

Renewable Energy Resources (RER)

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Wind Energy

Chapter 4

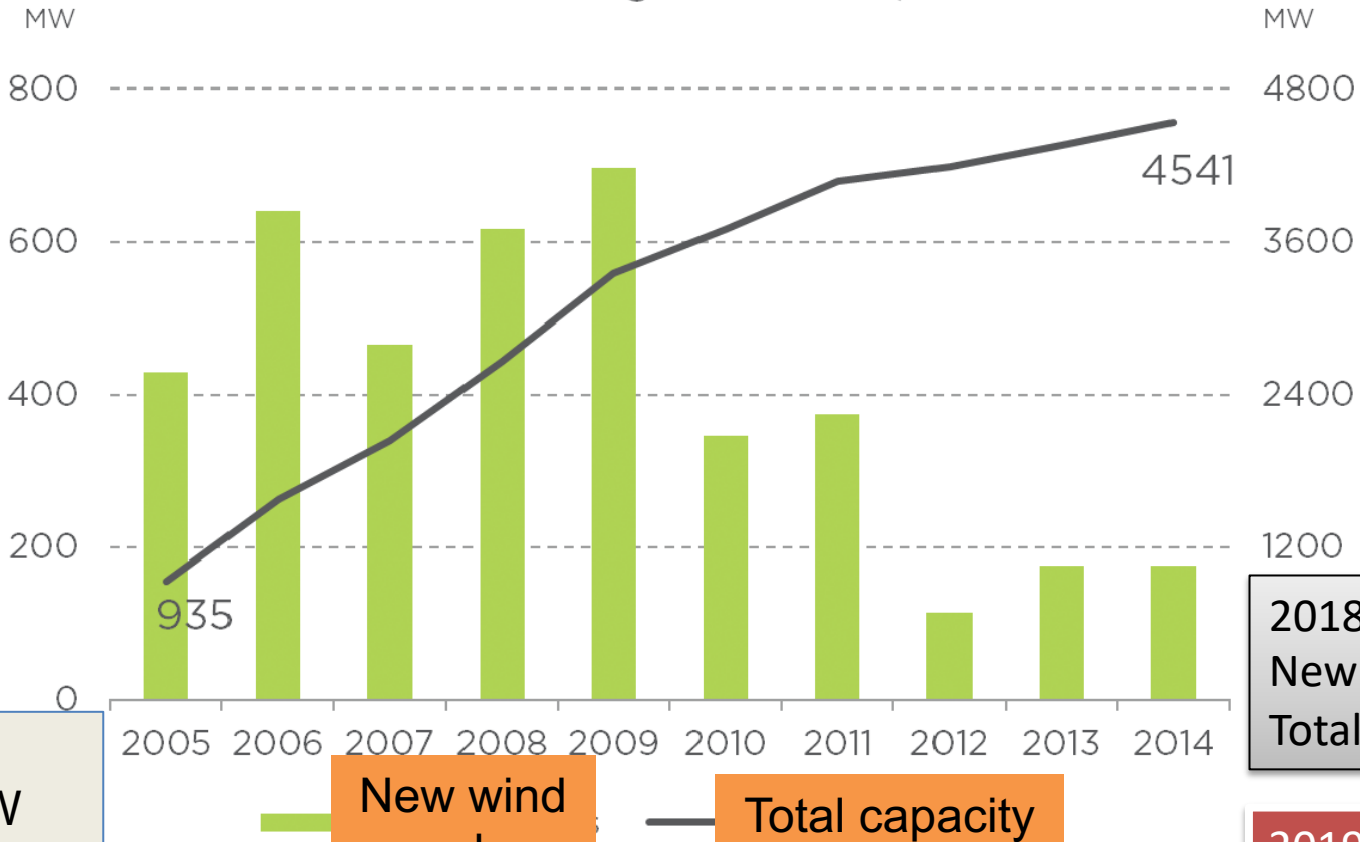
WIND FACTS AND FIGURES

Wind Power in Portugal

2016
New: 244 MW
Total: 5070 MW

2015
New: 285 MW
Total: 4826 MW

Potência Total Ligada - Evolução Anual



2018
New: 51 MW
Total: 5150 MW

2019
New: 58 MW
Total: 5208 MW

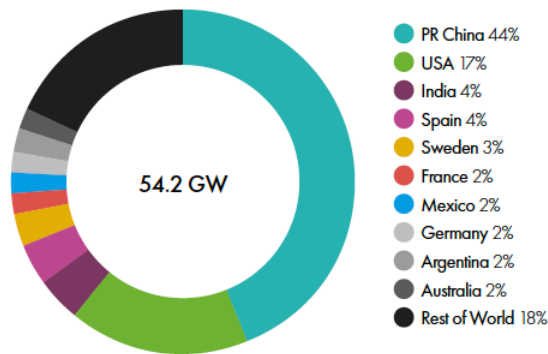
2017
New: 29 MW
Total: 5099 MW

Source: REN

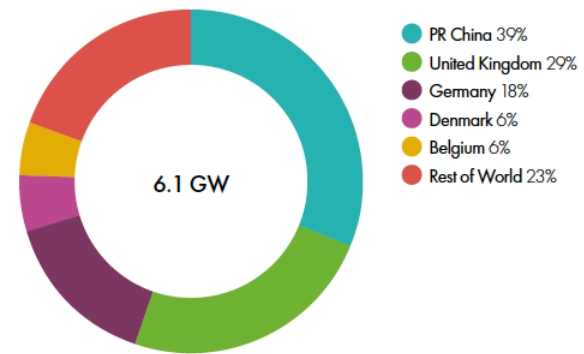
Wind Energy in the World

Top markets 2019

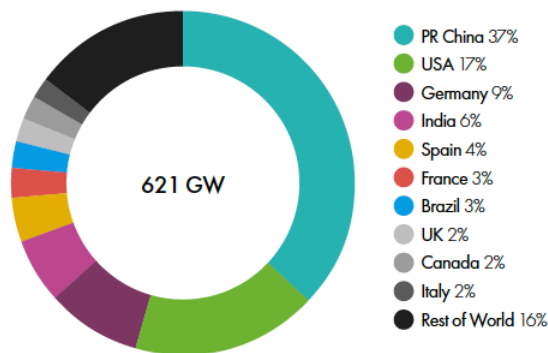
New installations onshore (%)



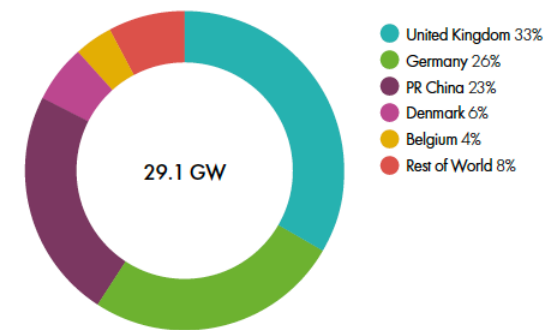
New installations offshore (%)



Total installations onshore (%)



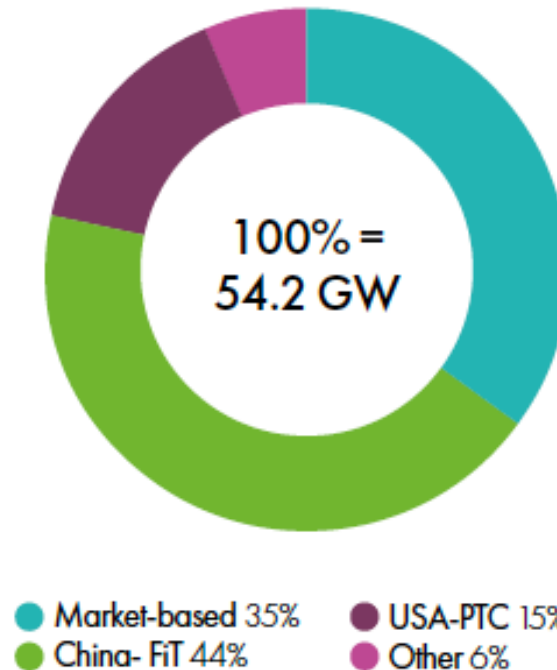
Total installations offshore (%)



Detailed data sheet available in GWEC's member only area. For definition of region, see Methodology and Definitions in the Appendix
Source: GWEC Market Intelligence, March 2020

Wind Support Mechanisms

New capacity 2019 by support mechanism
(%, onshore)



Wind LCOE

LCOE - Historic development

USD/ MWh

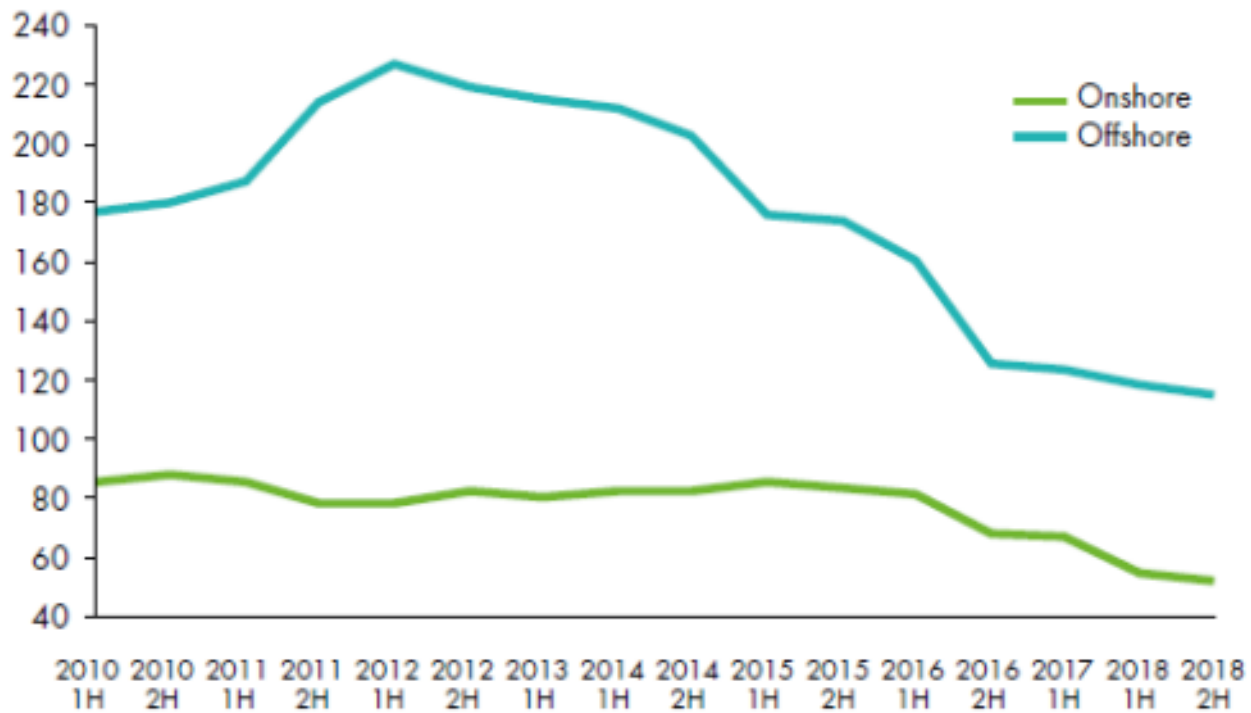
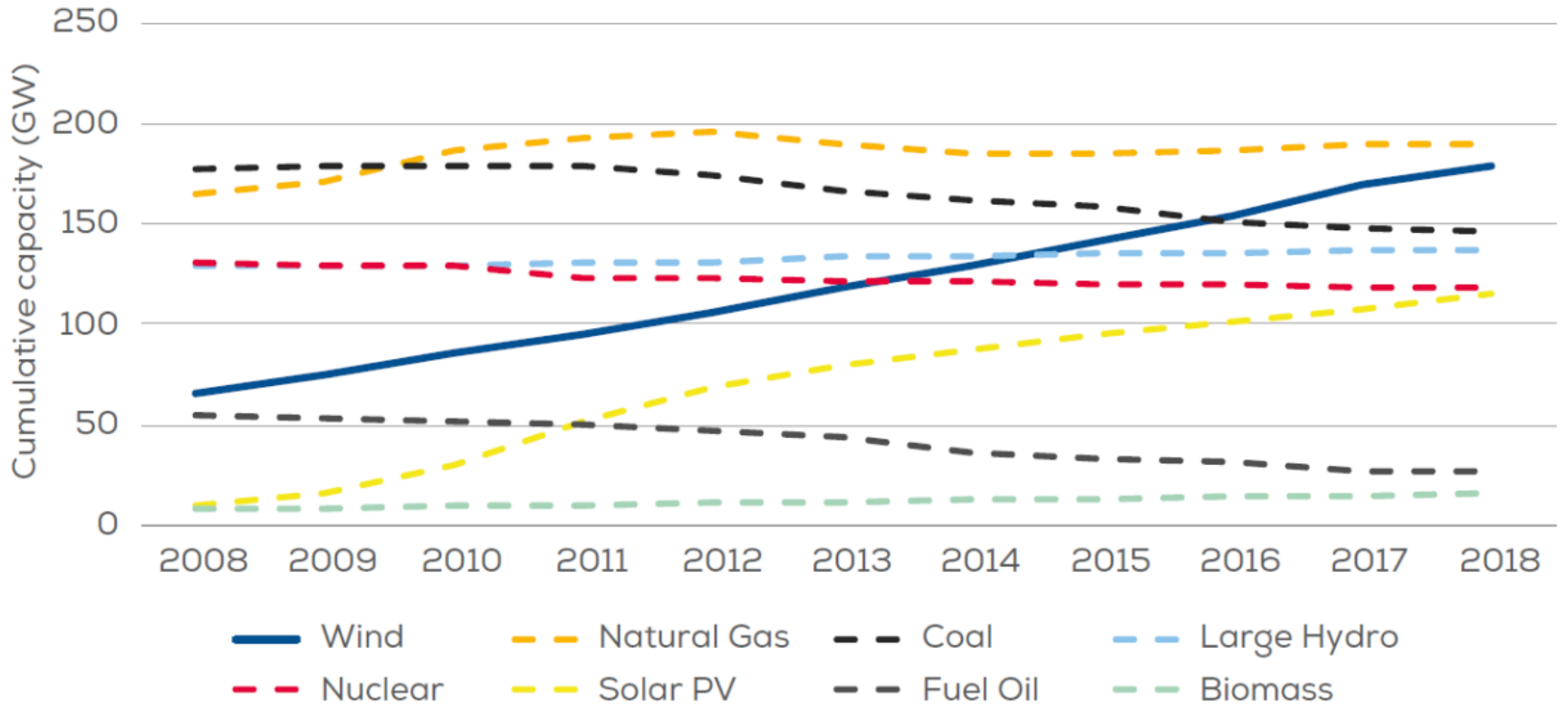


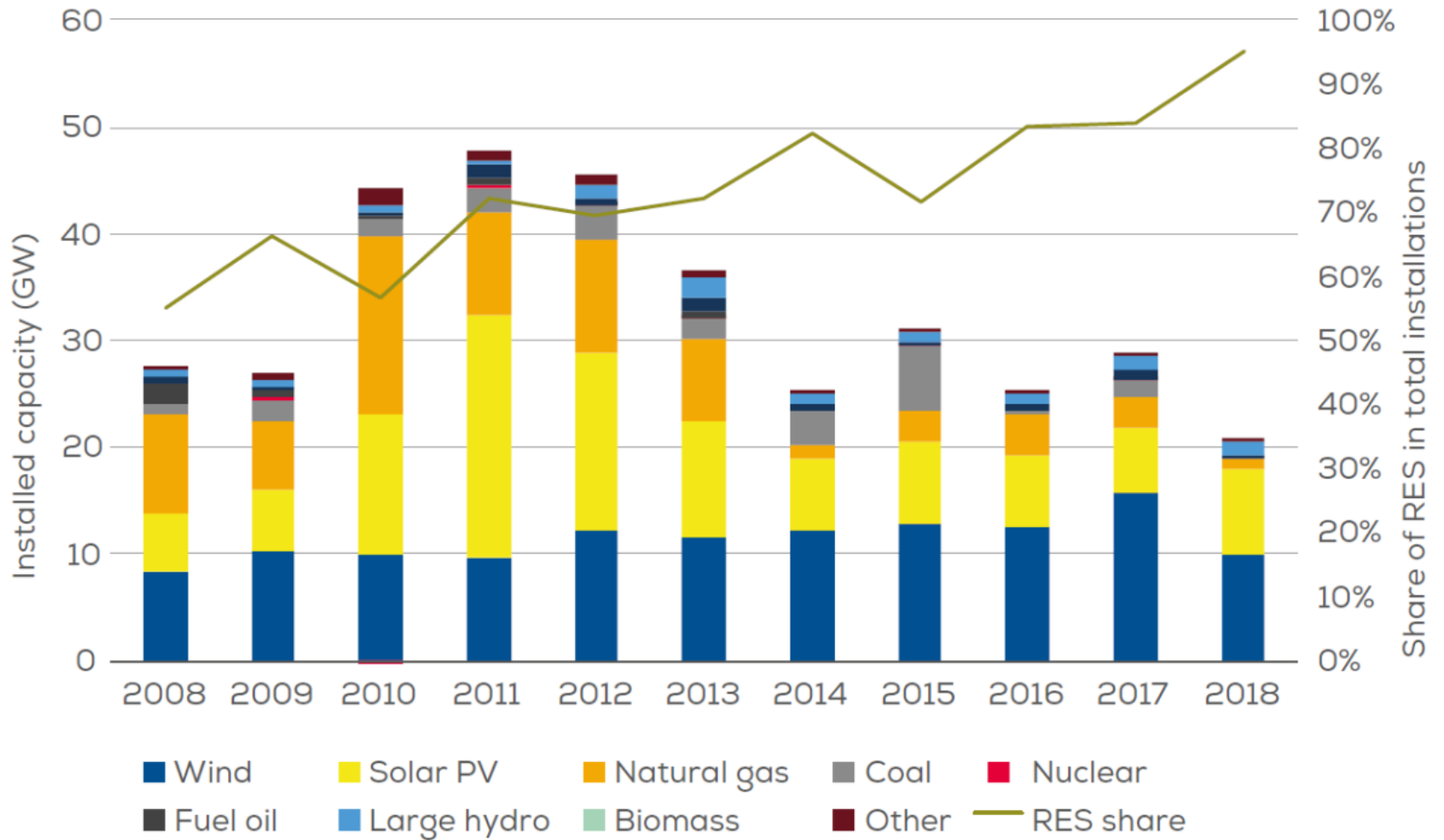
FIGURE 1
Total power generation capacity in the European Union 2008-2018



