR in the A and B crystalline forms (dashed lines) and in the amorphous form (solid line). The inset shows an enlargement of the low temperature range.

![Figure 2](image2.png)

**Figure 2.** Dielectric loss factor, \(\tan(\delta)\), of the amorphous form of SSR reported on a logarithmic scale as a function of temperature and frequency.
different dielectric events were noted for the amorphous form of SSR. In the low temperature range, a weak and broad relaxation mode was observed. This mode, designated $\beta_a$, moved from $10^{-1}$ to $10^6$ Hz as the temperature increased from $-155$ to $40^\circ$C. At high temperature, a more intense and narrow relaxation mode, labeled $\alpha_a$ relaxation, was noted. For sake of clarity, the isothermal DDS spectra, recorded over the 80–130°C temperature range in steps of 10°C, are shown in Figure 3. We note on this figure that the $\alpha_a$ mode extends over the entire accessible frequency range in the temperature range 80–130°C. In the absence of any crystalline phase, the $\alpha_a$ and $\beta_a$-relaxation modes are associated with specific molecular motions of the SSR amorphous phase. In the low frequency and high temperature range, the high values of $\tan(\delta)$ correspond to the undesired dielectric conductivity, noted as $\sigma$, which is due to motions of free electrical charges (electrons or ionic species).

To extract the relaxation time of molecular motions involved in both $\alpha_a$- and $\beta_a$-relaxation modes by taking into account the conductivity phenomenon and the complexity of each mode, all DDS spectra were fitted by a sum of Havriliak–Negami (HN) terms:

$$
\varepsilon^*(\omega) = \varepsilon_\infty + \sum_j \frac{\Delta \varepsilon_j}{[1 + (i\omega\tau_j)^\gamma]} + \frac{\sigma_0}{i\omega\tau_0} \quad (1)
$$

where $\varepsilon_\infty$ is the dielectric permittivity at very high frequency; $\Delta \varepsilon_j$ is the dielectric strength; $\tau_j$ is the relaxation time; and $\gamma_j$ and $\beta_j$ are the HN shape parameters ($0 < (\gamma_j/\beta_j) \leq 1$), which describe, respectively, the symmetrical and asymmetrical broadening of the $j^{th}$ relaxation mode ($j = 1$ and 2 for the $\alpha_a$ and $\beta_a$ relaxations, respectively). The $\sigma_0/i\omega\tau_0$ term, where $\varepsilon_0$ is the vacuum dielectric permittivity and $\sigma_0$ is the dc conductivity, takes into account the dielectric conductivity phenomenon ($\sigma$ event). The accuracy of the fit procedure is presented in Figure 3, where HN calculated functions are superimposed on the corresponding DDS experimental points. For each temperature, the fit accuracy coefficient ($R^2$) is >0.99.

The temperature dependence of HN relaxation times corresponding, respectively, to the $\alpha_a$- and $\beta_a$-relaxation modes, is represented in the Arrhenius diagram shown in Figure 4 (symbols). The temperature dependence of the $\beta_a$-relaxation time can be described by Arrhenius behavior:

$$
\tau(T) = \tau_{0a} \exp\left(\frac{E}{RT}\right) \quad (2)
$$

where $E$ is the activation energy, $\tau_{0a}$ is the pre-exponential factor, and $R$ is the ideal gas constant. In contrast, the $\alpha_a$-relaxation time follows the Vogel–Fulcher–Tammann (VFT) behavior law:

$$
\tau(T) = \tau_{0a} \exp\left(\frac{B}{T - T_0}\right) \quad (3)
$$

where $\tau_{0a}$ is the pre-exponential factor and $B$ and $T_0$ are constants. The different parameters determined from nonlinear least square fit and the associated $R^2$ values are listed in Table 1. The value of the fragility parameter of the $\alpha_a$ dynamics, $m = 54.7$, was derived from the following expression, which connects the VFT parameters $B$ and $T_0$ with the fragility index:

$$
m = 16 + \frac{590 \cdot T_0}{B} \quad (4)
$$

In the strong/fragile classification of Angell, the $m$ parameter of different liquid glass-forming systems varies from 16 (strong dynamics) to 200 (fragile dynamics) as the intermolecular strengths governing the behavior law of the time scale of molecular motions decrease. From the obtained value of the $m$ parameter, it can be deduced that the amorphous SSR is characterized by weak physical interactions that do not significantly constrain the molecular mobility of this disordered phase.

