

# MAP 3

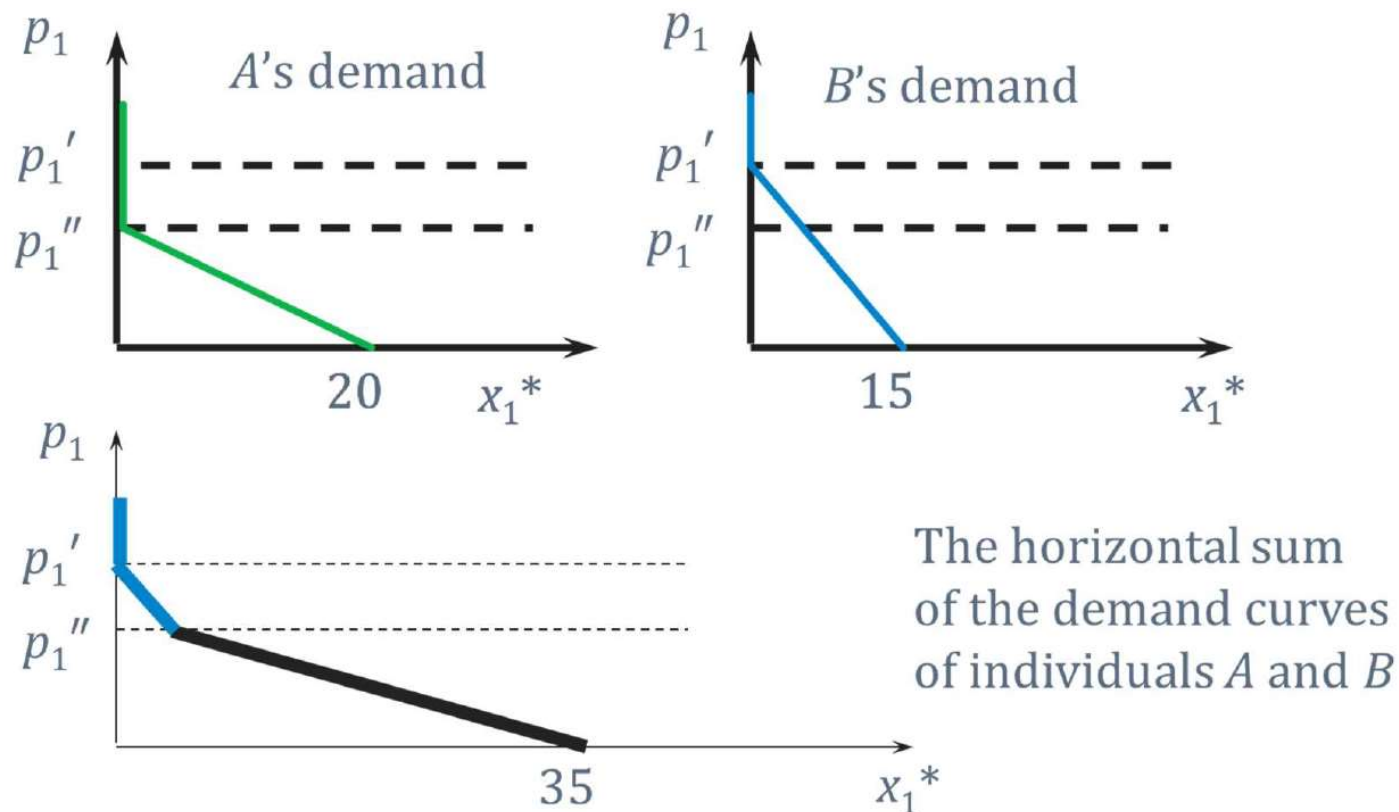
Utility, Choice, Market Demand

EARN

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The market inverse demand curve for any good is