Source: WindEurope

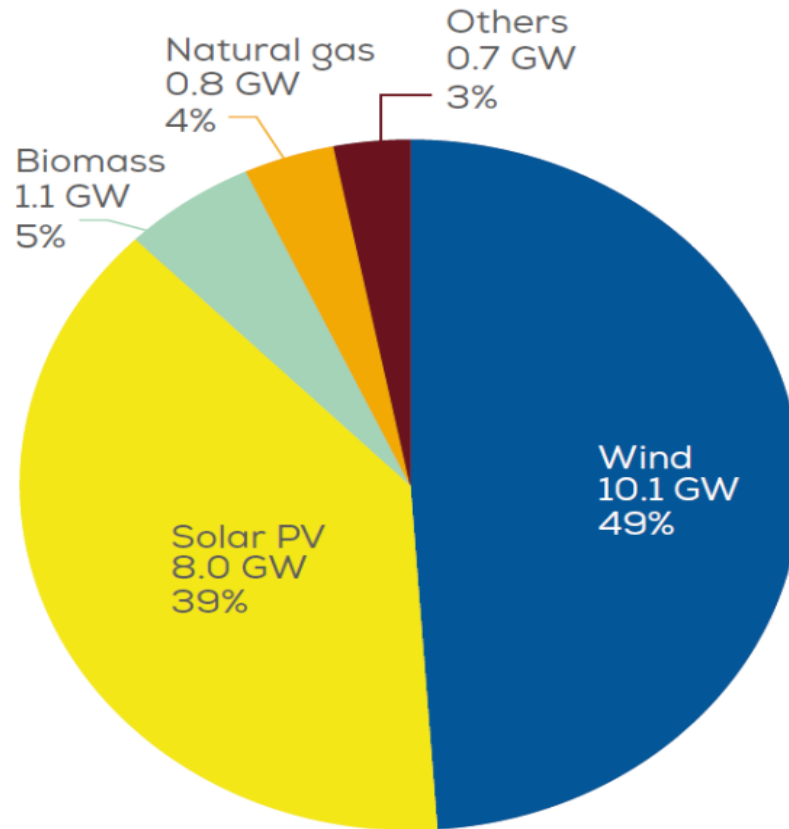
FIGURE 15

Annual installed capacity and renewable share in EU-28



Source: Wind Europe

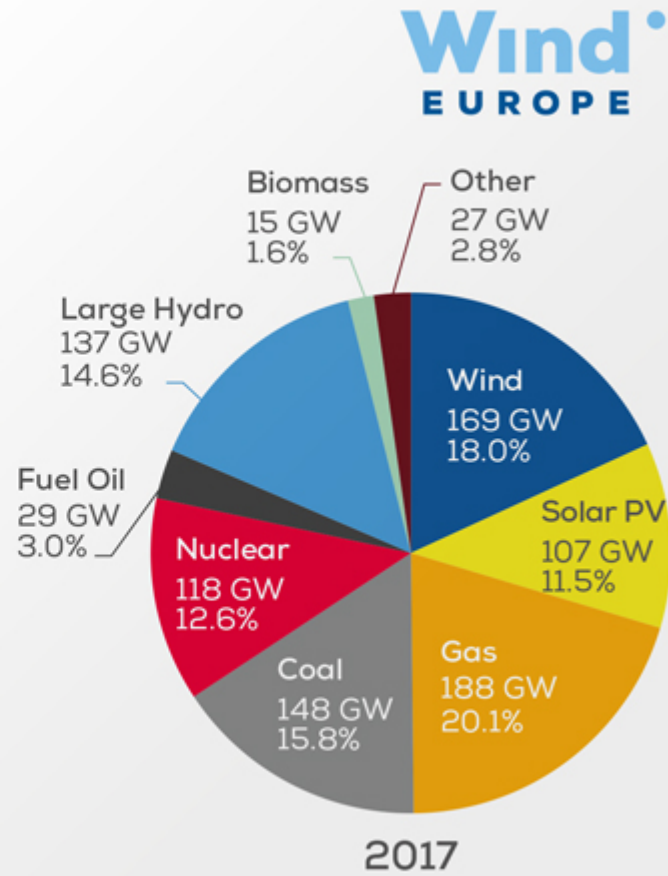
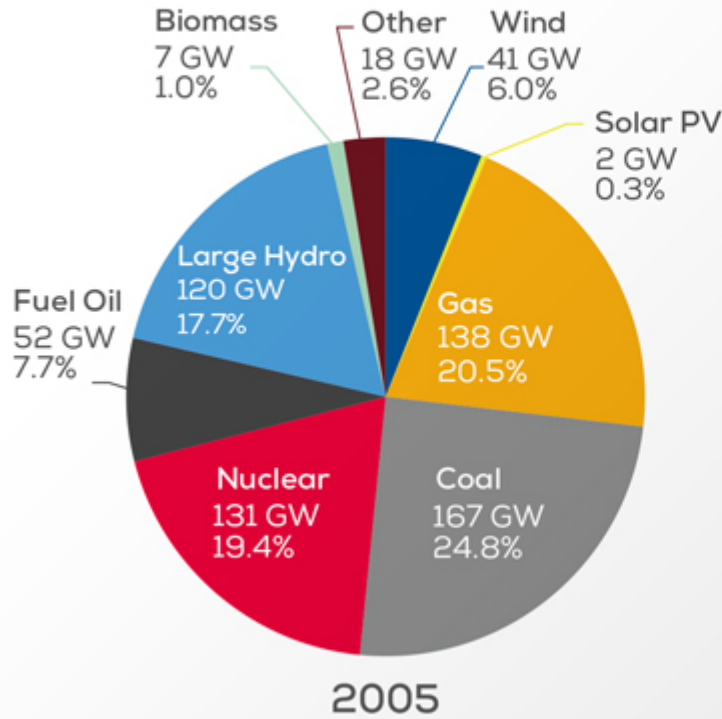
FIGURE 13
Share of new installed capacity in the EU-28



Source: Platts, SolarPowerEurope, WindEurope

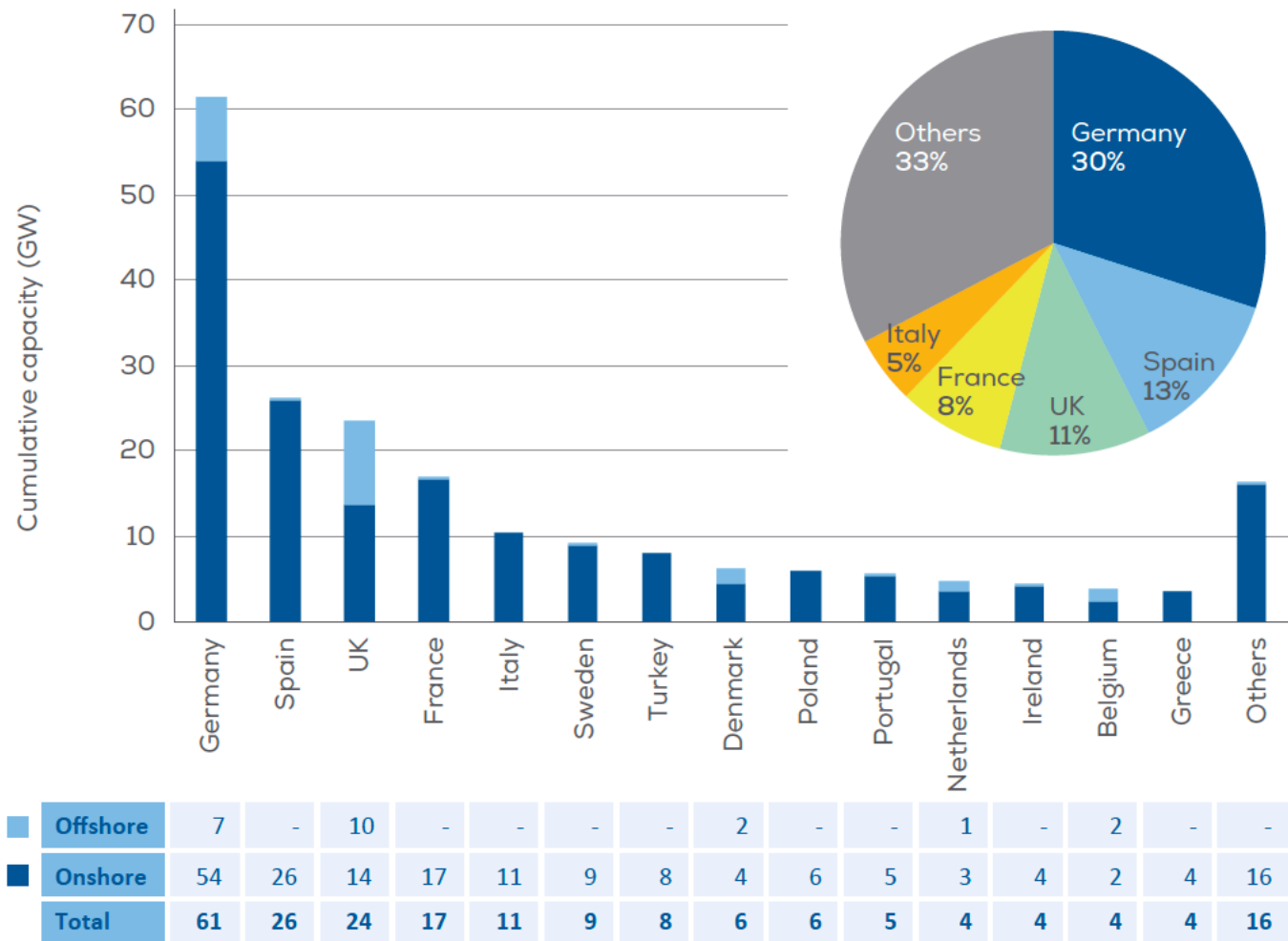
WIND IS NOW THE
2nd LARGEST POWER
 GENERATING CAPACITY
 IN THE EU

Share in installed capacity in 2005 and 2017



Source: WindEurope

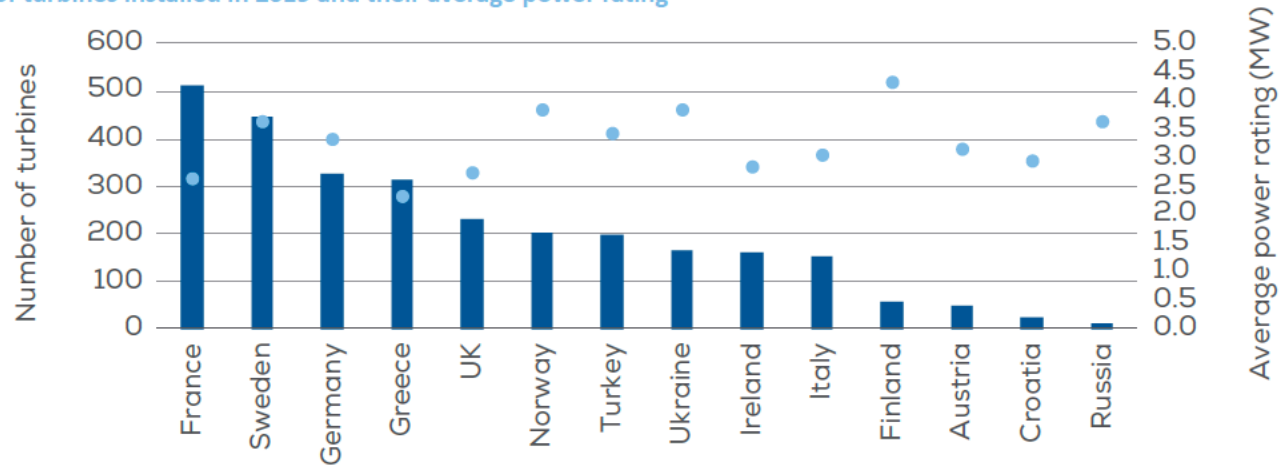
FIGURE 6
Total installed wind power capacity by country




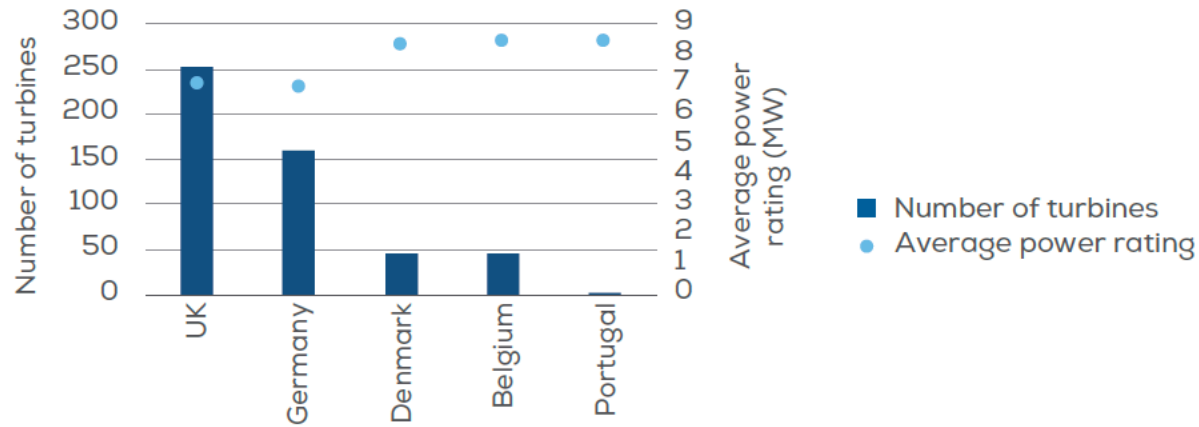
Source: WindEurope

FIGURE 10

Number of turbines installed in 2019 and their average power rating



|  | Number of turbines | 511 | 447 | 325 | 314 | 230 | 204 | 200 | 166 | 163 | 154 | 56 | 49 | 24 | 14 |
|---|----------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| | Average power rating | 2.6 | 3.6 | 3.3 | 2.3 | 2.7 | 3.8 | 3.4 | 3.8 | 2.8 | 3.0 | 4.3 | 3.1 | 2.9 | 3.6 |




|  | Number of turbines | 252 | 160 | 45 | 44 | 1 |
|---|----------------------|-----|-----|-----|-----|-----|
| | Average power rating | 7 | 6.9 | 8.3 | 8.4 | 8.4 |

FIGURE 4
Distribution of the new wind installations in Europe

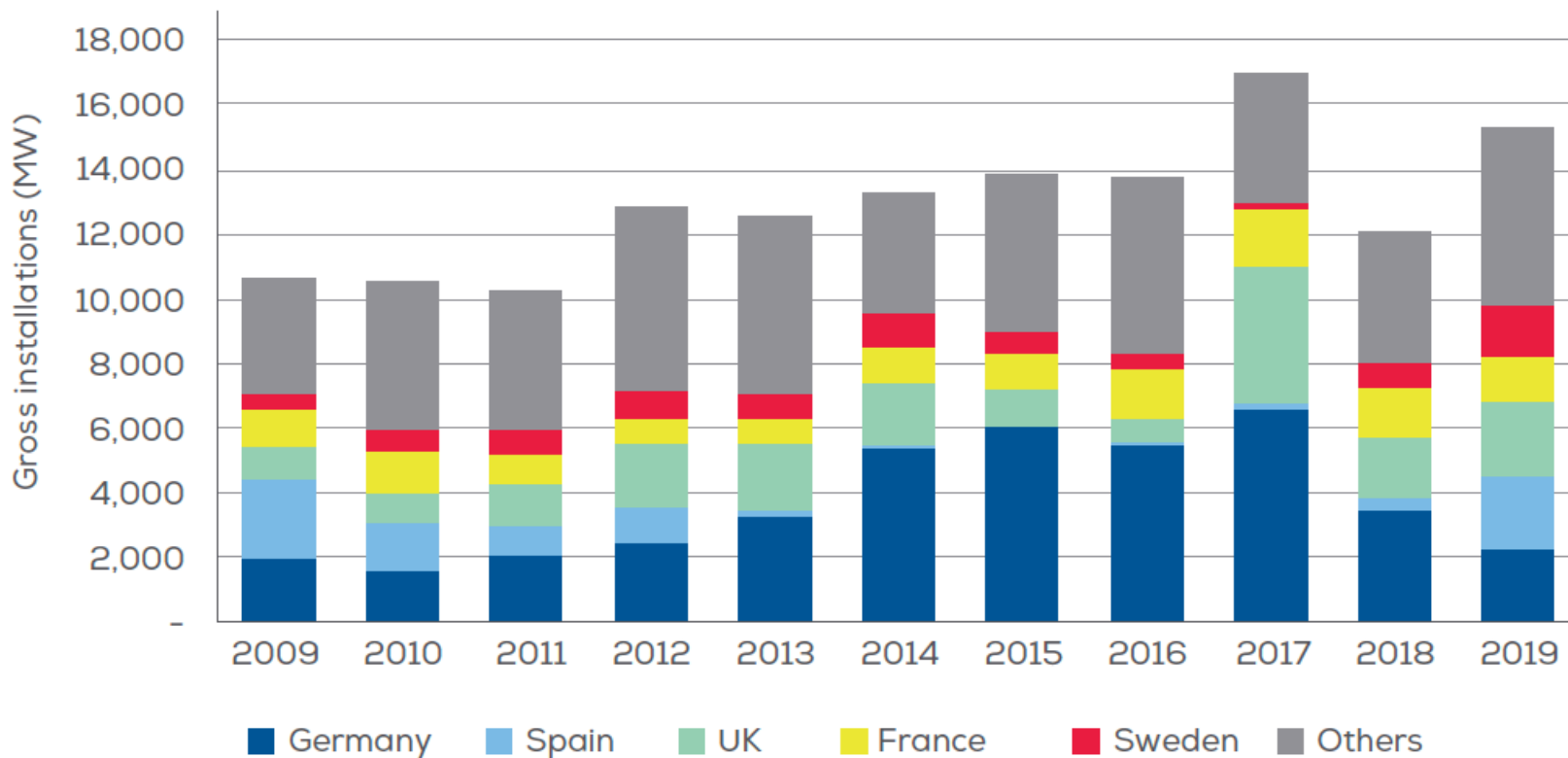
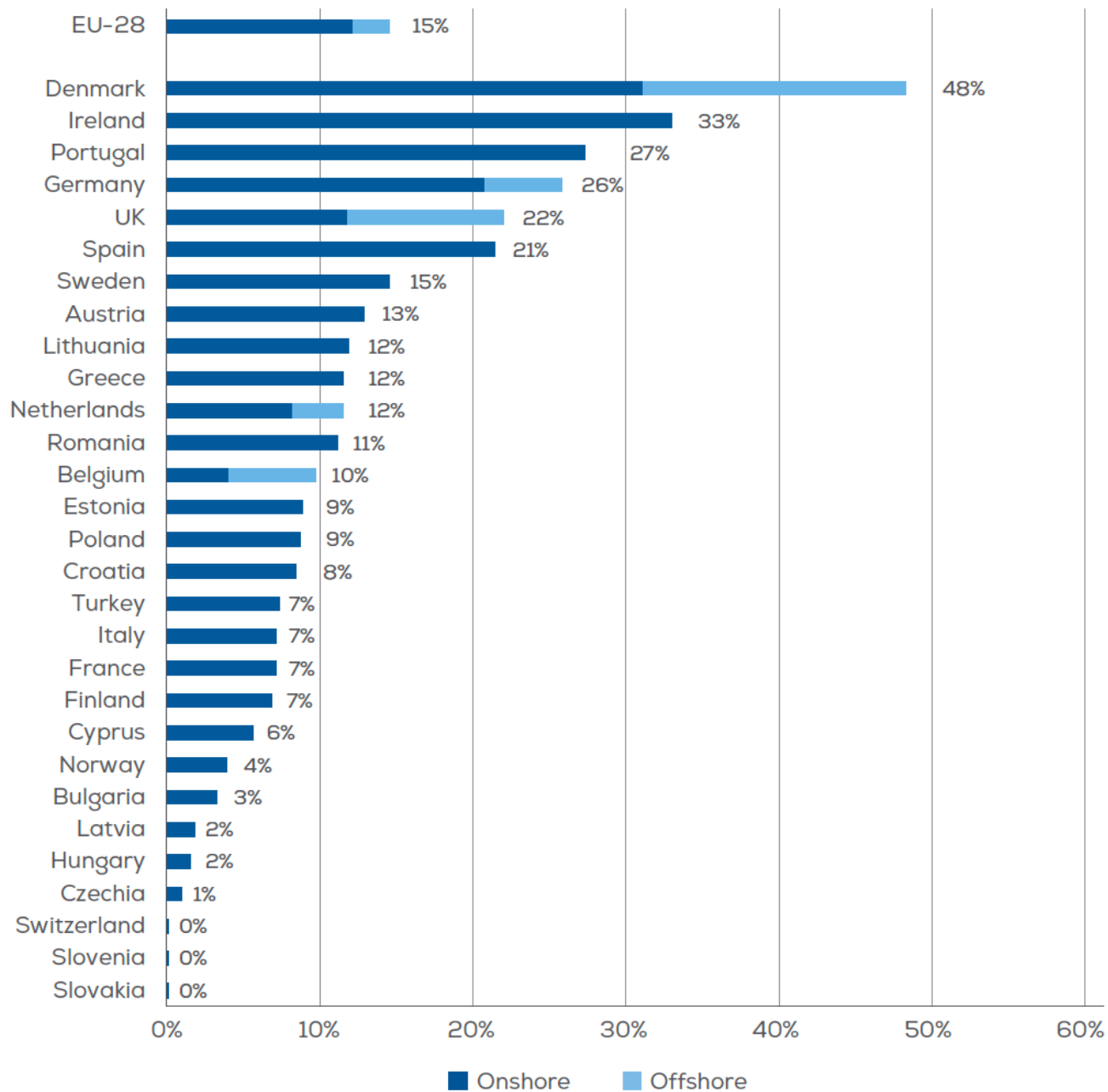