The VFT behavior law of the $\alpha_a$-relaxation time unequivocally associates this relaxation mode with the dielectric manifestation of the SSR amorphous phase dynamic glass transition. This assignment is also confirmed by the very good
agreement noted between the glass transition temperature determined by DSC \((T_g = 76.8 \, ^\circ\text{C})\) and the temperature \((T = 74.8 \, ^\circ\text{C})\) to which the \(\alpha_a\)-relaxation time was extrapolated at 100 s (100 s is the time value that is well known to be the time scale of molecular motions involved in the glass transition at \(T_g\)).\(^{28}\) The origin of the \(\alpha_a\)-relaxation mode is the cooperative motion of the whole of molecules.

The low temperature position and the Arrhenius temperature dependence of \(\beta_a\)-relaxation are characteristic of a secondary dielectric relaxation mode. This relaxation has been attributed to localized intramolecular mobility of SSR molecules on the basis of comparisons with that which has been demonstrated for amorphous and semicrystalline polymers.\(^{13,15–17,29,30}\) As for polymer materials, the \(\beta_a\)-relaxation process corresponds to the oscillation of small dipolar groups exhibiting relative high dipolar moments.

From DDS measurements, all dynamics specific to the amorphous form of SSR (intramolecular and molecular motions involved in the glass transition) were directly determined in a wide temperature range above and below \(T_g\).

**ThermoStimulated Current**

The TSC spectrum of the amorphous SSR drug, recorded from \(-170\) to \(100 \, ^\circ\text{C}\) after polarization of the sample at \(90 \, ^\circ\text{C}\), is shown in Figure 5. The inset shows an enlargement of the TSC response recorded at low temperature. Two different relaxation modes were resolved. At high temperature \((\sim 75 \, ^\circ\text{C})\), an intensive and narrow TSC peak was observed. The temperature position of this relaxation mode, very close to the glass transition temperature of amorphous phase detected by DSC, allows us to associate this mode with the dielectric manifestation of the glass transition. This relaxation mode corresponds to the one observed by DDS at high temperature and labeled the \(\alpha_a\)-relaxation process. At low temperature \((\sim -120 \, ^\circ\text{C}; \text{inset on Figure 5})\), a very broad and weak relaxation mode was noted. This mode corresponds to the secondary \(\beta_a\)-relaxation process previously observed by DDS.

TSC global spectra obtained from the polarization of the sample at a single high temperature

<table>
<thead>
<tr>
<th>Relaxation mode</th>
<th>Law</th>
<th>(R^2)</th>
<th>(\tau_{0\alpha}; \tau_{0\beta}) (s)</th>
<th>(E) (kJ · mol(^{-1}))</th>
<th>(B) (K(^{-1}))</th>
<th>(T_0) (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\beta_a)</td>
<td>Arrhenius</td>
<td>0.998</td>
<td>(8 \cdot 10^{-16})</td>
<td>53.2</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>(\alpha_a)</td>
<td>VFT</td>
<td>0.9997</td>
<td>(2.8 \cdot 10^{-18})</td>
<td>—</td>
<td>3926</td>
<td>-15.7</td>
</tr>
</tbody>
</table>

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**Figure 4.** Relaxation time, determined from DDS (symbols) and TSC (short solid lines) analyses, of species involved in the \(\beta_a\)- and \(\alpha_a\)-relaxation modes as a function of reciprocal temperature (Arrhenius plot). Solid and dashed lines report Arrhenius and VFT behavior laws characteristic of \(\beta_a\)- and \(\alpha_a\)-relaxation modes, respectively.

**Figure 5.** TSC global spectrum of amorphous SSR polarized at 90°C. The inset shows an enlargement of the TSC spectrum recorded in the low temperature range.
are complex. All relaxation modes detected by the TSC global procedure result from the relaxation of a distribution of relaxing species that differ from each other by their nature and/or their local environment. This fact is evidenced in Figure 5 by the clear shoulder observed on the low temperature side of the $\beta_a$-relaxation mode, which corresponds to the relaxation of slightly different dipolar groups from the one involved in the $\beta_a$-relaxation mode. This shoulder was observed by TSC and not by DDS because of the very low excitation frequency range of the TSC technique, which increases the resolution of the different relaxation modes by splitting the temperature range in which relevant motions occur.