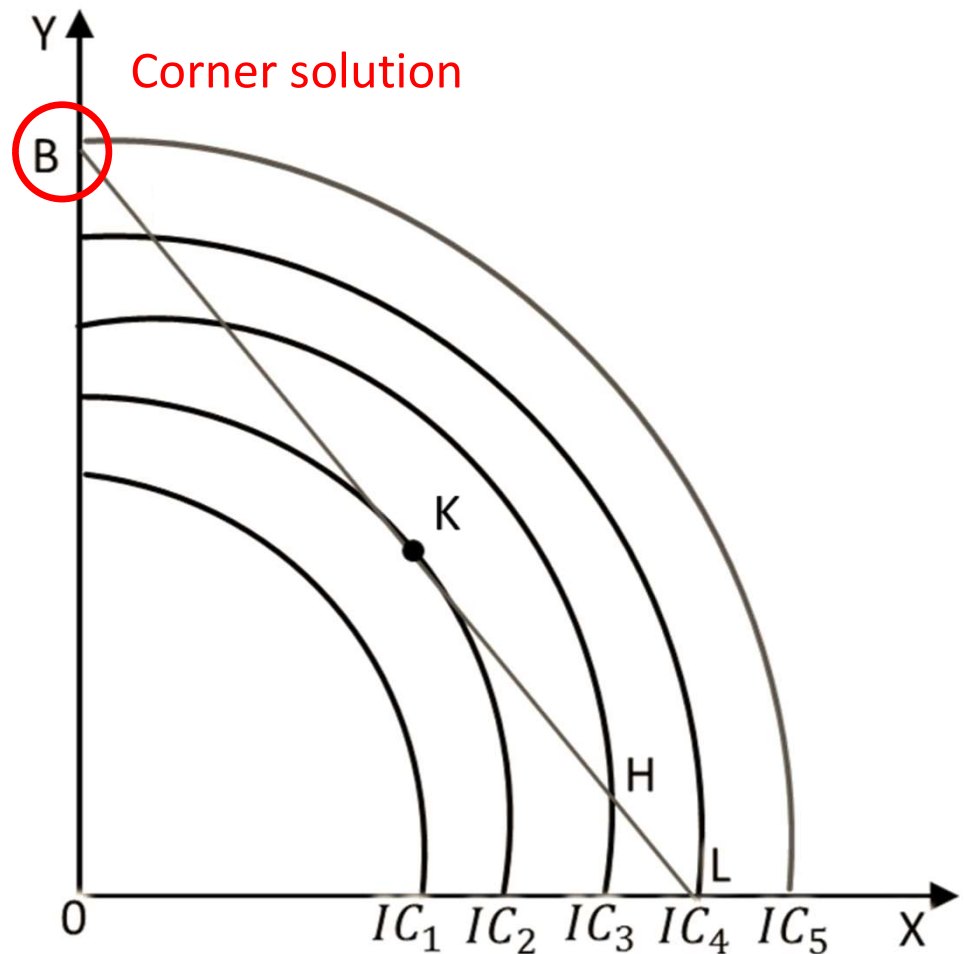
- Independent of individuals' inverse demand curves for the good.
- The vertical summation of individuals' inverse demand curves (along price axis).
- The horizontal summation of individuals' inverse demand curves (along quantity axis).**
- Derived from the firm's marginal cost of production.



In the figure below, X and Y are both goods. Which point represents the most preferred affordable bundle?

- a. B.
- b. L.
- c. K.
- d. H.

Correct answer.



Suppose an individual's utility is given by a Cobb-Douglas utility function  $U(x, y) = x \cdot \sqrt{y}$ . With a bundle of goods A  $(x, y) = (4, 16)$  his utility is  $U(4, 16) = 4 \cdot \sqrt{16} = 16$ . With a bundle B  $(x, y) = (4, 4)$  his utility is  $U(3, 4) = 4 \cdot \sqrt{4} = 8$ . Then:

- a. The individual is indifferent between bundle A and bundle B.
- b. Bundle A is twice as costly as bundle B.
- c. Bundle A is preferred twice as much as bundle B.
- d. Bundle A is preferred to bundle B.**

## Utility Functions – 3

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Utility is an ordinal (i.e. ordering) concept.

- E.g., if  $u(x) = 6$  and  $u(y) = 2$  then bundle  $x$  is strictly preferred to bundle  $y$ . But  $x$  is not preferred three times as much as is  $y$ .

Suppose that a consumer has Cobb-Douglas preferences, expressed as  $U(X, Y) = X^a \cdot Y^b$ . The marginal utilities for goods  $X$  and  $Y$  are, respectively,  $a \cdot X^{a-1} \cdot Y^b$  and  $b \cdot X^a \cdot Y^{b-1}$ . The same consumer has a budget  $m$  that can be spent on either  $X$  or  $Y$ . The price for  $X$  is  $p_X$ , and the price for  $Y$  is  $p_Y$ . Which of the answers below does not correspond to the system of equations that should be solved to give the consumer's optimal choice?

$$a. \begin{cases} -\frac{a \cdot X^{a-1} \cdot Y^b}{b \cdot X^a \cdot Y^{b-1}} = -\frac{p_X}{p_Y} \\ m = p_X \cdot X + p_Y \cdot Y \end{cases}$$

$$b. \begin{cases} -\frac{a \cdot X^{a-1} \cdot Y^b}{b \cdot X^a \cdot Y^{b-1}} = \frac{p_X}{p_Y} \\ m = p_X \cdot X + p_Y \cdot Y \end{cases}$$

$$c. \begin{cases} a \cdot p_Y \cdot Y = b \cdot p_X \cdot X \\ m = p_X \cdot X + p_Y \cdot Y \end{cases}$$

$$d. \begin{cases} Y = \frac{b}{a} \cdot \frac{p_X}{p_Y} \cdot X \\ X = \frac{m}{p_X} - \frac{p_Y}{p_X} \cdot Y \end{cases}$$

Slope of the indifference curve is equal to slope of the budget constraint:

$$MRS = -\frac{MU_X}{MU_Y} = -\frac{p_X}{p_Y}$$

$$-\frac{a \cdot X^{a-1} \cdot Y^b}{b \cdot X^a \cdot Y^{b-1}} = -\frac{p_X}{p_Y}$$

$$\frac{a \cdot X^{-1}}{b \cdot Y^{-1}} = \frac{p_X}{p_Y}$$

$$a \cdot p_Y \cdot Y = b \cdot p_X \cdot X$$

**Correct answer.**