FIGURE 8


Percentage of the electricity demand covered by wind in 2019¹¹



EUROPEAN WIND ENERGY GENERATION | 2019

15%
of EU's electricity demand

26%
Average capacity factor

48% 33% 27% 26% 22%

 Highest wind energy shares

ONSHORE
170 GW
 onshore wind capacity

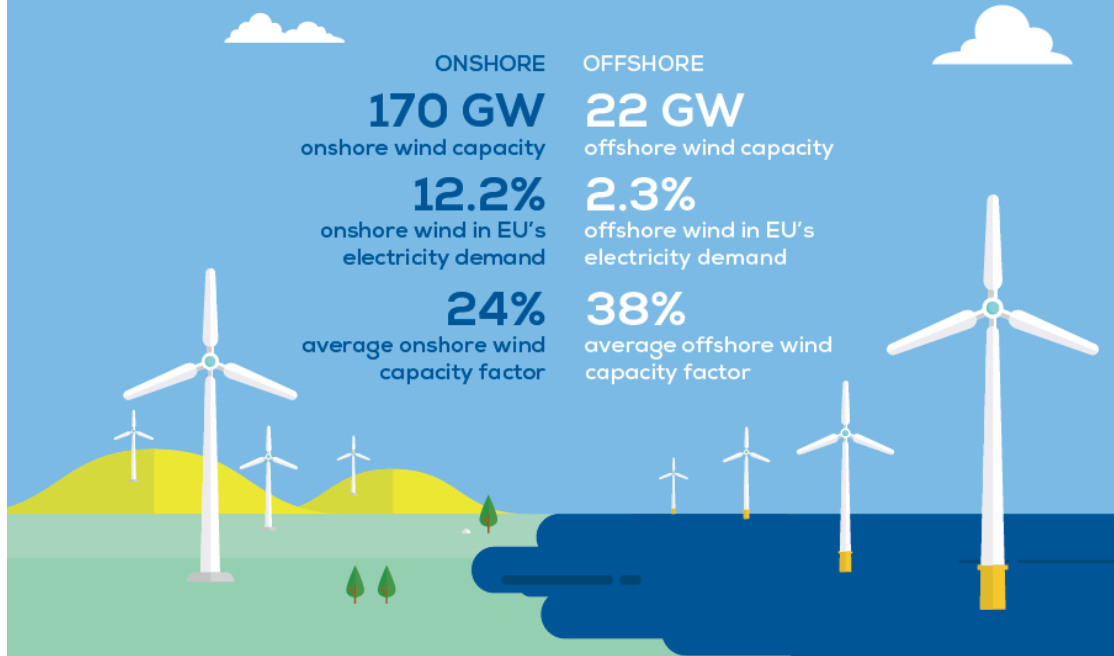
12.2%
 onshore wind in EU's
 electricity demand

24%
 average onshore wind
 capacity factor

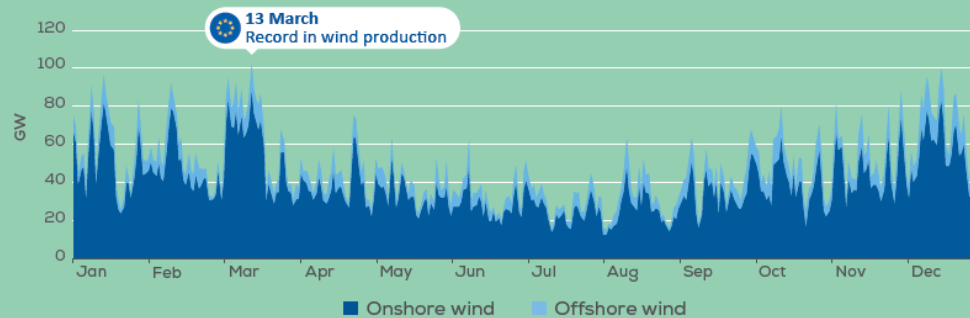
OFFSHORE
22 GW
 offshore wind capacity

2.3%
 offshore wind in EU's
 electricity demand

38%
 average offshore wind
 capacity factor



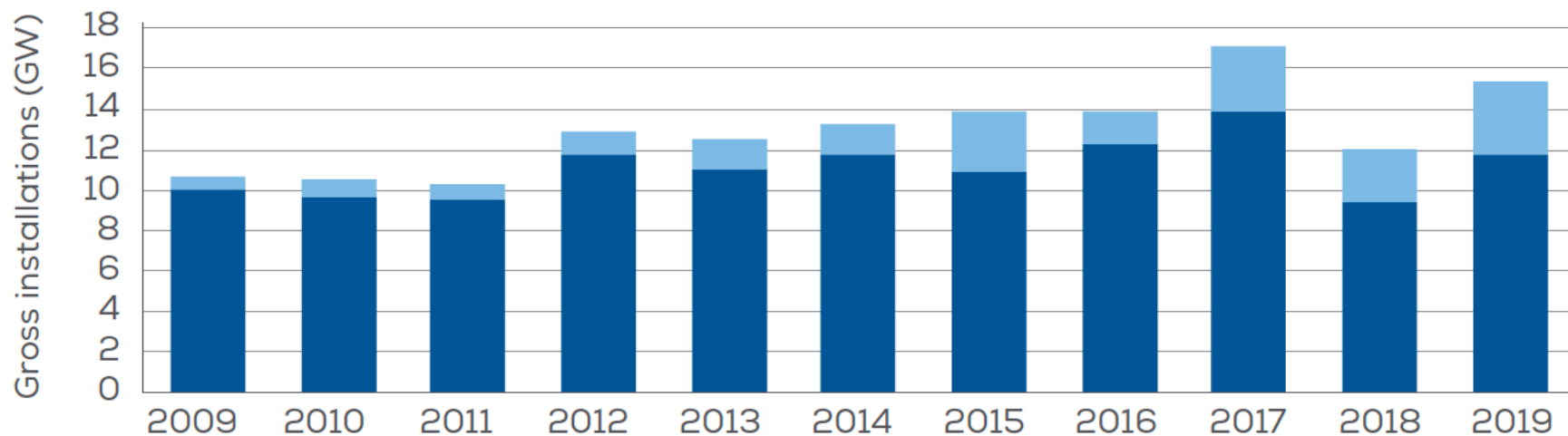
European wind energy generation in 2019



Data refers to EU Member States only

OFFSHORE WIND POWER

FIGURE 2
New annual onshore and offshore wind installations in Europe

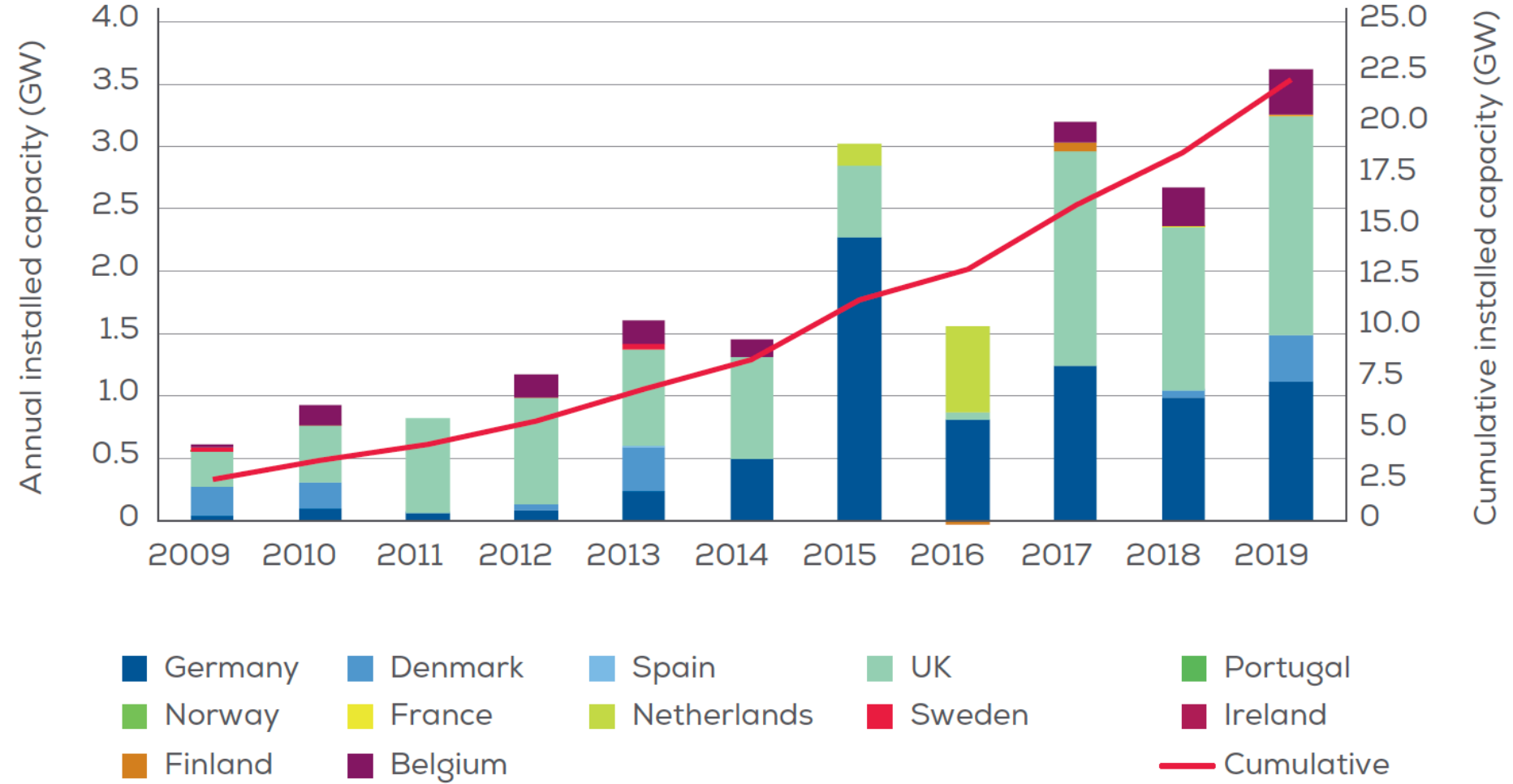


| | | | | | | | | | | | | |
|---|-----------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| ■ | Offshore | 0.6 | 0.9 | 0.8 | 1.2 | 1.5 | 1.5 | 3.0 | 1.6 | 3.2 | 2.7 | 3.6 |
| ■ | Onshore | 10.0 | 9.6 | 9.5 | 11.7 | 11.0 | 11.7 | 10.9 | 12.3 | 13.9 | 9.4 | 11.7 |
| | Total | 10.7 | 10.5 | 10.3 | 12.9 | 12.5 | 13.3 | 13.9 | 13.8 | 17.1 | 12.1 | 15.4 |

Source: WindEurope

FIGURE A

Annual offshore wind installations by country (left axis) and cumulative capacity (right axis) (GW)



Source: WindEurope

FIGURE 3

Cumulative installed capacity (MW) and number of turbines by country

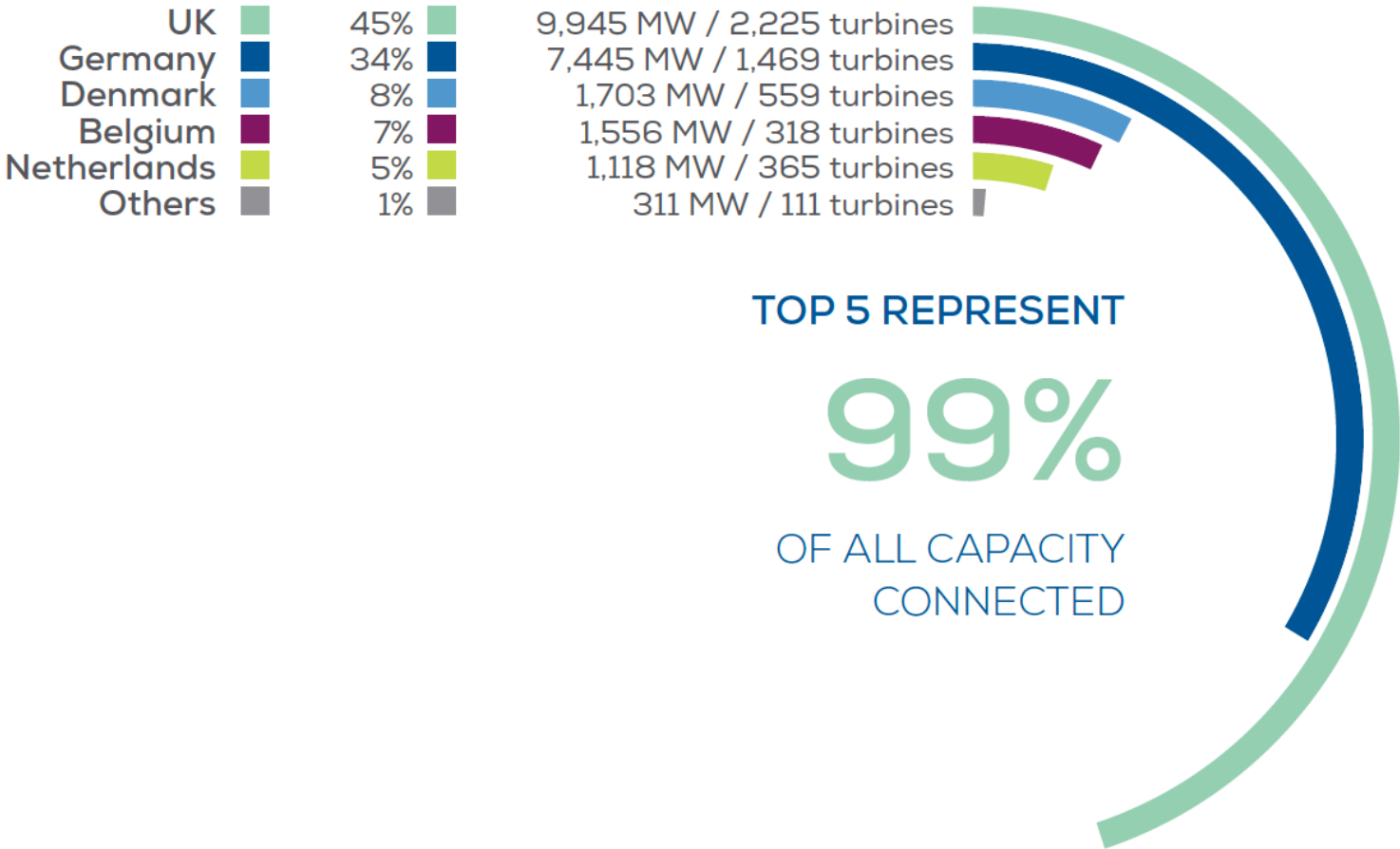


FIGURE 5

Yearly average of newly installed offshore wind turbine rated capacity (MW)

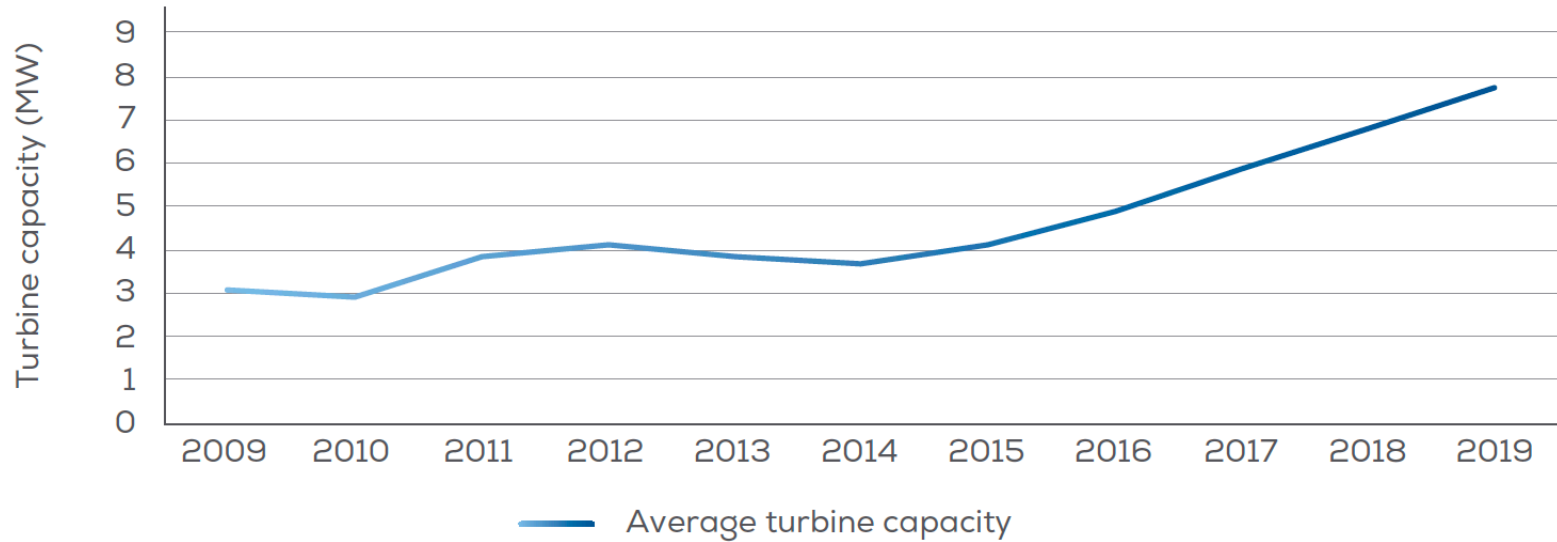


FIGURE 6

Average size of commercial offshore wind farm projects in the year (MW)

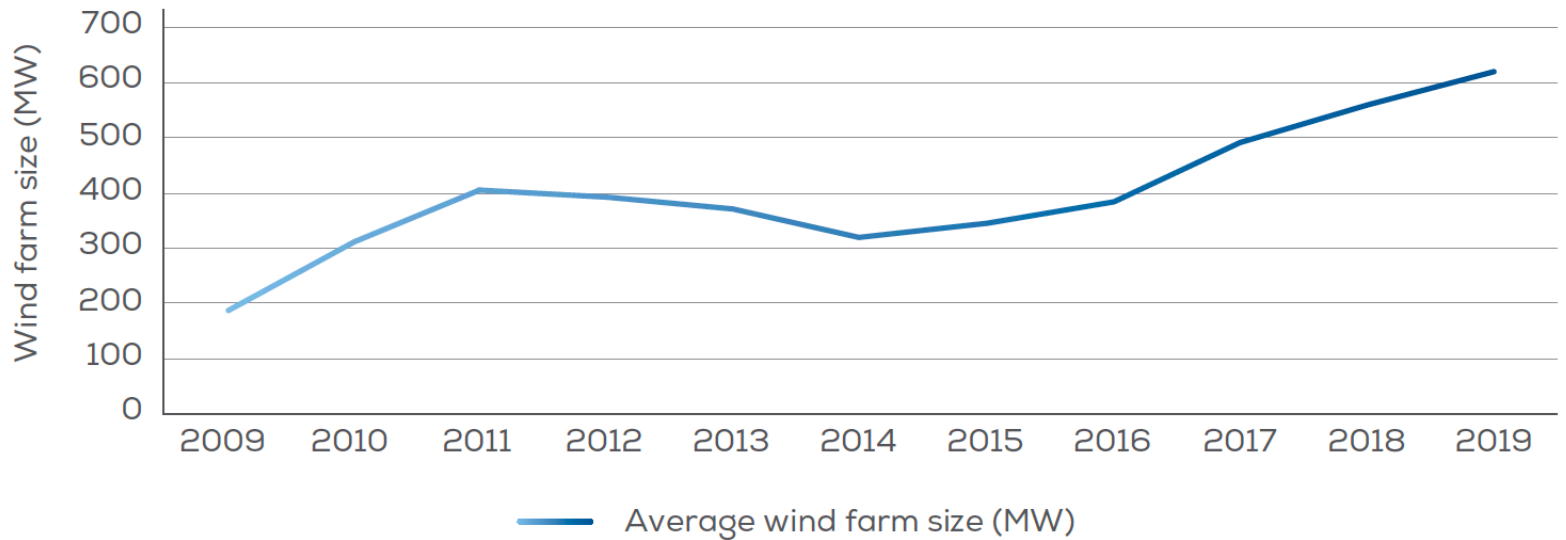


FIGURE 8

Average water depth and distance to shore of offshore wind farms under construction during 2019. The size of the bubble indicates the capacity of the site