The fractional polarization technique (TSC-FP) was used to experimentally determine the distribution of different species involved in each relaxation mode with their own dynamics. For this investigation, the sample was polarized within a narrow temperature window ($\Delta T = 5^\circ$C) during the cooling process of the classical TSC thermal program. This polarization window orients only a set of identical species. The TSC-FP elementary spectrum corresponding to the relaxation of selected species was then recorded by the same procedure as that used for the TSC method. By shifting the position of the polarization window along the temperature axis, in steps of 2.5°C, the mobility of all sets of species with different dynamics can be analyzed. Further details regarding the TSC-FP method are available in the literature.\textsuperscript{15,18,29,30}

The elementary TSC-FP spectra obtained for the $\alpha_a$-relaxation mode by shifting the polarization window ($\Delta T = 5^\circ$C) from 45 to 80°C in steps of 2.5°C are plotted in Figure 6. The good agreement between the TSC complex spectrum reported in Figure 5 and the shape of the envelope of all elementary TSC-FP spectra confirms that all different molecular species involved in the $\alpha_a$-relaxation process were selected by the successive polarization windows.

According to Bucci et al.,\textsuperscript{31} the analysis of each elementary TSC-FP spectrum with eq. 5 leads to the temperature dependence of elementary relaxation times, $\tau_{i\text{FP}}$, which characterizes the dynamics of species involved in the $\alpha_a$-relaxation mode:

$$\tau_{i\text{FP}} = \frac{1}{q} \int_T^{T_0} \frac{I_i(T')dT'}{I_i(T)}$$

In 5, $I_i$ is the depolarization current of the $i^{th}$ recorded TSC-FP spectrum and $q$ is the heating rate. The temperature dependence of the different elementary relaxation times, $\tau_{i\text{FP}}$, is shown as a function of reciprocal temperature in Figure 7. All $\tau_{i\text{FP}}$ exhibit linear behavior on the Arrhenius diagram, which can be described by eq. 2. For each dynamic displayed in Figure 7, the activation parameters were determined from a nonlinear least square fit. The dynamics of relaxing species, which contribute to the $\alpha_a$-relaxation mode, were characterized by a narrow distribution of activation parameters; the activation energy varies from 103 to 240 kJ mol$^{-1}$.

**Isothermal Crystallization**

Before considering the DDS study of the crystallization kinetics of the amorphous SSR, it was important to check that no dielectric response of SSR in the crystalline form interferes with

\begin{figure}
\centering
\includegraphics[width=0.8\textwidth]{figure6.png}
\caption{Elementary TSC-FP spectra of the $\alpha_a$-relaxation mode of the amorphous form of SSR.}
\end{figure}

\begin{figure}
\centering
\includegraphics[width=0.8\textwidth]{figure7.png}
\caption{Arrhenius plot of elementary relaxation times $\tau_{i\text{FP}}$ determined from analyzes of TSC-FP spectra recorded in the $\alpha_a$ temperature range of the amorphous form of SSR.}
\end{figure}
dielectric responses specific to the amorphous form of SSR. Isothermal DDS spectra for the SSR drug in A crystalline form, recorded from −155 to 130°C in steps of 5°C, are shown in Figure 8. As in the case of the amorphous phase, an important dielectric conductivity was observed in the high temperature and low frequency range. The single relaxation mode that characterizes the A crystalline SSR was observed for high frequencies in the lowest accessible temperature range. This weak relaxation mode, named γc, might correspond to oscillations of small dipolar groups located in the crystalline phase that are not inhibited by strong interactions imposed by neighboring molecules. In the entire investigated temperature range, the more-or-less scattered dielectric properties recorded in the 10−7–102 Hz frequency range correspond to the dielectric noise associated with the specific detection mode of the dielectric spectrometer used only in this frequency range. This noise is significantly magnified by the large tan(δ) scale adopted in this figure to observe the weak γc-relaxation mode. No additional relaxation mode was detected in this frequency range.

It is evident from the results in Figure 8 that the frequency—temperature position of the single weak dielectric relaxation mode detected for SSR in the A crystalline form is outside the range in which the αa-relaxation mode was detected. This result supports the choice of the αa-relaxation mode to follow the crystallization of the amorphous form of SSR. Also, this result and the lack of any dielectric event for the A crystalline form of SSR in the αa-relaxation domain, except the conductivity, show that A crystalline and amorphous dielectric responses are not interfering, thereby confirming that the αa- and the βa-relaxation modes are representative of the amorphous state of the SSR. The same conclusion was drawn concerning the B crystalline form with respect to the amorphous phase (data not shown).

The isothermal crystallization of the amorphous SSR was analyzed by real-time in situ dielectric measurements performed in the 100–140°C temperature range, in which the αa-relaxation mode was observed. These experiments correspond to the isothermal cold crystallization of the amorphous SSR because the temperature of the system was increased from room temperature to the temperature of crystallization. As an example, the dielectric properties recorded for SSR, initially in amorphous form, at 120°C in the 102–106 Hz frequency range for different times between 0 and 41,000 s, are reported in Figure 9 (symbols corresponding to experimental points are not reported here for sake of clarity). It is evident that the intensity of the loss peak (Fig. 9a) and the increment of the real part of the complex permittivity corresponding to the αa-relaxation mode (Fig. 9b) both decrease as the experiment time increases. These simultaneous phenomena correspond to the isothermal crystallization of the amorphous phase of SSR.