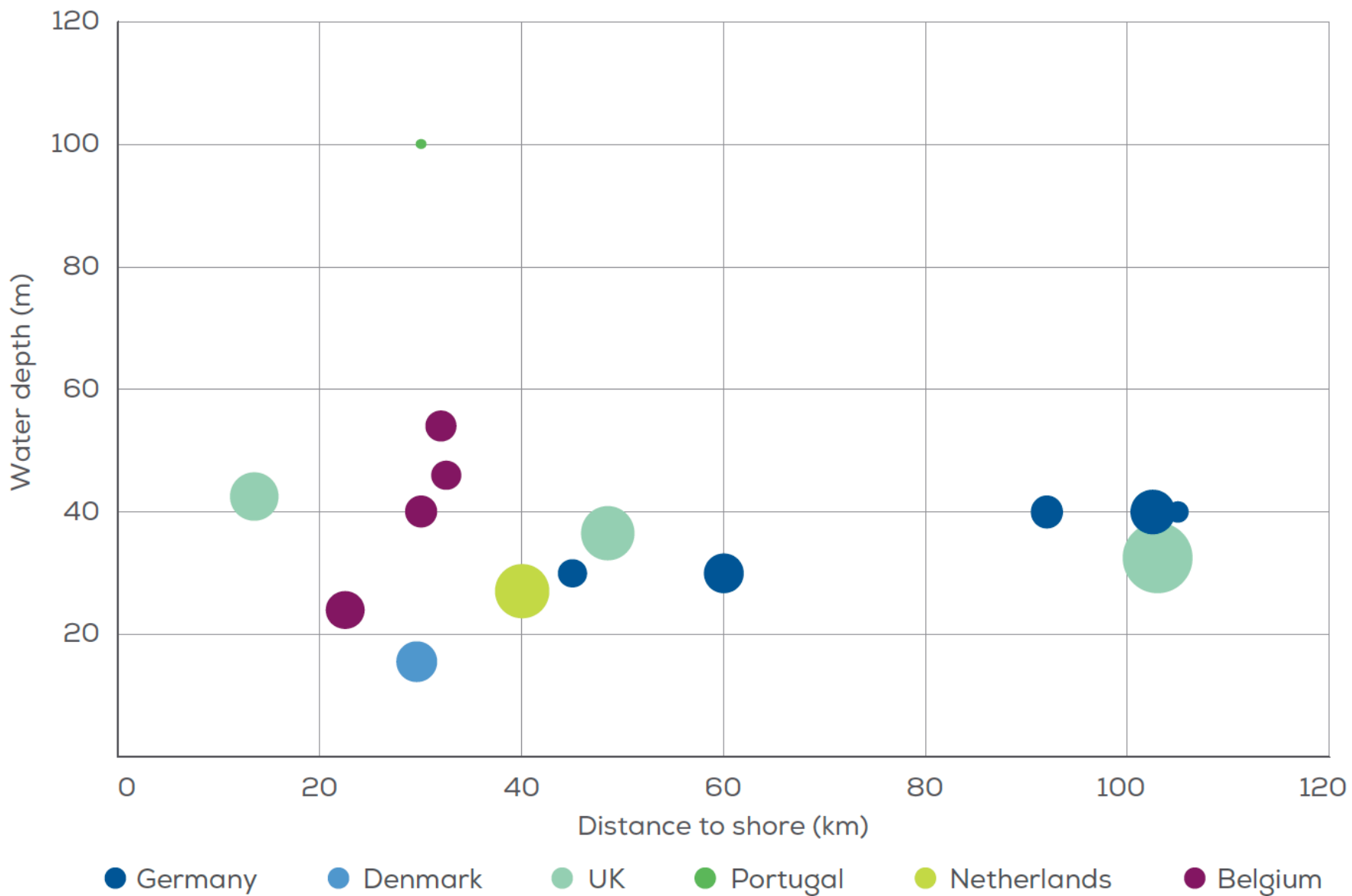


FIGURE 12

Wind turbine manufacturers' share at the end of 2019

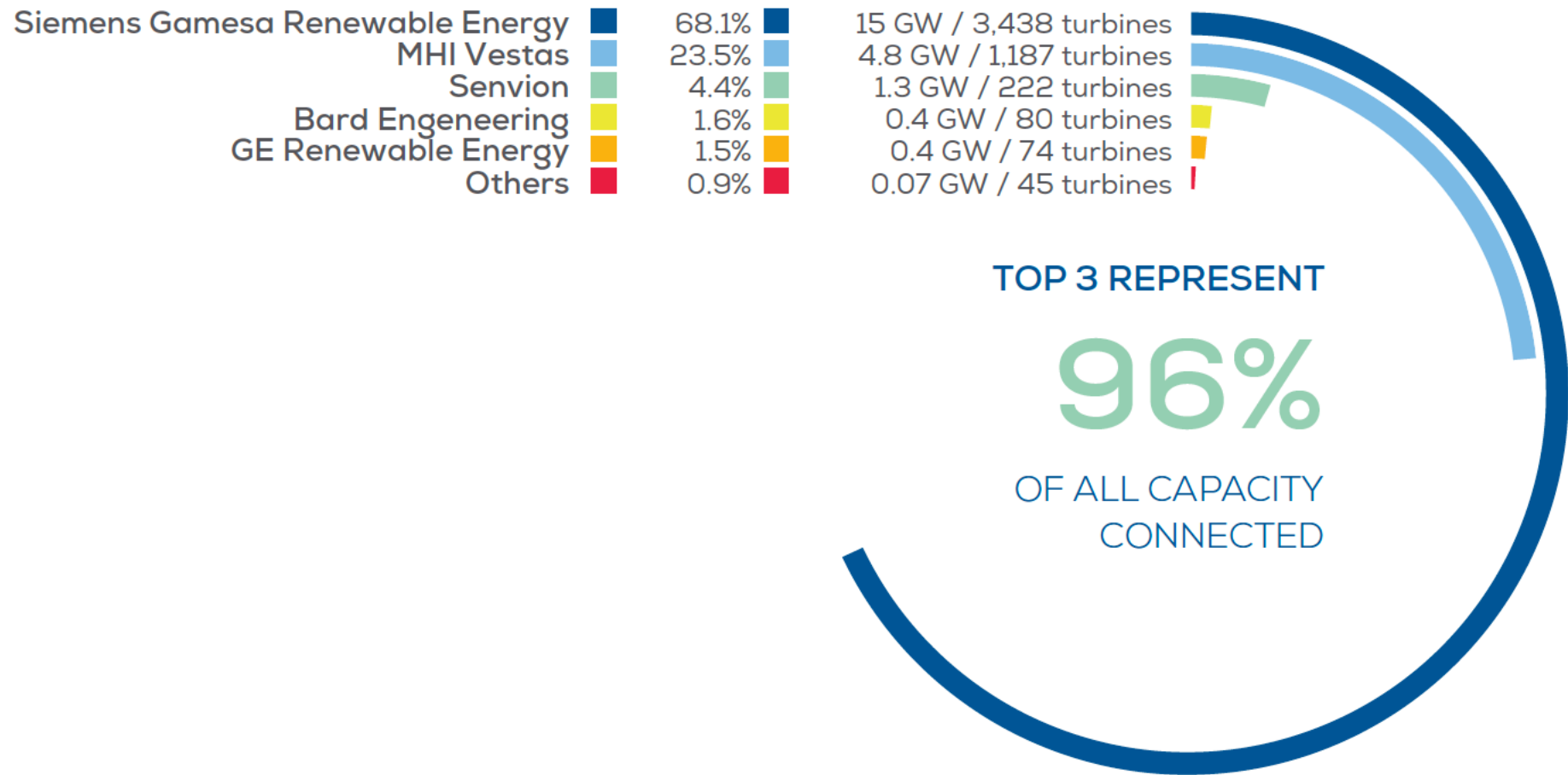
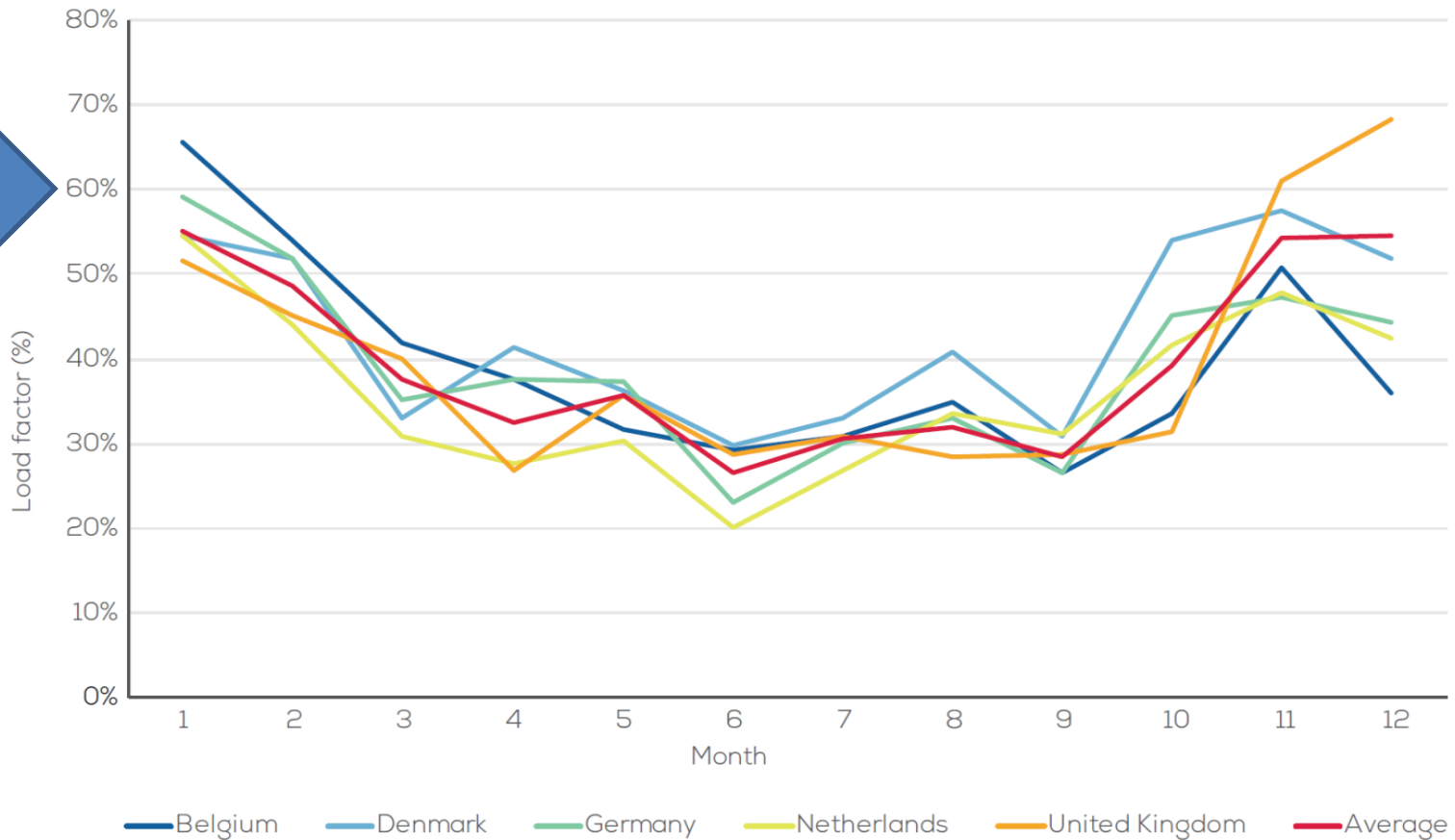


FIGURE 13

Monthly national load factors of offshore wind in 2016 (percent)⁷



Average in offshore Europe:
37% = 3200 h

Source: WindEurope

Cumulative offshore installations

- 5,047 offshore turbines are now installed, and grid connected, making a cumulative total of 22,072 MW.
- Including sites with partial grid-connected turbines, there are now 110 offshore wind farms in 12 European countries.
- The UK has the largest amount of offshore wind capacity in Europe with 45% of all installations. Second is Germany with 34%, followed by Denmark (8%).

Offshore – Example in Portugal



- [Aguçadoura – Póvoa do Varzim](#)
 - WindFloat, 2 MW
 - 6 km distance
 - 60 m depth
 - EDP, Principle Power, A. Silva Matos e Vestas
 - 20 M€
 - Decommissioned in 2017

WindFloat Atlantic

- Phase II – 3 WTG of 8.4 MW, Total of 25 MW
- Floating structure with 30 m height and 50 m between each column
- WTG rotor at 164 m height



The WindFloat Atlantic is the next stage of development and intends to demonstrate the pre-commercial phase of the technology



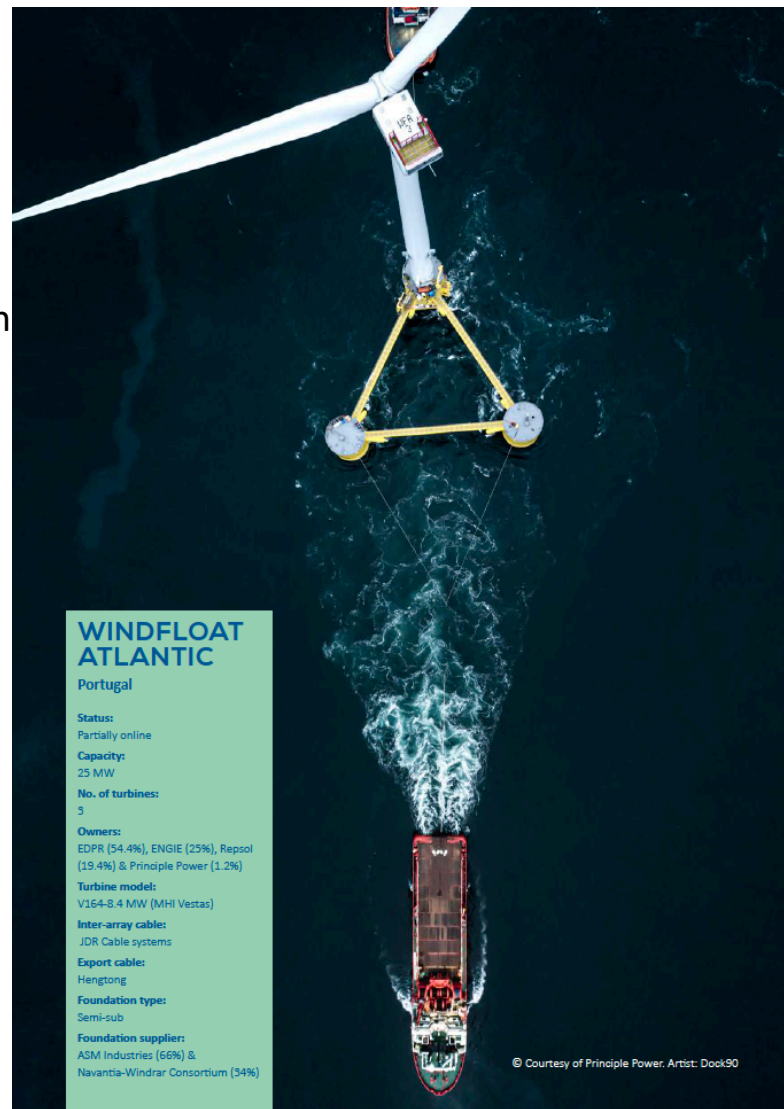
- **Total capacity:** 25MW capacity, (3 units equipped with MHI-Vestas V164)
- **Total investment:** ~125M€ (partly funded by the EC)

NER 300 and FiT

Equity

Project Finance

- **Location:** 20 km off the coast of **Viana do Castelo**, in water depth of 85-100m, in an area of sand and sediments, suitable for mooring
- **Interconnection:** to be constructed by REN, allowing a **direct connection at 60kV** with no onshore or offshore substation
- **Construction:** several **shipyards** options available close to final location. **Turbine installation quayside**
- **Floating structure certification:** designed for **25 years**, certified throughout design, construction and installation by **ABS**, an independent party
- **Key Dates:**
 - FID: Q2-2017
 - Start Fabrication: Q3 2017



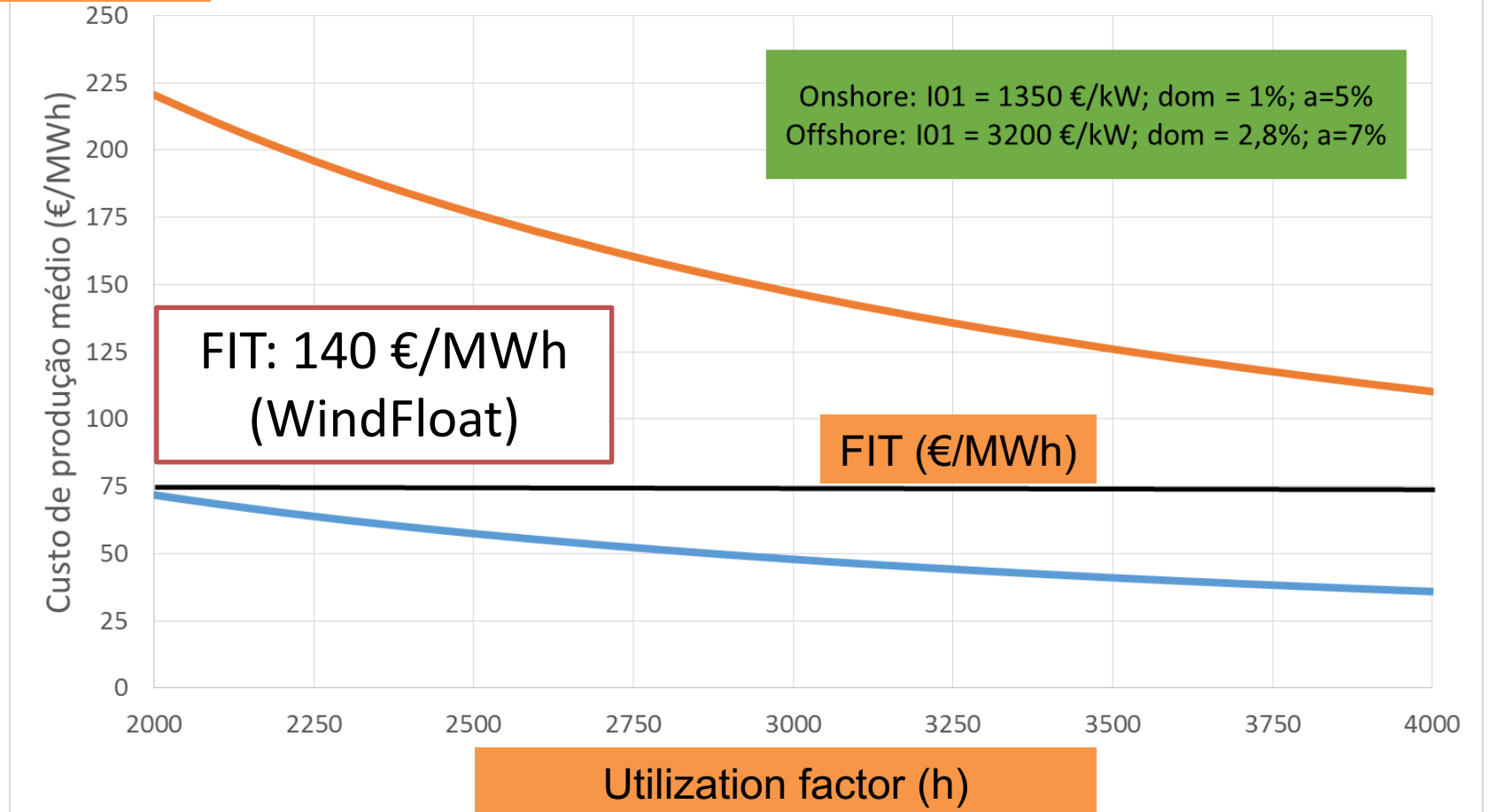
Source: EDP-Inovação

Estimated costs

Avaliação económica onshore / offshore

LCOE(€/MWh)