![Figure 8](image)

**Figure 8.** Dielectric loss factor, tan(δ), of SSR in the A crystalline form, reported as a function of temperature and frequency.

![Figure 9](image)

**Figure 9.** Frequency dependence of isothermal DDS measurements recorded at 120°C for different times: (a) the loss factor tan(δ); (b) real part of the complex permittivity ε′. Arrows displayed on both figures indicate the decreasing signal as the time increases.
The first tan(δ) spectra characterized by high conductivity and the peak positioned at ~6 \times 10^4 \text{Hz} and tan(δ)_{max} = 0.26 correspond to an entirely amorphous sample. After an induction period of time, the intensity of the tan(δ) peak associated with the \( \alpha_a \)-relaxation mode decreases with time, indicating crystallization of the amorphous phase. The frequency position and the shape of the \( \alpha_a \)-relaxation mode are weakly time dependent. At very long times, the \( \alpha_a \)-relaxation is no longer observed, suggesting that conversion of amorphous phase into crystalline phase was completed.

Crystallization was also observed with the real part of the complex permittivity, \( \varepsilon' \). During the isothermal crystallization, the intensity of the \( \varepsilon' \) increment (i.e., the dielectric strength \( \Delta \varepsilon \)) decreases continuously with time, whereas its frequency position stays nearly constant. For each spectrum recorded at a selected time, we note also that the \( \varepsilon' \) value recorded in the low frequency range is frequency independent. This result indicates that the time needed for each frequency sweep (<1 min for the selected frequency range for experiment performed at 120 °C) was short enough to conserve the sample in an isostructural state.

The fact that neither the shape of DDS spectra nor the frequency position of the \( \alpha_a \)-relaxation mode evolves very much during crystallization time suggests that the SSR amorphous phase is weakly disturbed by physical constraints imposed by the crystal growth. Depending on the chemical nature of the sample, different results have been reported in the literature regarding this point. For polymers such as poly(ethylene terephthalate)\(^{32,33}\) and poly(ether ether ketone)\(^{34}\) that contain rigid backbones, DDS spectra shift to a lower frequency (i.e., the mean relaxation time of the \( \alpha_a \)-relaxation mode increases) during the crystallization, indicating that molecular motions in amorphous phases are significantly restricted by the presence of crystallites. In contrast, for low molecular weight systems\(^{35,36}\) or polymers with flexible chains, such as poly(l-lactic acid),\(^{37}\) the relaxation time of the \( \alpha_a \)-relaxation mode is unaffected by the degree of crystallinity until the crystallinity is high enough to constrain the mobility of amorphous phase. In the latter case, the confinement effect on the amorphous phase appears as the distances between crystallites become shorter than the size of cooperative rearranging regions (CCR) specific of the amorphous phase at the considered crystallization temperature. The difference between the two kinds of polymers arises from the propensity of each polymer chain to participate simultaneously in both amorphous and crystalline phases.

In the crystallization study described here, the range of interest of the degree of crystallinity is low enough to assume that the confinement effect was ineffective. Therefore, it can be considered that this low molecular weight drug crystallizes in a two-phase system; that is, the system is only composed of amorphous and crystalline zones, which is the ideal one-state model.\(^{18}\) From this reasonable assumption, the degree of crystallinity of the sample was calculated by the determination of the amorphous content from the intensity of the \( \alpha_a \)-relaxation mode.

To extract the crystallization kinetics from dielectric data by taking into account the dielectric conductivity, all isothermal DDS spectra recorded at different times for each crystallization temperature were fitted by the HN expression (eq. 1). For each temperature, the time dependence of the dielectric strength, \( \Delta \varepsilon(t) \), of the maximum of the imaginary peak, \( \varepsilon''_{\text{max}}(t) \), and that of the maximum of the loss factor, tan(δ)\(_{\text{max}}(t) \), were determined and normalized to the corresponding value of the SSR drug in the wholly amorphous state (at \( t = 0 \)). The three normalized parameters were found similar. The time dependence of the degree of crystallinity \( \chi_c \) for each crystallization temperature between 100 and 140 °C was estimated from the normalized dielectric strength\(^{35}\) according to eq. 6:

\[
\chi_c(t) = 1 - \frac{\Delta \varepsilon(t)}{\Delta \varepsilon(t = 0)} \quad (6)
\]

As expected, the \( \chi_c \) curves shift to a shorter time as the crystallization temperature increases (see results in Figure 10).