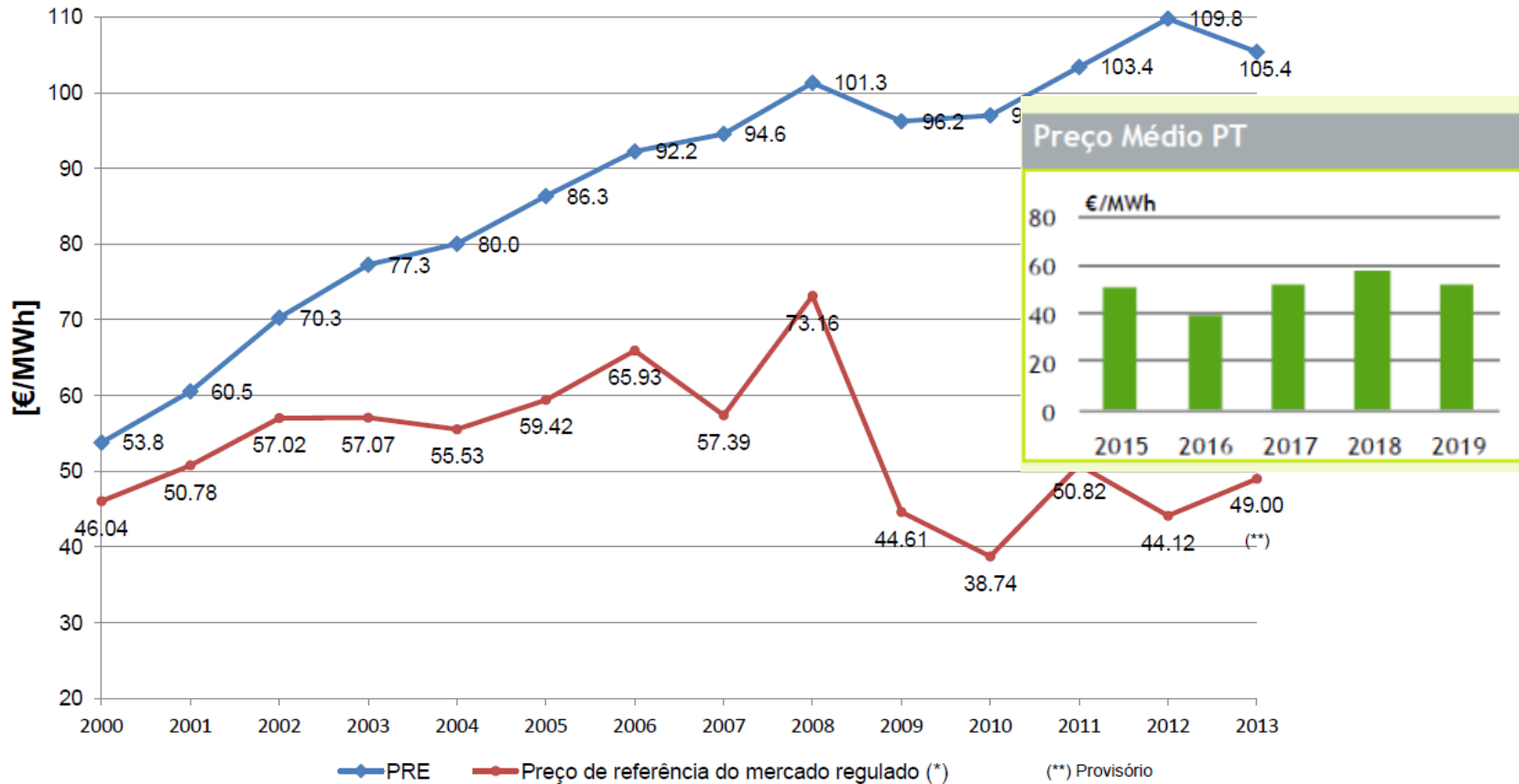
— onshore — offshore



RENEWABLE ENERGY PRICES AND COSTS

Average annual prices

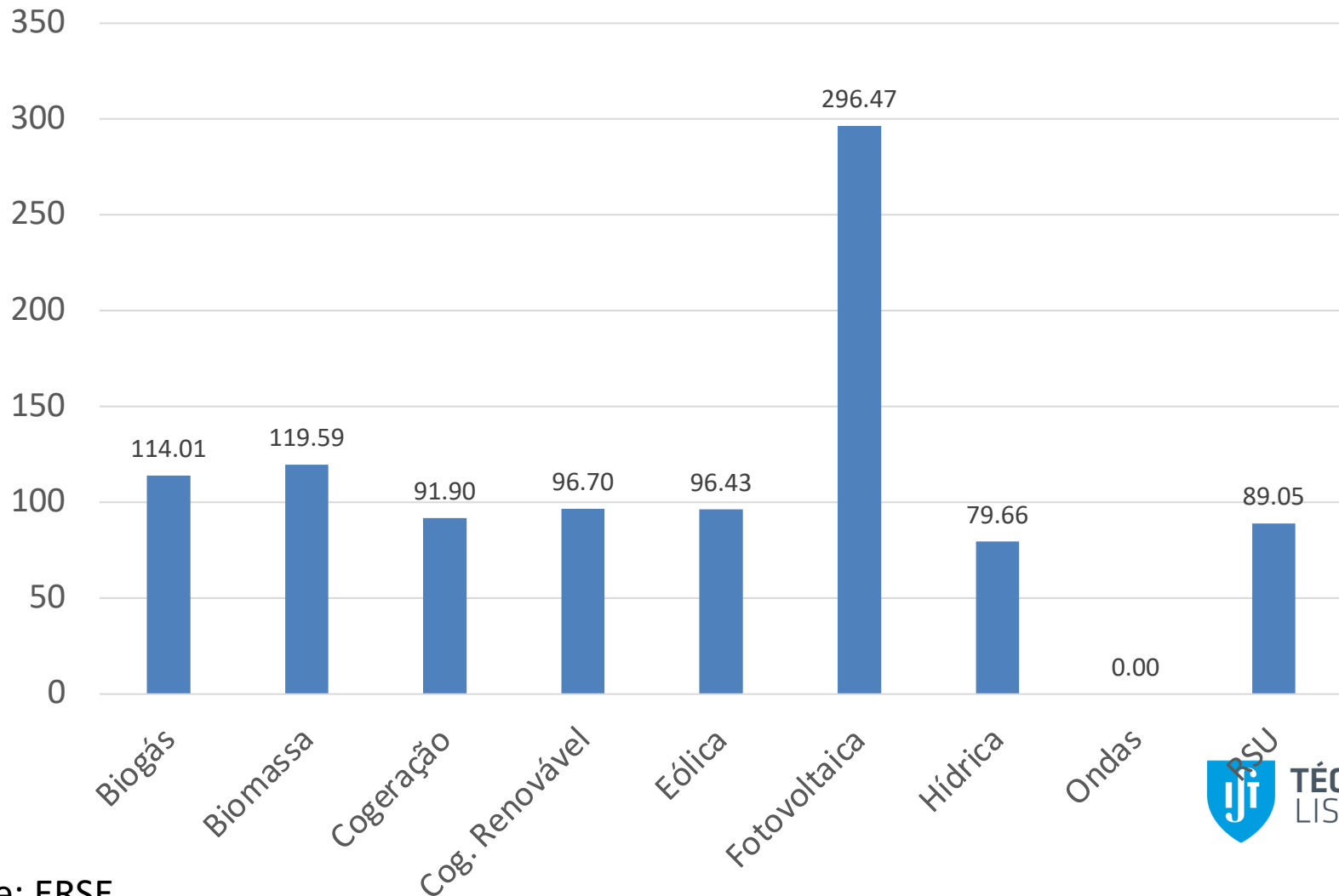
FIT (Ago2017): 104.12 €/MWh



MIBEL spot price (€/MWh)
 (2017): 52.5; (2018): 57.4; (2019): 47.87

FIT per technology

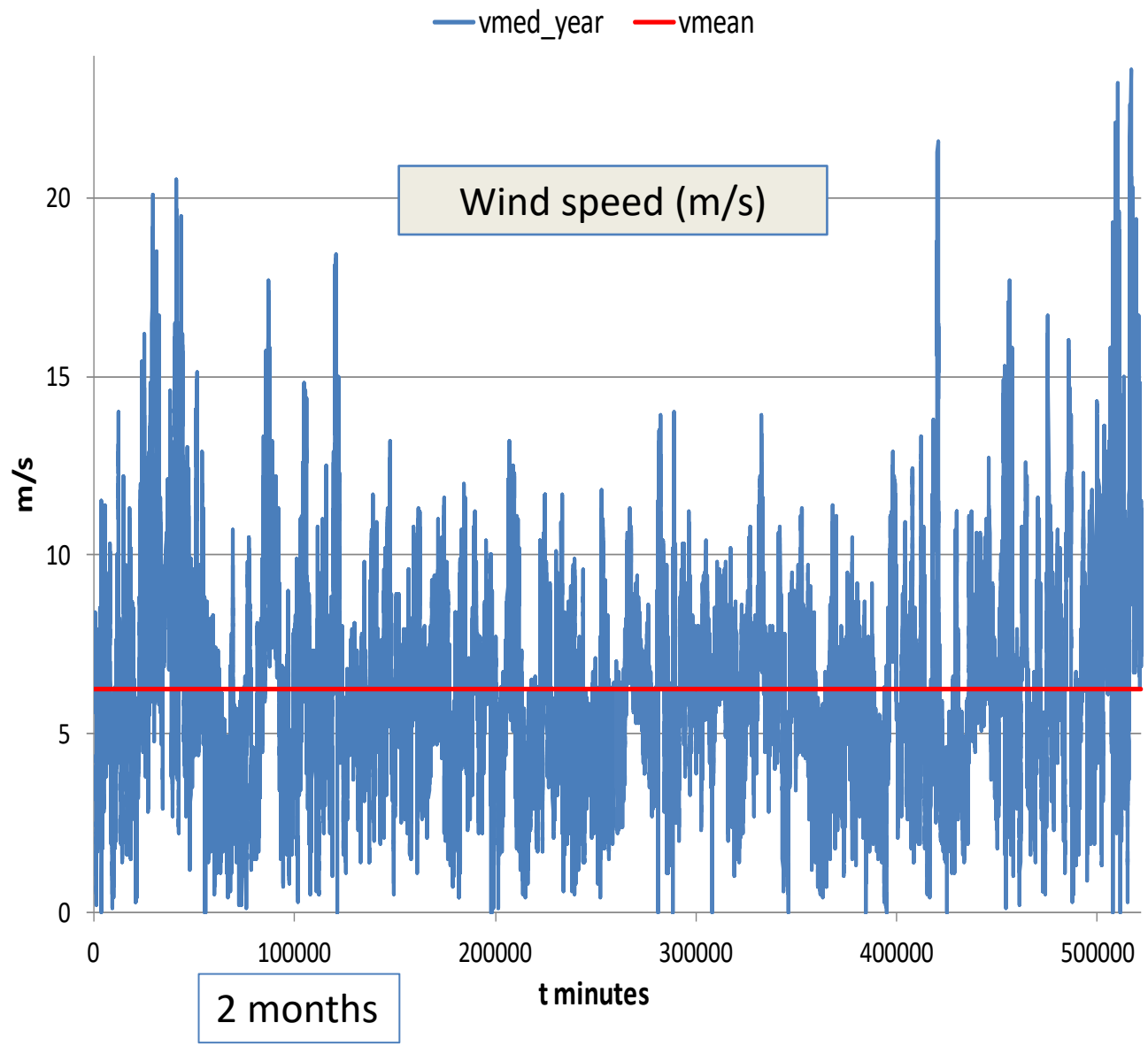
Ago 2017



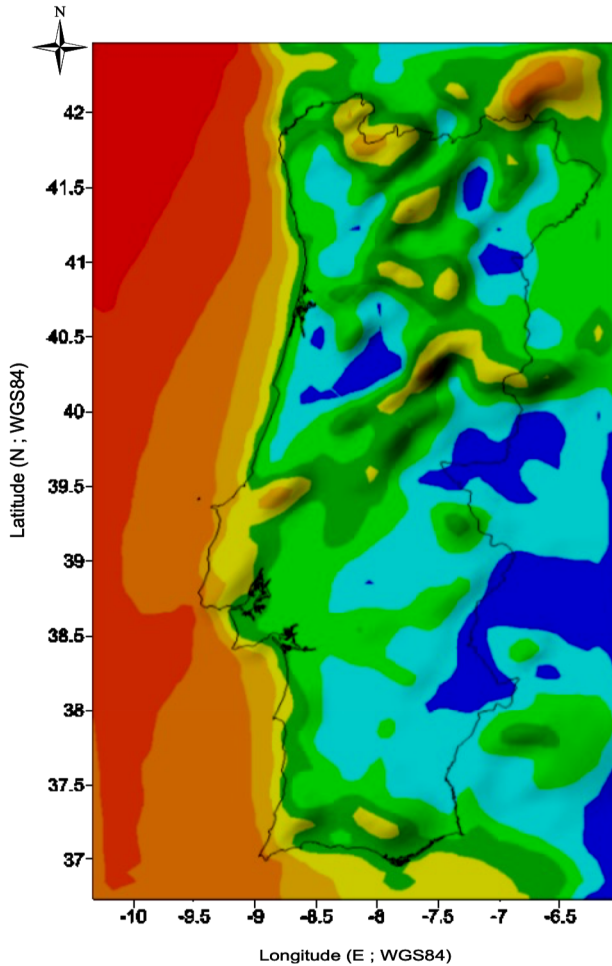
Source: ERSE

WIND CHARACTERISTICS

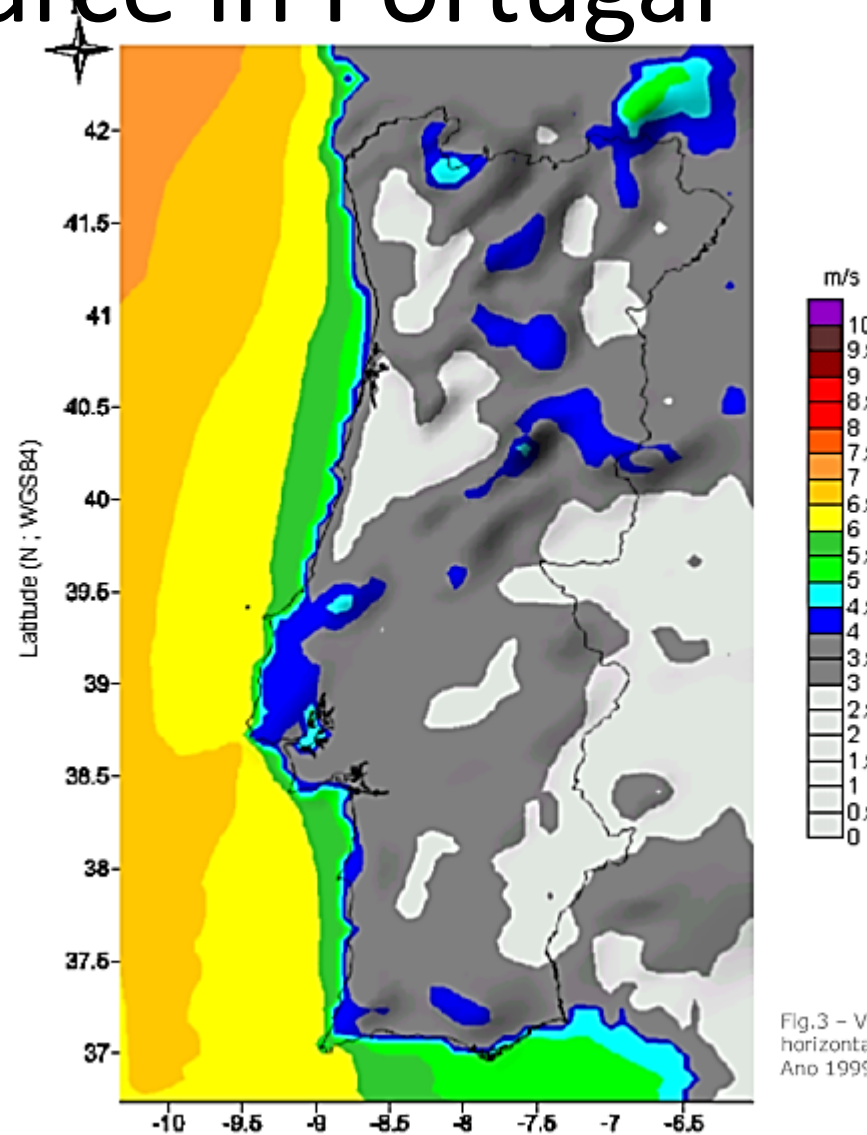
Variations in time



Wind resource in Portugal



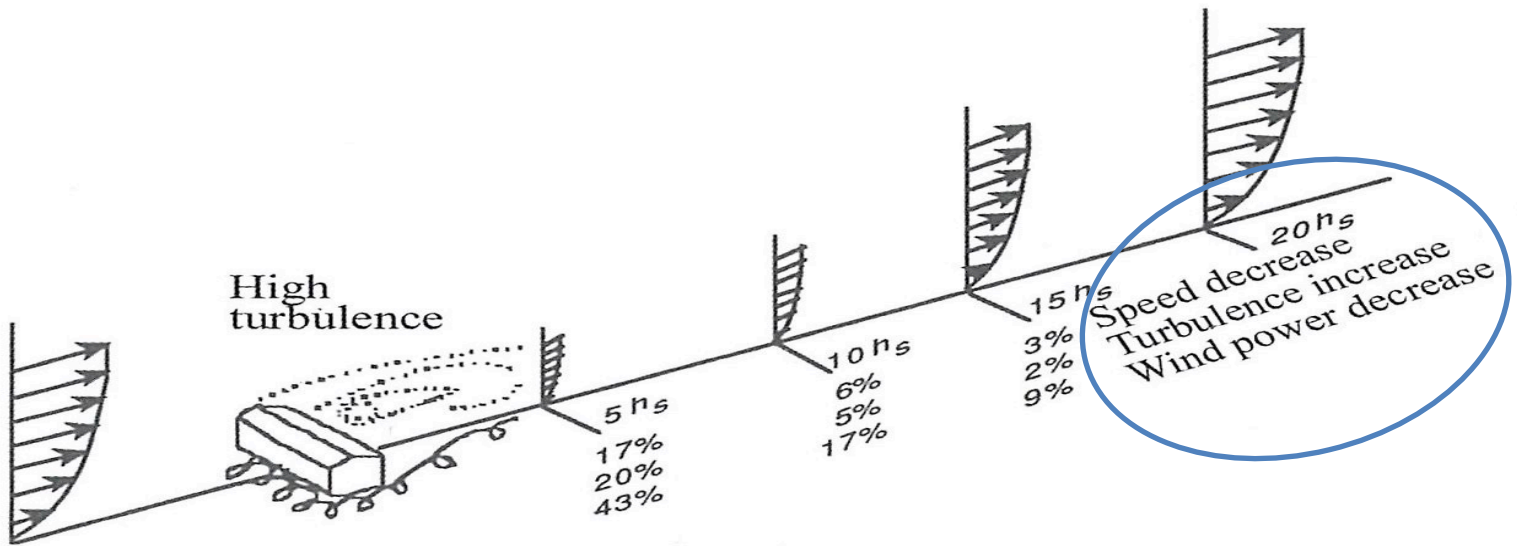
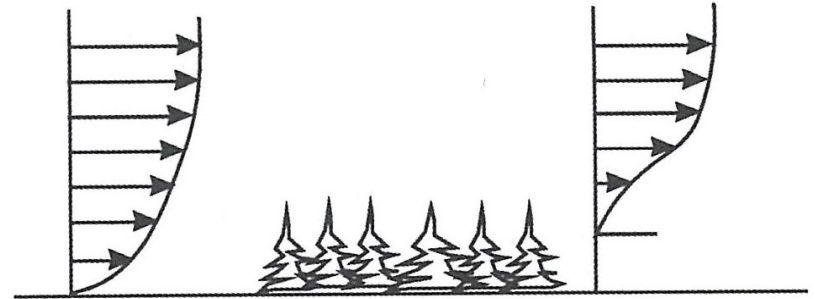
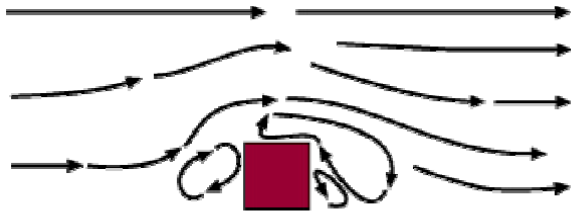
Average wind speed at 60m



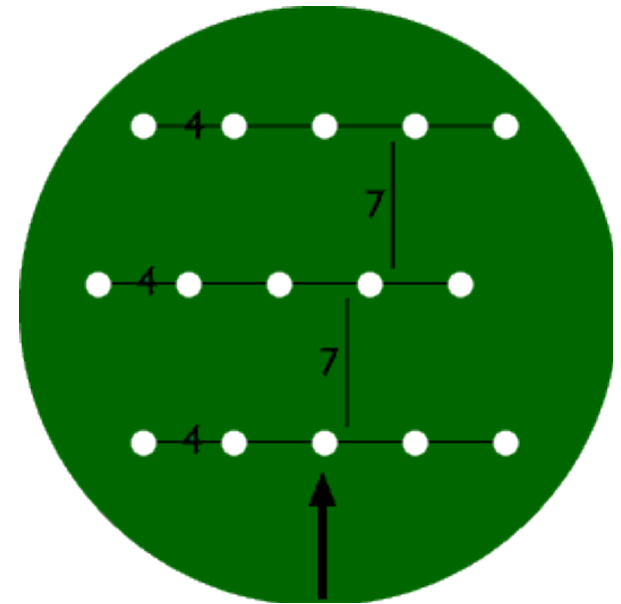
Average wind speed at 10m

Fig.3 - Velocidade média horizontal a 10 m [m/s].
Ano 1999, 9x9 km

Effect of terrain

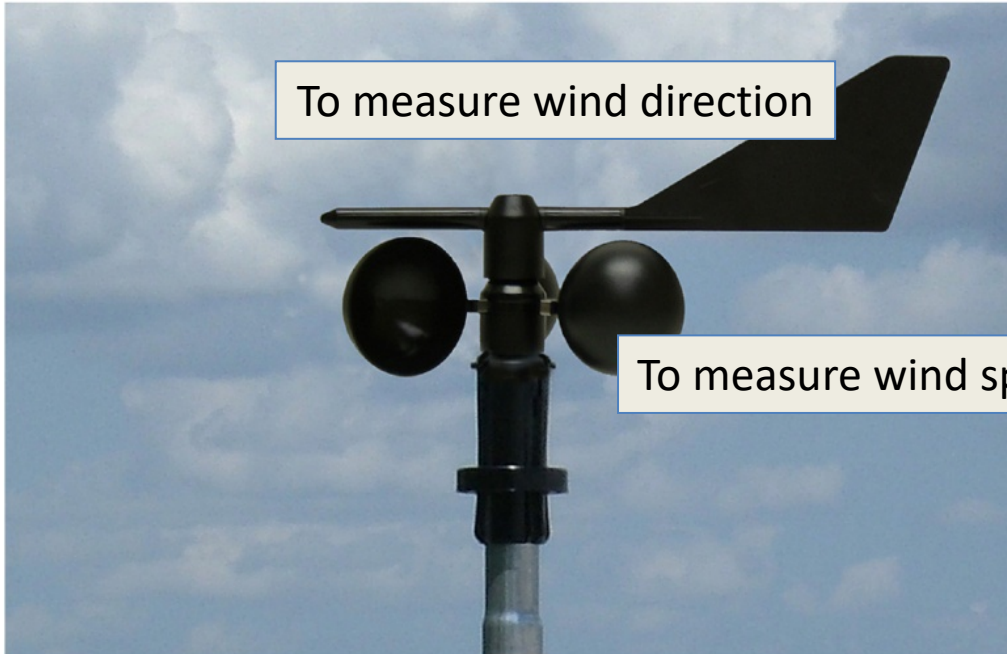


Wake effect



Recommended distances between turbines (as a function of rotor diameter) in order to minimize wake effect

Anemometers



To measure wind direction

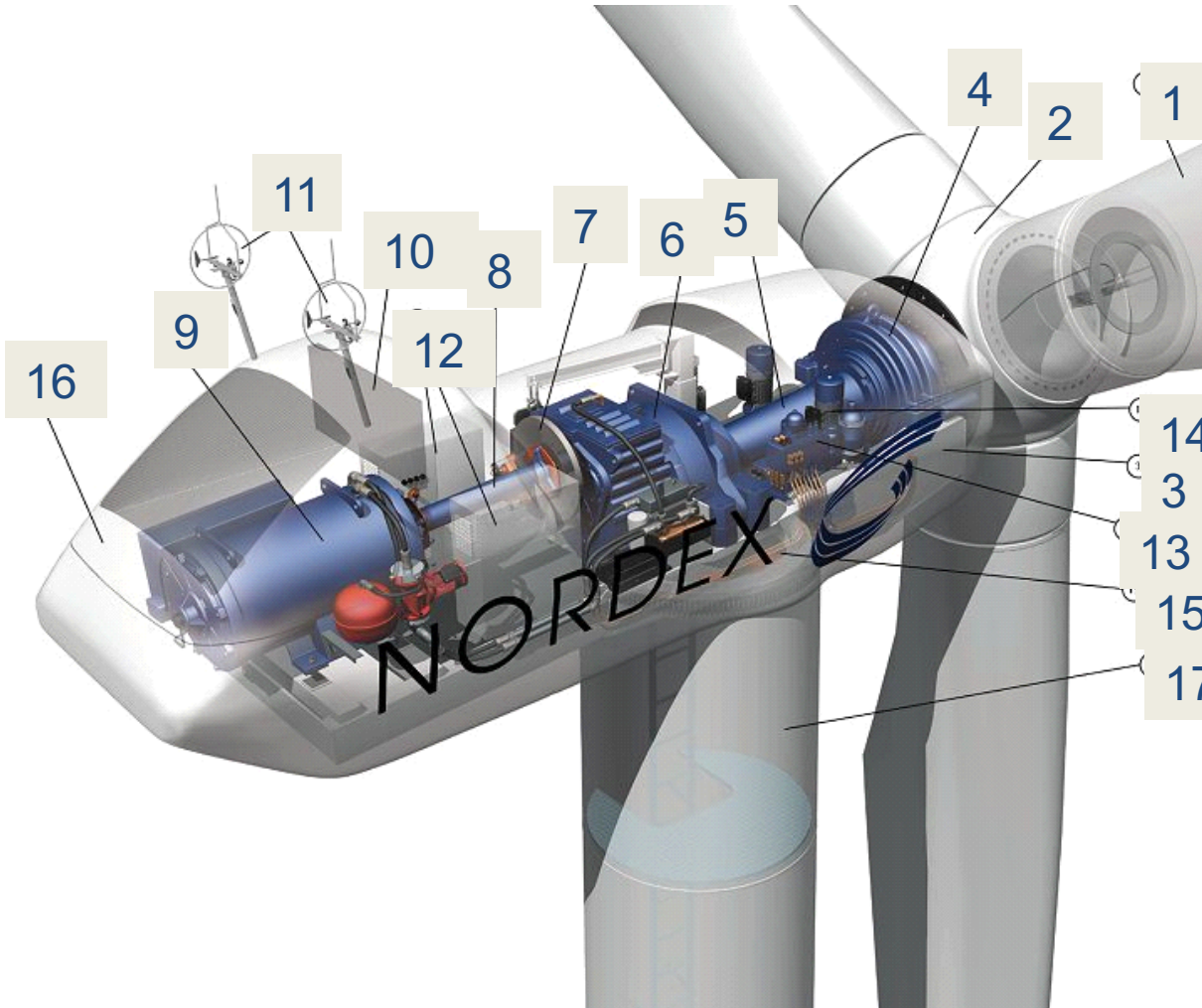
To measure wind speed

WIND GENERATOR COMPONENTS

Rotor, nacelle and tower

- Rotor
 - Upwind / Downwind
 - Solidity / Number of blades
 - Flexible blades
 - Blade material: Glass Reinforced Plastic; Carbon Fiber (expensive, best choice); Wood-Epoxy laminates
- Cabin (Nacelle)
 - Main shaft
 - Disk brakes
 - Gearbox (if it exists)
 - Generator
 - Yaw mechanism
- Tower
 - Tubular / Trusses

Components



- 1 – rotor blades
- 2 – hub
- 3 – cabin
- 4 – rotor support bearing
- 5 – rotor shaft
- 6 – gearbox
- 7 – brake
- 8 – generator shaft
- 9 – generator
- 10 – radiator
- 11 – anemometer and direction sensor
- 12 – control system
- 13 – hydraulic system
- 14 – yaw mechanism
- 15 – support bearing of the yaw
- 16 – cabin cover
- 17 – tower

Nacelle – 75 tons
Rotor – 40 tons
Tower – 152 tons
Total – 267 tons



Vestas [V90](#) [V903d](#)

Rotor Diameter: 90 m

Area swept: 6 362 m²

Nominal revolutions: 16.1 rpm

Operational interval: 8.6 - 18.4 rpm

Number of blades: 3

Hub height: 80 - 105 m

Cut-in wind speed: 4 m/s

Nominal wind speed (3 000 kW): 15 m/s

Cut-out wind speed: 25 m/s



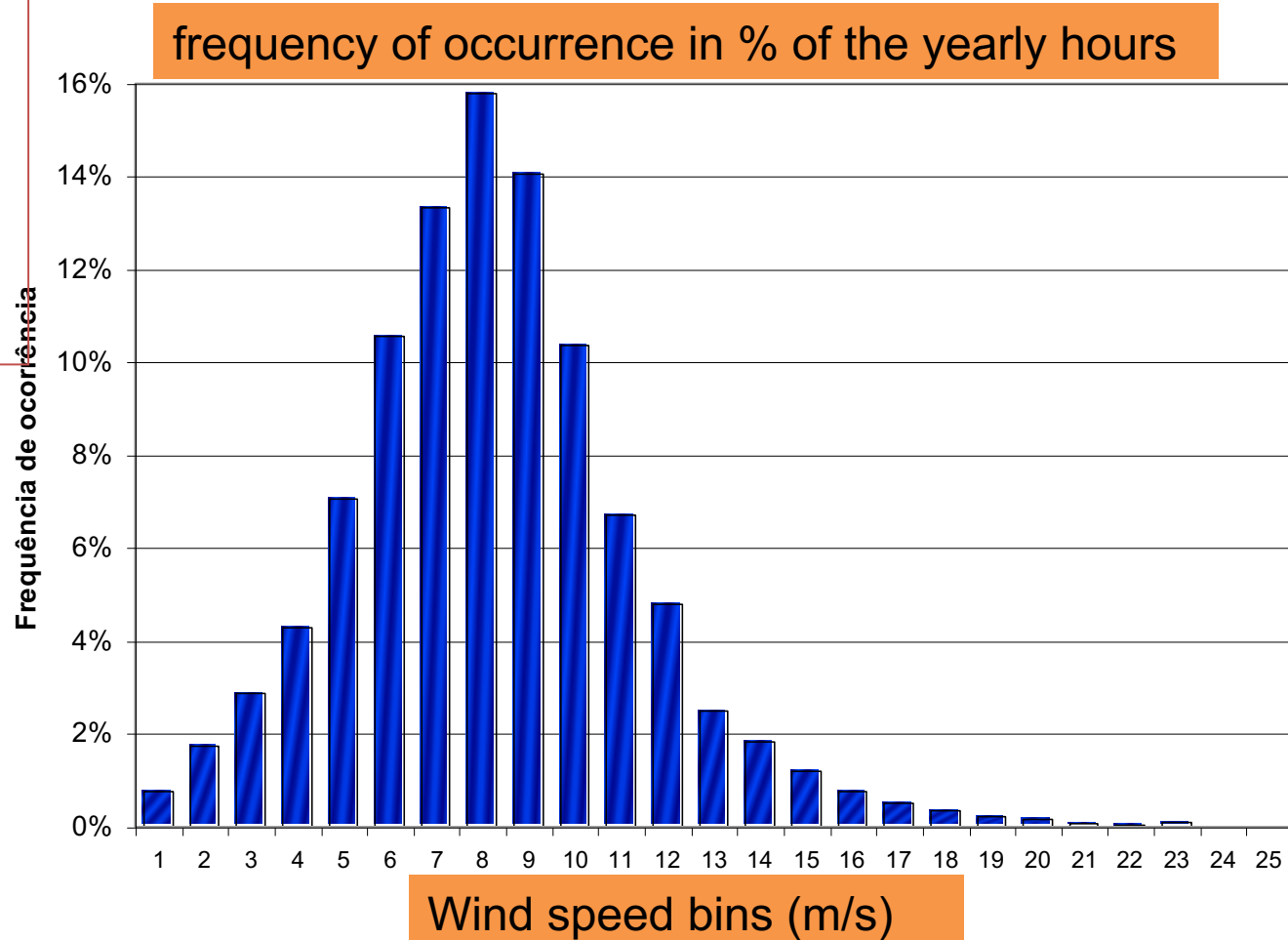
WIND DATA ANALYSIS

Methods

- Method of bins
 - Histogram
 - Data separated in data intervals (bins) of width 1m/s with f_j occurrences
- Statistical analysis
 - Weibull distribution
 - Rayleigh distribution

Method of bins

| h | u | classe |
|------|-------|--------|
| 8679 | 6,50 | 7 |
| 8680 | 8,38 | 8 |
| 8681 | 9,75 | 10 |
| 8682 | 9,76 | 10 |
| 8683 | 10,98 | 11 |
| 8684 | 10,64 | 11 |
| 8685 | 11,76 | 12 |
| 8686 | 13,72 | 14 |
| 8687 | 15,42 | 15 |
| 8688 | 16,94 | 17 |



Weibull pdf

$$f(u) = \frac{k}{c} \left(\frac{u}{c}\right)^{k-1} \exp\left(-\left(\frac{u}{c}\right)^k\right)$$

pdf: probability density function

Probability of the wind speed to be equal to a particular value u

$k > 0$ is the shape parameter
 $c > 0$ is the scale parameter (m/s)

$$u_{ma} = \int_0^{\infty} u f(u) du$$



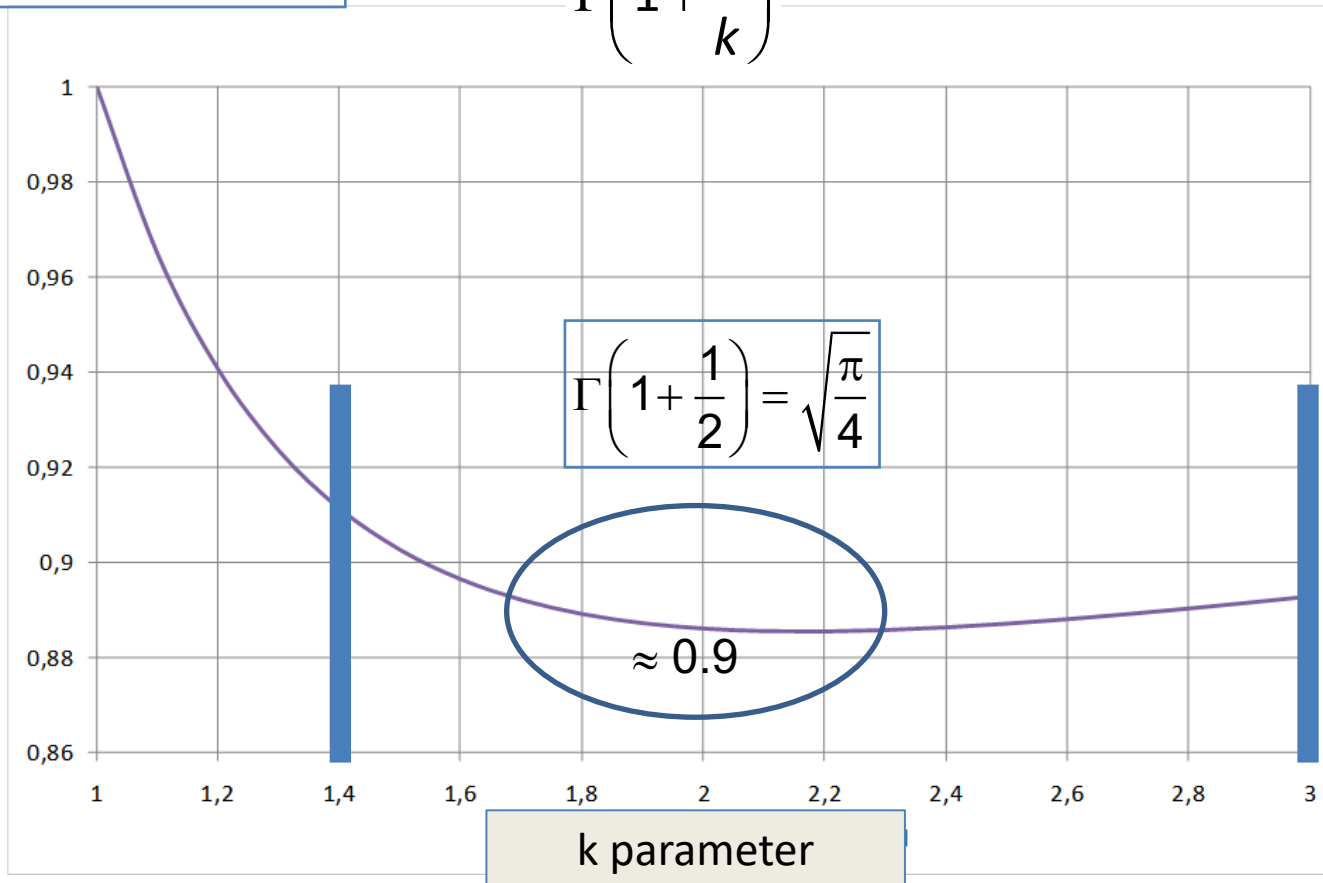
$$u_{ma} = \sum_{\bar{u}=0}^{\bar{u}_{max}} u f(u)$$