The time evolution of the degree of crystallinity has been often described by the well-known Avrami equation:\(^{38}\)

\[
\chi_c(t) = 1 - \exp(-kt^n) \quad (7)
\]

where \( n \) and \( k \) are the Avrami constants that take into account the mechanism of nucleation and the shape of crystal growth. However, to determine at each temperature a characteristic time for the isothermal crystallization, the Avrami equation has been rewritten here as a phenomenological Kohlraush–Williams–Watts (KWW) equation:\(^{28}\)

\[
\chi_c(t) = 1 - \exp \left( -\left( \frac{t}{\tau_{cr}} \right)^b \right) \quad (8)
\]
where \( t_{cr} \) is the characteristic crystallization time and \( b \) is a constant. These constants are obviously connected to the Avrami parameters by the relationships

\[
 t_{cr} = \frac{k}{C_0^{1/n}} \quad \text{and} \quad b = n.
\]

For each temperature, the characteristic crystallization time was determined from the nonlinear least square KWW fits of the time dependence of the degree of crystallinity. The accuracy of fits \((R^2 > 0.996)\) can be seen in Figure 10, where solid lines represent the recalculated time dependence of \( \xi_c(t) \).

The temperature dependence of the characteristic crystallization time, \( \tau_{cr} \), as a function of reciprocal temperature is shown in Figure 11. A clear trend is noted for the \( \tau_{cr} \) parameter, and, as expected, the characteristic time is reduced at higher temperatures. Even if data points are somewhat scattered due to experimental uncertainties, the temperature dependence of the characteristic crystallization time can be described by Arrhenius behavior (eq. 2) that is characterized by an activation energy of 81.5 kJ \( \cdot \) mol\(^{-1} \) \( (R^2 = 0.91) \).

After all isothermal crystallization experiments, the crystallized sample was recovered and gently ground to obtain a fine powder so that its XRPD diffractogram could be recorded at room temperature (data not shown). No amorphous background was noted on the diffractograms acquired for material that had been subjected to any of the employed crystallization temperatures. This result is in agreement with DDS results, indicating that the crystallization was completed after the considered crystallization time. As expected, the B crystalline form was obtained during the isothermal crystallization of the amorphous SSR performed at temperatures >120°C. For temperatures <120°C, a mixture of both A and B crystalline forms was observed, with an increasing A/B ratio as the temperature was decreased. At 100°C, the XRPD spectrum was largely representative of the A crystalline form. These results are in agreement with the theoretically calculated temperature of the solid–solid transition between the two crystalline forms. It is important to note that the temperature dependence of the characteristic crystallization time \( \tau_{cr} \) was unaffected, whatever the form or the mixture of forms obtained during the isothermal crystallization in the dielectric cell. The latter result is consistent with the physical meaning of \( \tau_{cr} \), which represents the characteristic time of the vanishing of amorphous phase during the crystallization and consequently the characteristic time of the global apparition of crystal phases whatever the crystalline form. In this context, the KWW phenomenological expression that is used here to extract a characteristic time for the isothermal crystallization of amorphous phase remains valid for temperatures <120°C, where mixtures of both A and B crystalline forms were observed.

**DISCUSSION**

**Molecular Mobility: Complementary Nature of DDS and TSC Techniques**

The molecular mobility specific of the amorphous SSR drug was studied in a wide temperature and frequency range by both DDS and TSC techniques. The temperature dependencies of relaxation

![Figure 10](image1.png)

**Figure 10.** Time dependence of the degree of crystallinity (symbols) of SSR drug during isothermal crystallization performed at different temperatures between 100 and 140°C at steps of 5°C. Solid lines correspond to KWW fit of \( \xi_c(t) \) according to eq. 10.

![Figure 11](image2.png)

**Figure 11.** Temperature dependence of the characteristic crystallization time \( \tau_{cr} \).
times determined by DDS and TSC were superimposed on the same Arrhenius diagram (Fig. 4). The double vertical arrows on the right-hand side of Figure 4 represent the accessible excitation frequency range of both TSC and DDS experiments. It is evident that the TSC technique allows the study of the dynamics of the sample in the very low frequency range (i.e., a very long time range between $10^3$ and $10^4$ s).

As already mentioned, the $\beta_a$-relaxation mode associated with localized molecular motions involves Arrhenius dynamics over the entire temperature range. The low activation energy and the pre-exponential factor that characterize the $\beta_a$-relaxation process (compare with Table 1) are specific to small size species that relax independently from each other. Further experiments based on solid-state carbon-13 nuclear magnetic resonance ($^{13}$C NMR) measurements have been scheduled to characterize in detail the dipolar groups involved in this relaxation. Some complementary dielectric analyses are also necessary to investigate the distribution of dynamics involved in the $\beta_a$-relaxation mode and to thereby access the local density distribution of the SSR amorphous phase.

As shown in Figure 4, at very high temperatures and in the very short time range, the $\alpha_a$-relaxation time diverges rapidly from the $\beta_a$ dynamics as the temperature decreases. This phenomenon, currently observed for fragile glass-forming systems and well known as the bifurcation of the $\alpha\beta$ relaxation process, is related to the increasing cooperativity specific to molecular motions involved in the $\alpha_a$-relaxation mode as the temperature decreases. Indeed, when the temperature is reduced, important hindrances affect the larger species involved in the $\alpha_a$-relaxation, implying their VFT dynamics and thus the observed bifurcation.

Contrary to the dynamics of species implied in secondary $\beta_a$-relaxations, which obey Arrhenius behavior over the entire frequency–temperature range probed by TSC and DDS, a change in the dynamics of molecular motions in the main $\alpha_a$-relaxation process of amorphous SSR was noted at $T_g$ (Fig. 12). Indeed, whereas relaxation times derived from the TSC-FP analyses of molecular dynamics involved in the $\alpha_a$-relaxation process exhibit Arrhenius temperature behavior, that determined by DDS shows VFT temperature dependence. We note that the crossover between the VFT and the Arrhenius behaviors takes place in a temperature range centered around the $T_g$ detected by DSC and in the time range located around 100 s. The variation of the $\alpha_a$-relaxation temperature behavior was observed several years ago from mechanical, viscosity, and dielectric measurements on many glass-forming materials. This variation seems to be universal for fragile systems exhibiting VFT temperature behavior for $T > T_g$, and corresponds to the crossover from the equilibrium liquid state (system in a ergodic state for $T > T_g$) to the out-of-equilibrium glassy state (system in a nonergodic state for $T < T_g$) when the temperature goes through the thermodynamic glass transition domain. These results (Fig. 12) clearly show the kinetic nature of the dynamic glass transition by showing the change in terms of kinetics law occurring at $T_g$. In fact, $T_g$ represents the temperature at which the ergodic-to-nonergodic transition takes place by decreasing the temperature.