Annual mean wind speed

Gamma function

$$u_{\text{ma}} = c\Gamma\left(1 + \frac{1}{k}\right)$$

$$\Gamma\left(1 + \frac{1}{k}\right)$$



Weibull cdf

$$F(u) = 1 - \int_{-\infty}^u f(u) du = 1 - \int_0^u f(u) du$$

Probability of the
wind speed to exceed
a particular value

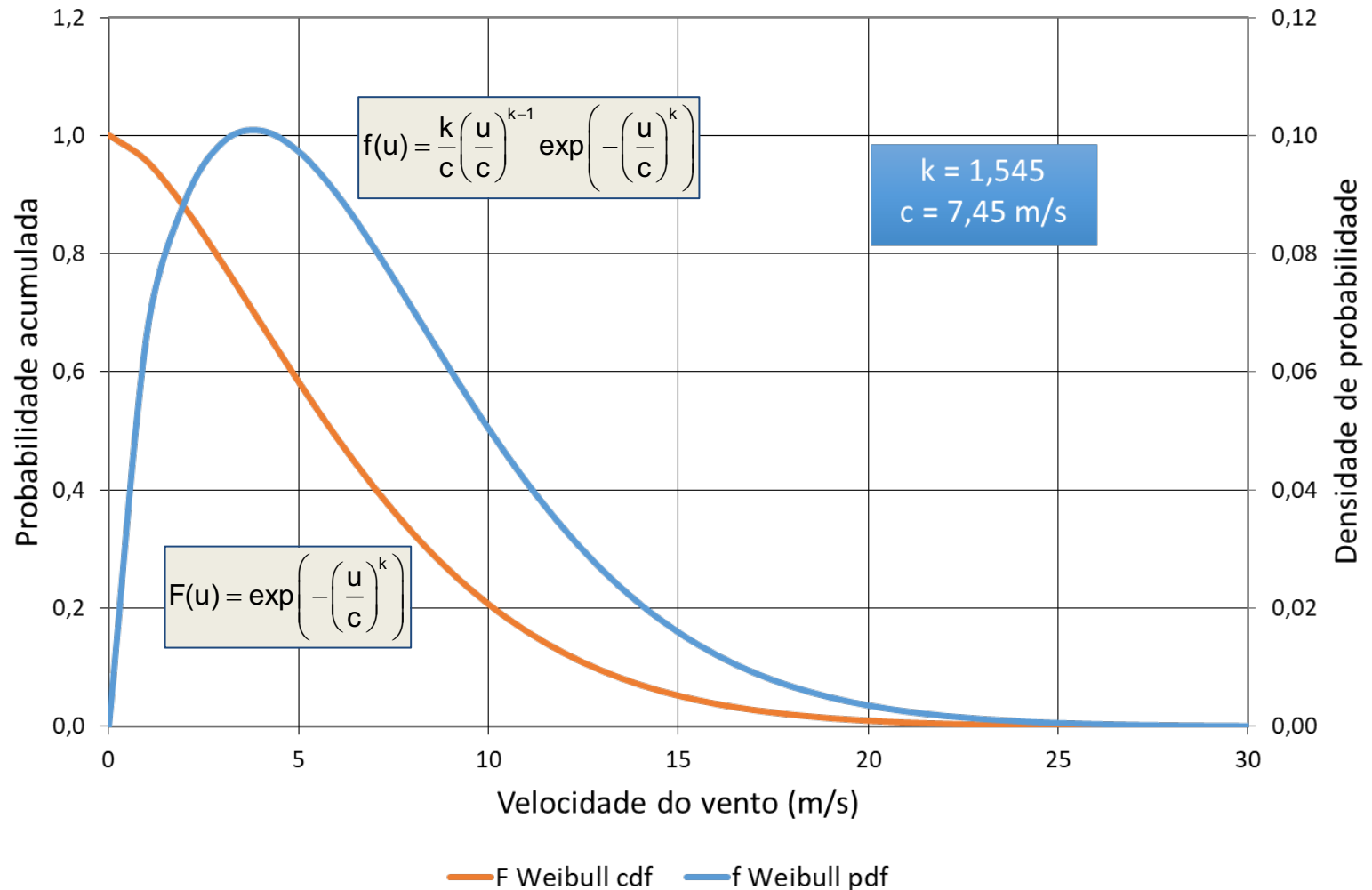
$$f(u) = -\frac{dF(u)}{du}$$

cdf: cumulative distribution function

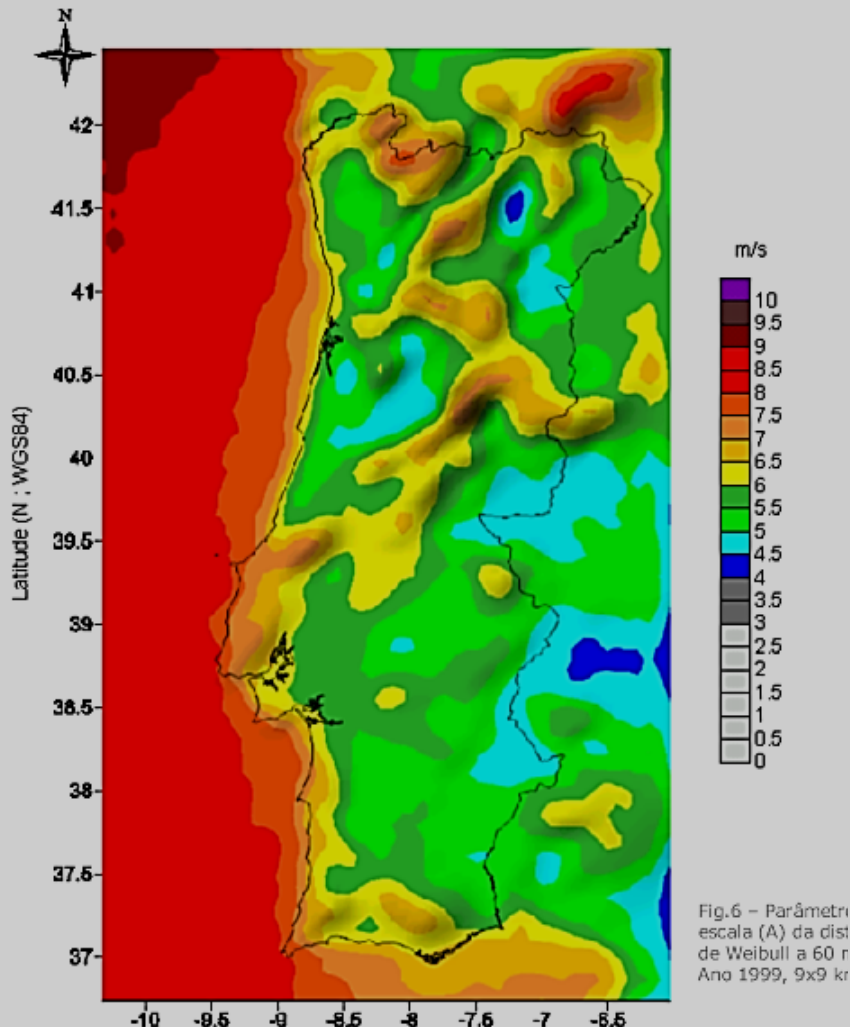
$$F(u) = \exp\left(-\left(\frac{u}{c}\right)^k\right)$$

Weibull pdf & cdf

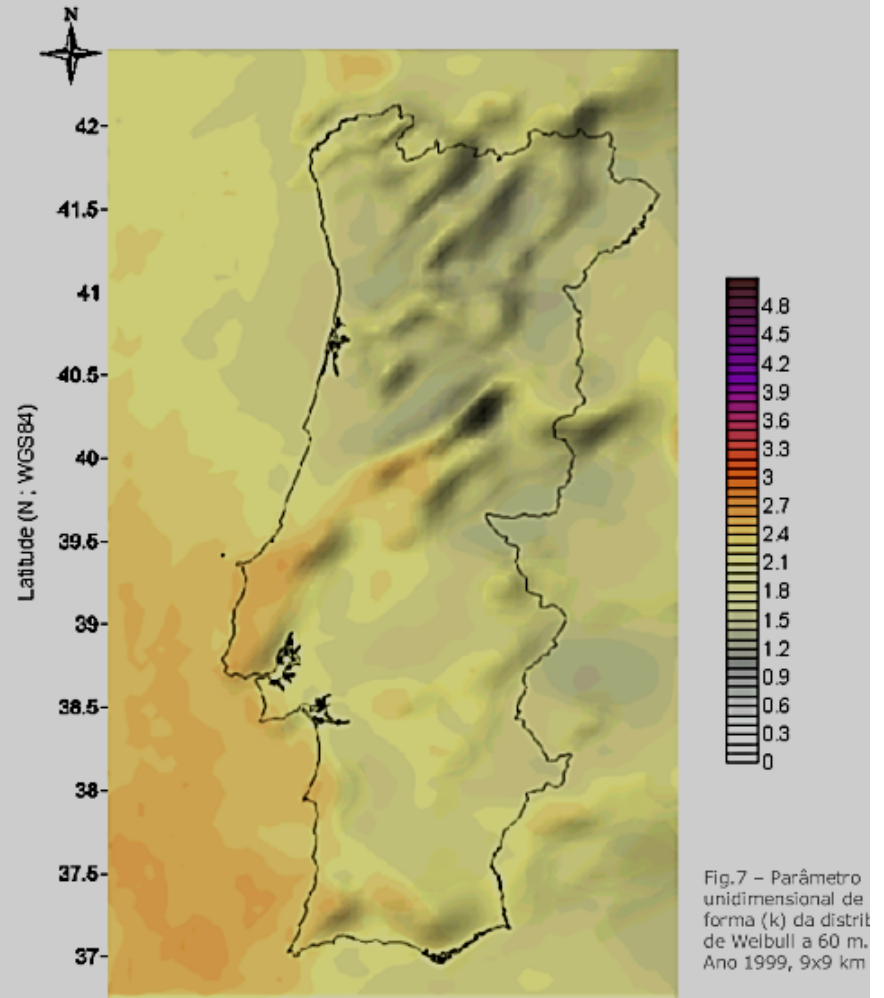
Weibull pdf & cdf



Weibull parameters in Portugal



c parameter (60 m height)

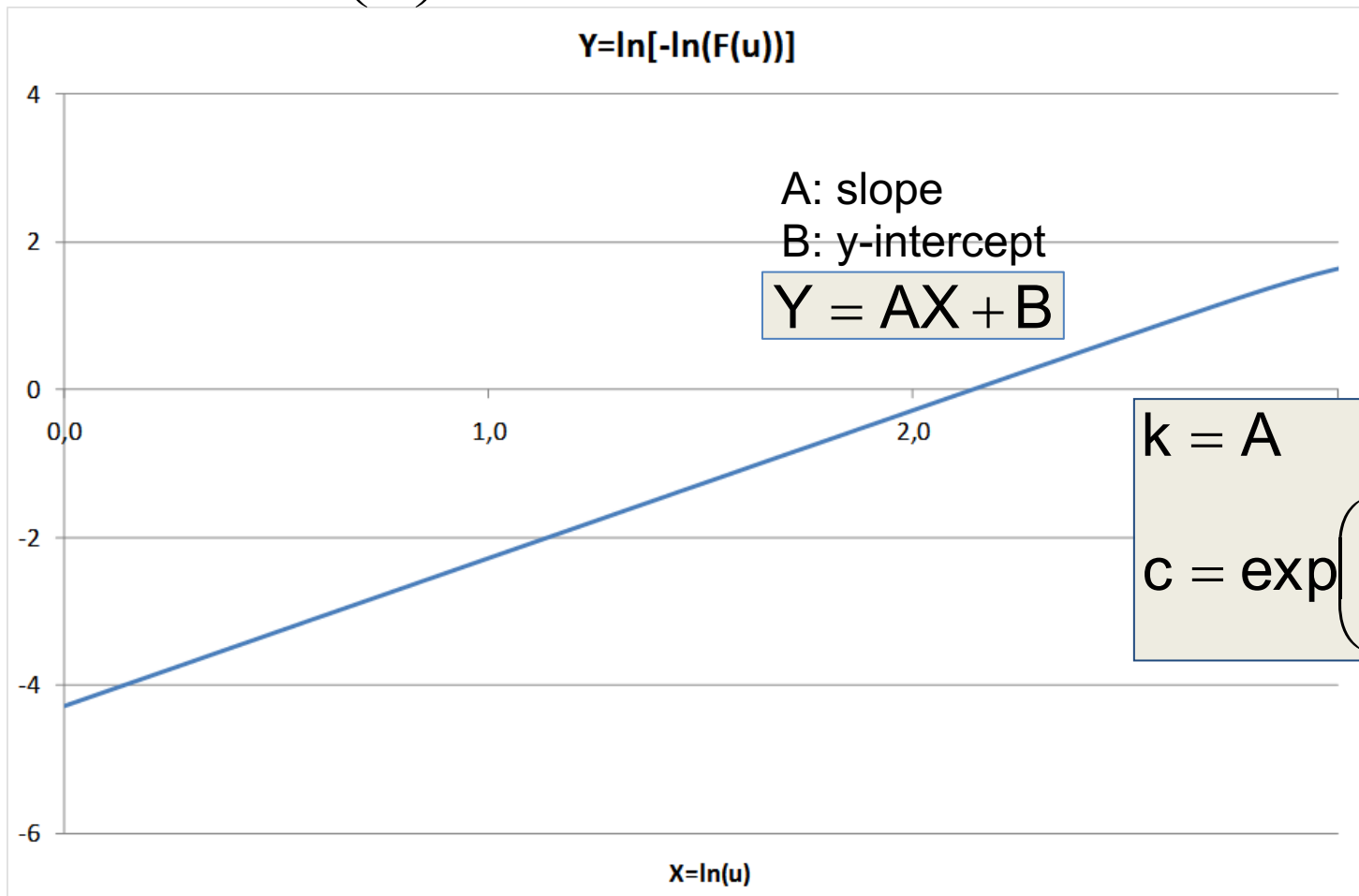


k parameter (60 m height)

$$F(u) = \exp\left(-\left(\frac{u}{c}\right)^k\right)$$

Weibull parameters estimation

$$\ln[F(u)] = -\left(\frac{u}{c}\right)^k \rightarrow \ln[-\ln(F(u))] = k \ln(u) - k \ln(c)$$



Weibull parameters estimation

Least Squares Method

- Given data: known experimental histogram
- Modern solution
- **Excel solver**
 - Objective: compute the best fit k and c , by minimizing the mean square error
 - Guess initial values
 - Change k and c , in order to minimize the quadratic error

Weibull parameters estimation

Least Squares Method

| | f(u)_Experim. | f(u)_LS | E_QUAD |
|---|---------------|---------|---------|
| 1 | 0,028 | 0,090 | 0,00396 |
| 2 | 0,053 | 0,082 | 0,00084 |
| 3 | 0,074 | 0,074 | 0,00000 |
| 4 | 0,089 | 0,067 | 0,00050 |
| 5 | 0,099 | 0,061 | 0,00143 |
| 6 | 0,101 | 0,055 | 0,00216 |
| 7 | 0,099 | 0,050 | 0,00240 |
| 8 | 0,091 | 0,045 | 0,00216 |

| WEIBULL_LS | |
|------------|-------|
| k | c |
| 1,00 | 10,00 |

Initial values

Av_E_QUAD 0,01798

| | f(u)_Experim. | f(u)_LS | E_QUAD |
|---|---------------|---------|---------|
| 1 | 0,028 | 0,028 | 0,00000 |
| 2 | 0,053 | 0,053 | 0,00000 |
| 3 | 0,074 | 0,074 | 0,00000 |
| 4 | 0,089 | 0,089 | 0,00000 |
| 5 | 0,099 | 0,099 | 0,00000 |
| 6 | 0,101 | 0,101 | 0,00000 |
| 7 | 0,099 | 0,099 | 0,00000 |
| 8 | 0,091 | 0,091 | 0,00000 |

| WEIBULL_LS | |
|------------|------|
| k | c |
| 2,00 | 8,46 |

Final values

Av_E_QUAD 0,00000

Rayleigh distribution

Weibull with $k=2$

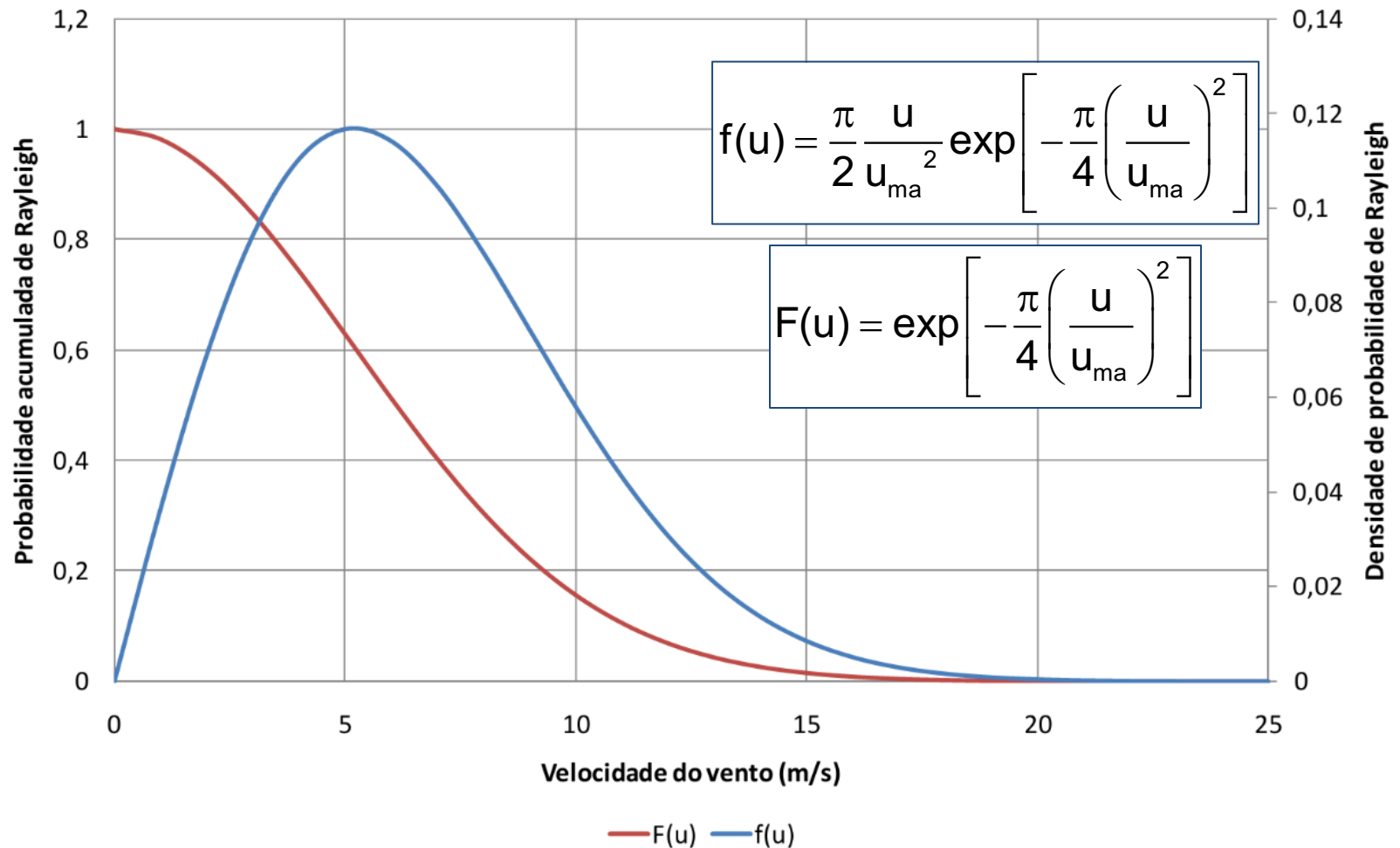
$$f(u) = \frac{k}{c} \left(\frac{u}{c} \right)^{k-1} \exp \left(- \left(\frac{u}{c} \right)^k \right)$$

$$c = \frac{u_{ma}}{\Gamma \left(1 + \frac{1}{2} \right)} = \frac{2}{\sqrt{\pi}} u_{ma} \quad \longrightarrow \quad f(u) = \left(\frac{\sqrt{\pi}}{u_{ma}} \right) \left(\frac{u\sqrt{\pi}}{2u_{ma}} \right) \exp \left\{ - \left[\left(\frac{u\sqrt{\pi}}{2u_{ma}} \right)^2 \right] \right\}$$

$$f(u) = \frac{\pi}{2} \frac{u}{u_{ma}^2} \exp \left[- \frac{\pi}{4} \left(\frac{u}{u_{ma}} \right)^2 \right]$$