The physical interpretation of the VFT, the Arrhenius dynamics, and the crossover between them has been made in relation to the Adam and Gibbs (AG) model. For $T > T_g$, the sharp increase of the apparent activation energy, $E$ (related to $d[\log(\tau)]/d(1/T)$), of the $\alpha_a$ dynamics as the temperature decreases has been explained by a continuous establishment of the cooperativity between the involved molecular motions. In this context, the thermodynamic AG model assumes that amorphous systems comprise a large number of CCRs. These domains, based on species that relax in the same cooperative way, are considered independent from each other. The AG model suggests the following expression for the relaxation
time of species involved in the main $\alpha$-relaxation mode:
\[
\tau(T) = \tau_0 \exp\left( \frac{N_A S^*_c \Delta \mu}{k_B T S_c(T)} \right) \tag{9}
\]
where $\Delta \mu$ is the individual potential energy barrier; $S^*_c$ is the configurational entropy of the minimum number of species able to rearrange [suggested for polymers to be $S^*_c = k_B \ln(3!)^{45}$]; $S_c(T)$ is the macroscopic configurational entropy, which is related to the total number of configurational states accessible to the sample; and $N_A$ is Avogadro’s number. Recent work carried out with different techniques shows that the size of CRRs is at a minimum at very high temperature (in the $\alpha\beta$ regime) and increases by coalescence of small CRRs when the temperature decreases to $T_g^{39,40,46}$. The system becomes more and more cooperative, and the configurational entropy $[S_c(T)]$ decreases continuously as the temperature decreases.\textsuperscript{42,44} Based on experimental observations and on a thermodynamic approach, the following expression of the configurational entropy has been proposed for temperatures $> T_g$:\textsuperscript{47}
\[
S_c(T) = T_g \Delta C_p(T_g) \frac{T - T_0}{T T_0} \tag{10}
\]
where $\Delta C_p(T_g)$ is the isobaric heat capacity step at $T_g$ and $T_0$ is the temperature at which $S_c$ vanishes, which is referred to in the literature as the Kautzmann temperature. Using eq. 10, eq. 9 for the relaxation time proposed in the AG model can be rewritten as follows:
\[
\tau(T) = \tau_0 \exp\left( \frac{N_A S^*_c \Delta \mu}{T_g \Delta C_p T_g k_B (T - T_0)} \right) \tag{11}
\]
Equation 11 can take the VFT form (eq. 3) by considering $B = N_A S^*_c \Delta \mu/T_g (T_g \Delta C_p T_g k_B)$ and $\tau_{0v} = \tau_0$.
At $T_g$, the cooperativity of molecular motions is so significant that large size CRRs occupy the entire system, which then becomes frozen. The number of CRRs at $T_g$ is at a minimum, and the large volume of CRRs reaches an out-of-equilibrium constant value for temperatures $< T_g$. This situation imposes a constant value, $S_c(T_0)$, for the macroscopic configurational entropy. The value $S_c(T_0)$, which verifies eq. 10, is dependent on the fictive temperature, $T_f$, introduced by Tool\textsuperscript{48} and can only be affected by ageing time applied on the sample in the glassy state before measurements. Below $T_g$, the relaxation time introduced in the AG model (eq. 9) can then be written as:
\[
\tau(T) = \tau_0 \exp\left( \frac{N_A S^*_c \Delta \mu}{k_B T S_c(T)} \right) \tag{12}
\]
This relaxation time corresponds to the time scale of molecular motions involved in the $\alpha$-relaxation mode for the amorphous phase in the glassy state at a given physical ageing state that is taken into account by the fictive temperature $T_f$. Different relaxation times $\tau_{FP}$ determined by the TSC-FP method below $T_g$ correspond to the time scale of the relaxing species located in the different CRRs that have different constant size. The TSC-FP method, therefore, can be used to characterize the distribution of constant size CRRs below $T_g$.
For temperatures $< T_g$, CRRs increase with the ageing time to reach their equilibrium size, which is not acquired during the cooling. The evolution of the size of CRRs is in fact related to the evolution of the environment of relaxing species, which is often referred as the structural relaxation of amorphous phase. The fictive temperature $T_f$ and the $S_c$ parameter values have decrease with the ageing time.\textsuperscript{42,44} From these evolutions, the relaxation time $\tau$ of molecular motions then becomes time dependent (through $T_f$ and $S_c$ in eq. 12), and their activation energies $[E = N_A S^*_c \Delta \mu/S_c(T)]$ increase with the ageing time. The time scale of the evolution of $T_f$, $S_c$, or of the relaxation time $\tau$ of molecular motions may be interpreted as the structural relaxation time, $\tau_r$. As described elsewhere,\textsuperscript{19,20} the structural relaxation time $\tau_r$ can be determined by DSC aging experiments by measuring the enthalpy recovery after storage for different periods at different temperatures. However, the structural relaxation time $\tau_r$ cannot be identified as molecular mobility unequivocally related to specific relaxing species. Consequently, the structural relaxation time $\tau_r$ determined below $T_g$ and the relaxation time $\tau$ of molecular motions involved in the $\alpha$-relaxation mode (Arrhenius or VFT, below and above $T_g$, respectively) cannot be connected themselves at $T_g$ in the same Arrhenius diagram.

The AG model, almost unanimously accepted to describe the dynamics of glass-forming systems over a wide time–temperature range, gives the physical meaning of dynamics behavior relationships in addition to the VFT–Arrhenius crossover specific to the molecular mobility involved in the $\alpha$-relaxation mode. These results indicate the obvious complementary nature of the DDS and TSC dielectric techniques; that is, DDS allows characterization of the molecular mobility of SSR amorphous phase in the liquid state for...
temperatures $>T_g$, and the TSC technique is particularly suitable to study molecular motions in the glassy state for temperatures $<T_g$.

**Correlation between Molecular Mobility and Isothermal Crystallization Kinetics**

To find a possible correlation between the molecular mobility of the SSR drug substance in amorphous form and the kinetics of its isothermal crystallization, the relaxation time of the different molecular motions specific to the amorphous phase and the characteristic isothermal crystallization time were reported on the same Arrhenius diagram (Fig. 13).

Even if the crystallization time is more affected than the molecular mobility by experimental uncertainties, the first point to be noted from Figure 13 is the significant difference between the VFT dynamics of molecular motions involved in the $\alpha_a$-relaxation mode at temperatures $>T_g$ and the Arrhenius temperature dependence of the $\tau_{cr}$ crystallization time in the same temperature range. This first observation seems to exclude any direct correlation between the $\alpha_a$-relaxation and the isothermal crystallization kinetics. However, to confirm this conclusion, it is necessary to perform some additional isothermal crystallization measurements below $T_g$. This approach will, first, increase the analysis temperature range of crystallization analysis and thereby achieve better accuracy for the determination of its behavior, and second, determine if the characteristic crystallization time exhibits a VFT–Arrhenius crossover as is the case for the molecular mobility. For temperatures $<T_g$, the real-time *in situ* DDS measurements appear to be prohibited because of the displacement of the $\alpha_a$-relaxation mode in a frequency range that is inaccessible for this dynamic experiment. In addition, it is an inefficient use of experimental time to study this temperature range. A new method based on the high resolution of the TSC technique is in development and could avoid this difficulty.

The main interesting point observed in Figure 13 is the connection that can be made between the Arrhenius temperature dependence of the $\beta_a$-relaxation mode and the crystallization time $\tau_{cr}$. The dynamics of the $\beta_a$-relaxation mode was analyzed by DDS in the $-155$ to $-40^\circ C$ temperature range. One of the main characteristics of the secondary $\beta_a$-relaxation is to keep the same Arrhenius dynamics over the entire range of temperatures (above and below $T_g$). This behavior is related to the localized nature of involved molecular motions that are unaffected by the glass transition of amorphous phase. The temperature behavior law of the $\beta_a$-relaxation time, therefore, can be legitimately extrapolated in the temperature range in which the isothermal crystallization of amorphous phase was analyzed. In the $100$–$140^\circ C$ temperature range, the two nearly parallel behavior laws associated with the $\beta_a$-relaxation time and the characteristic crystallization time indicate that the molecular motions involved in the $\beta_a$-relaxation mode participate in the mechanism of the crystal growth characterized by the crystallization time $\tau_{cr}$. This result suggests that due to their intramolecular motions, molecules localized in the amorphous phase very near to the crystal surfaces can adjust their local conformation to allow their inclusion in the neighboring crystallite. Based on a very different method, a similar conclusion was made by Hikima et al. regarding the isothermal crystallization of triphenylethylene. In this case, the microscopic investigation carried out in the glass transition region showed that the isothermal crystallization was controlled by the molecular motions involved in the $\beta_a$-process and not by that involved in the $\alpha_a$-relaxation mode.

**CONCLUSIONS**

In the first part of this paper, the molecular mobility of the amorphous form of SSR was
thoroughly analyzed over wide frequency and temperature ranges using both DDS and TSC dielectric techniques. Two relaxation processes, with dynamics specific to glass-forming complex systems, were identified for the amorphous SSR. The secondary $\beta_g$-relaxation mode, characterized by Arrhenius behavior over the entire accessible time–temperature range, was associated with intramolecular movements corresponding to oscillations of small dipolar groups that must be identified by solid-state NMR. The dynamics of the main $\alpha_g$-relaxation process, assigned to the dielectric manifestation of the dynamic glass transition, was described by VFT behavior law at temperatures $> T_g$ and by the Arrhenius law at temperatures $< T_g$. The physical meaning of the VFT and the Arrhenius laws and of the crossover between them at $T_g$ was explained in the context of the AG model by the temperature dependence of the size of CRRs, which govern the time scale of molecular movements involved in the $\alpha_g$-relaxation mode. DDS and TSC behaved as complementary techniques, giving original information on the intramolecular and molecular mobility in disordered phases over a wide temperature range, above and below $T_g$.

In the second part of the manuscript, the isothermal crystallization kinetics of the amorphous form of SSR was analyzed at different temperatures with real-time in situ dielectric measurements. Whatever the crystalline form obtained from these experiments, the decrease of the dielectric response of the amorphous phase was recorded as a function of time. The characteristic crystallization time was determined by KWW analyses of the time dependence of the degree of crystallinity. The characteristic crystallization time followed an Arrhenius temperature dependence in the supercooled liquid state ($T > T_g$).

Based on the comparison of the behavior laws specific to the molecular mobility of amorphous phase and the characteristic crystallization time, it is concluded that, above $T_g$, the crystal growth of the SSR is controlled by the intramolecular movements involved in the $\beta_g$-relaxation mode independently from the molecular mobility responsible for the $\alpha_g$-relaxation.

To confirm the correlation observed between the intramolecular mobility of amorphous phases and the crystallization kinetics of these disordered phases, and to thereby highlight the mechanism of crystallization, it would be interesting to explore the temperature range $< T_g$. The aim of this research was obviously to predict the temperature dependence of the crystallization kinetics from the knowledge of the different behavior laws that govern the molecular mobility of amorphous phase. The influence of specific physical interactions with excipients on the molecular mobility of amorphous drugs and the subsequent influence on the crystallization kinetics will be the next fundamental point to be considered in future dielectric investigations. The results of such studies will help in the preparation of specific pharmaceutical formulations that stabilize drugs in the amorphous state, which is well suited to some clinical purposes.

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REFERENCES