Rayleigh pdf & cdf

$u_{ma} = 6,5 \text{ m/s}$



POWER IN THE WIND

Available power in the wind

$$E_{\text{cin}} = \frac{1}{2}mu^2 = \frac{1}{2}(\rho Ax)u^2$$

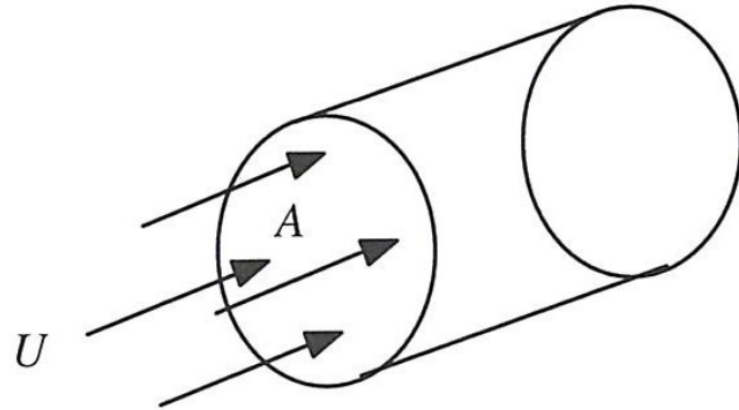
m: mass of the volume of air (kg)

u: constant speed of air (m/s)

ρ : air density (1,23 kg/m³, $\theta=15^\circ\text{C}$)

A: area of the disk of air (m²)

x: thickness of the volume of air (m)



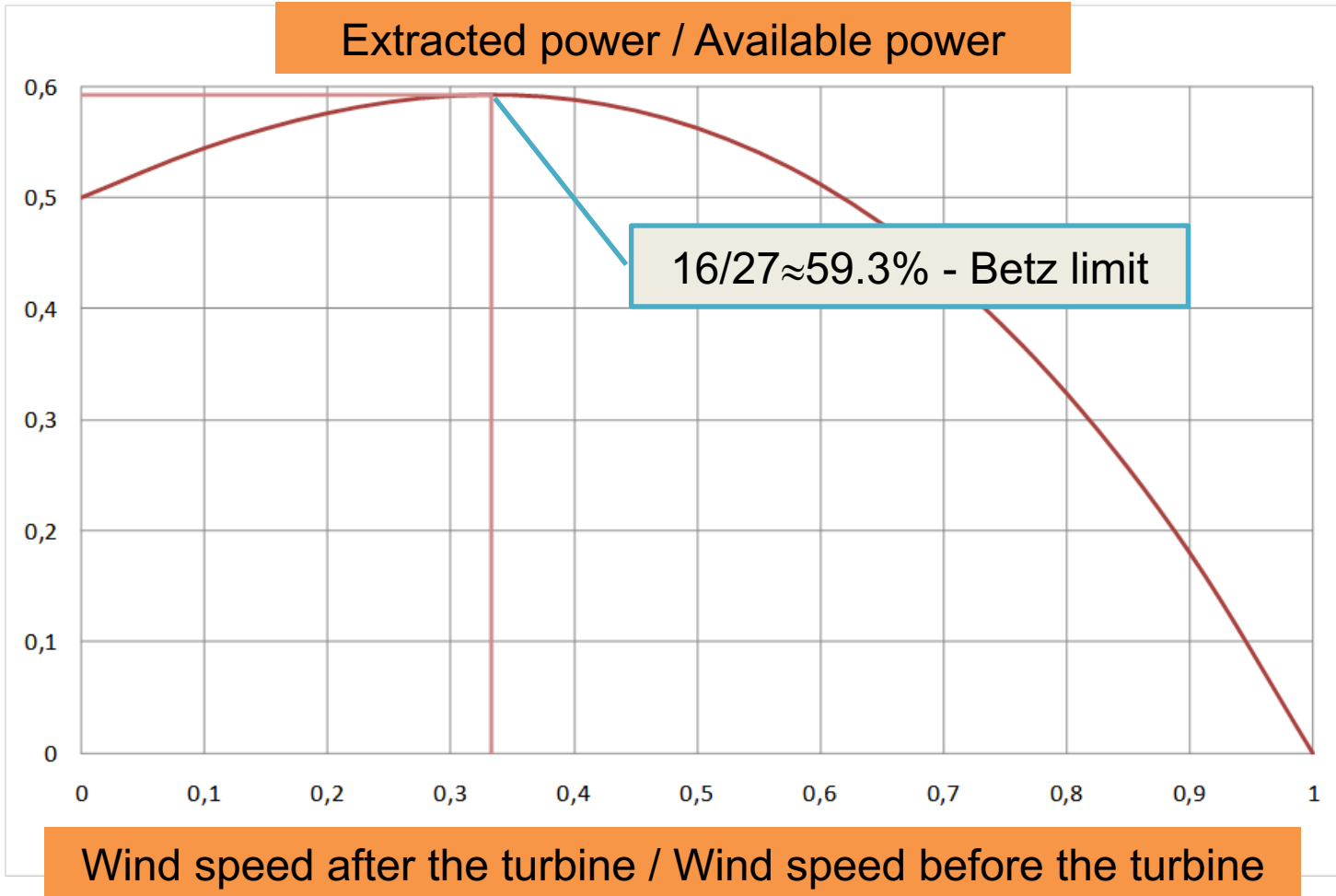
**Available power
in the wind**

$$P_{\text{avail}} = \frac{dE_{\text{kin}}}{dt} = \frac{1}{2} \left(\rho A \frac{dx}{dt} \right) u^2$$

$$P_{\text{avail}} = \frac{1}{2} \rho A u^3$$

$$\frac{P_r}{P_{\text{disp}}} = \frac{1}{2} \left(1 + \frac{u_2}{u_1} \right) \left[1 - \left(\frac{u_2}{u_1} \right)^2 \right]$$

Betz law



Currently about 45% of the available wind energy is captured by modern turbines

Prandtl law

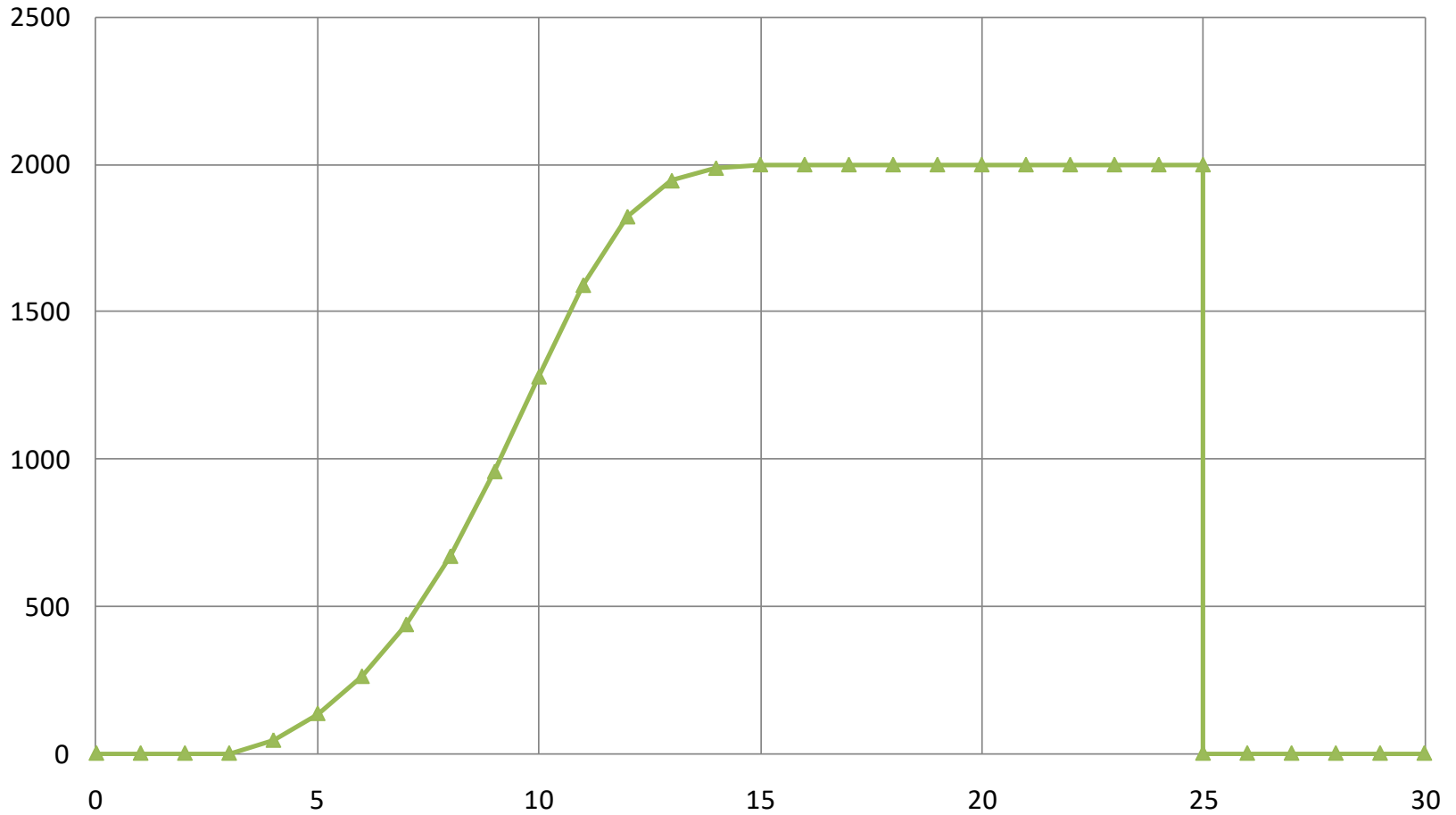
$$\frac{u(z_1)}{u(z_2)} = \frac{\ln\left(\frac{z_1}{z_0}\right)}{\ln\left(\frac{z_2}{z_0}\right)}$$

| Roughness Class RC | Roughness Length, Z ₀ (m) | Energy Index (%) | Local Terrain Type, Landscape, Topography, Vegetation |
|--------------------|--------------------------------------|------------------|--|
| 0 | 0.0002 | 100 | Water surface. |
| 0.5 | 0.0024 | 73 | Completely open terrain with a smooth surface, such as concrete runways in airports, mowed grass. |
| 1 | 0.03 | 52 | Open agricultural area without fences and hedgerows and very scattered buildings. Only softly rounded hills. |
| 1.5 | 0.055 | 45 | Agricultural land with some houses and 8 meter tall sheltering hedgerows within a distance of about 1250 meters. |
| 2 | 0.1 | 39 | Agricultural land with some houses and 8 meter tall sheltering hedgerows within a distance of about 500 meters. |
| 2.5 | 0.2 | 31 | Agricultural land with many houses, shrubs and plants, or 8 meters tall sheltering hedgerows within a distance of about 250 meters |
| 3 | 0.4 | 24 | Villages, small towns, agricultural land with many or tall sheltering hedgerows, forests and very rough and uneven terrain. |
| 3.5 | 0.8 | 18 | Larger cities with tall buildings. |
| 4 | 1.6 | 13 | Very large cities with tall buildings and sky scrapers. |

POWER CURVE

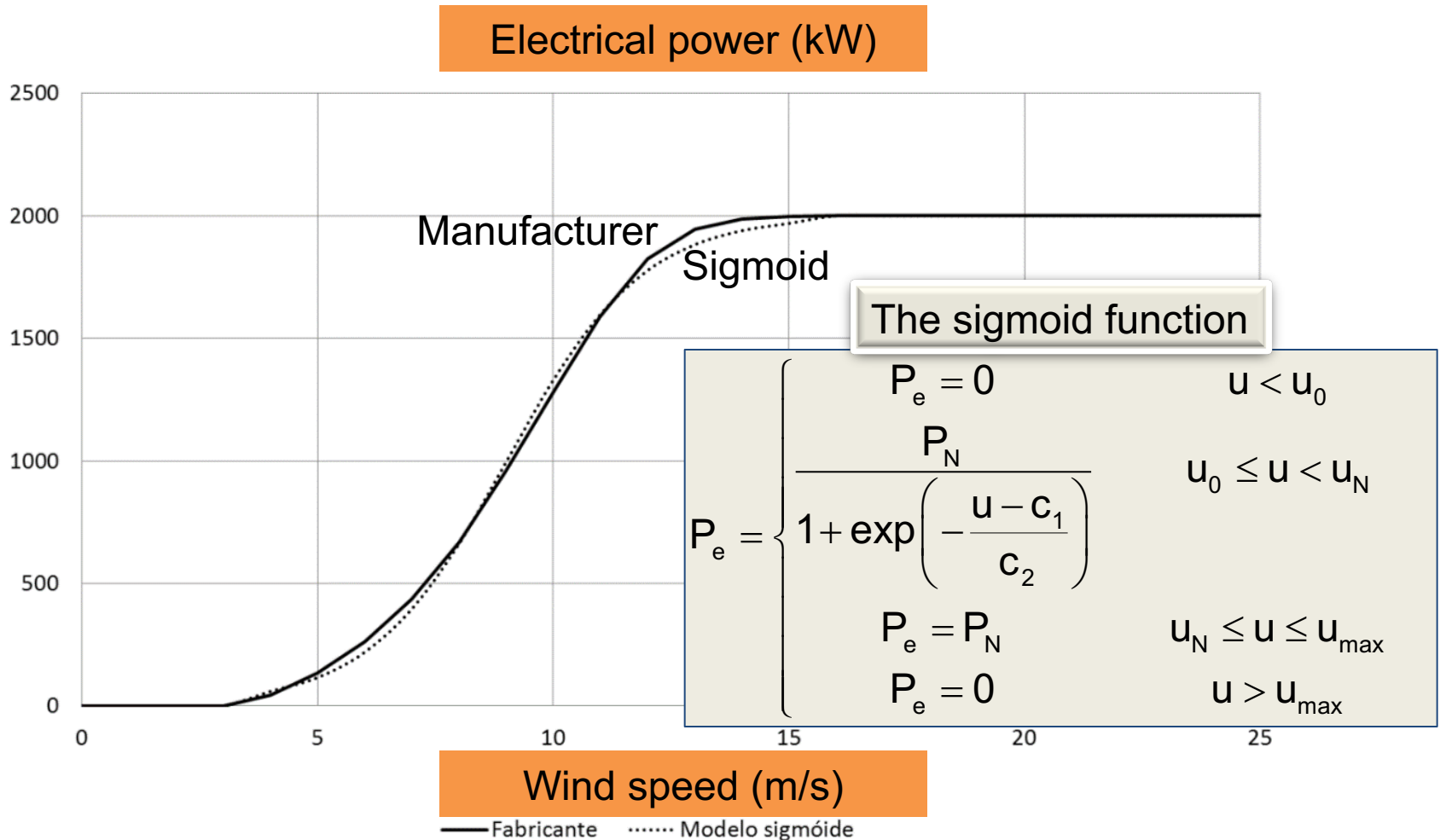
Power curve

Electrical power (kW)



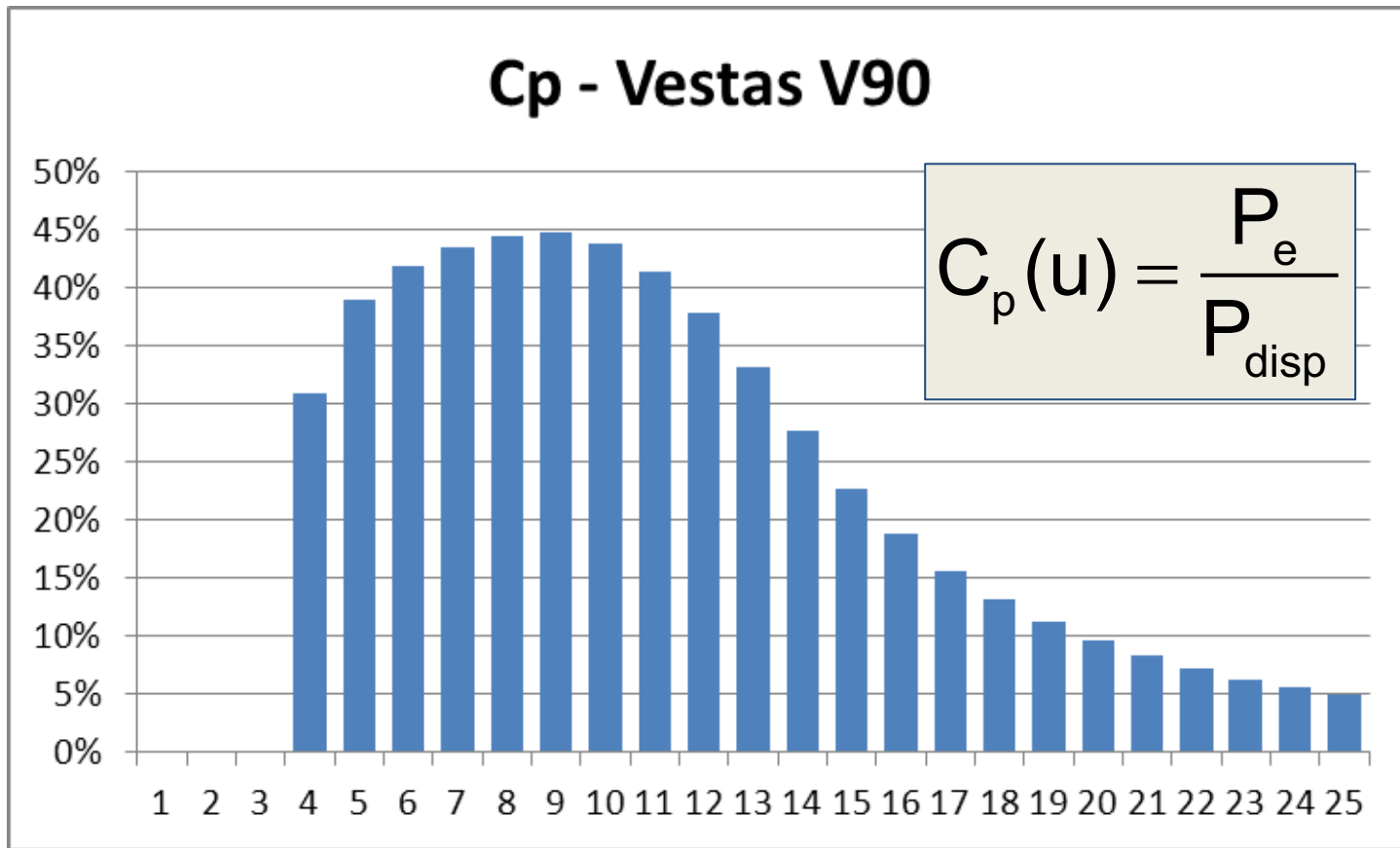
Wind speed (m/s)

Analytical representation



Power coefficient – C_p

AKA Coefficient of performance



ENERGY PRODUCTION ESTIMATES

Methods depend on available data

Data: analytical expressions for pdf and pc

$$E_a = 8760 \int_{u_0}^{u_{\max}} f(u) P_e(u) d\bar{u}$$

P_{med} (average power)
 f(u) – pdf
 P_e(u) – power curve (pc)

Data: discrete histogram and pc

$$E_a = \sum_{u_0}^{u_{\max}} f_r(u) P_e(u)$$

f_r – frequency of occurrence in hours/year; f_r(u)=8760f(u)

$$E_a = 8760 \sum_{i=u_1}^{u_{\max}} \left[(F(i-1) - F(i)) \frac{P_e(i) + P_e(i-1)}{2} \right]$$

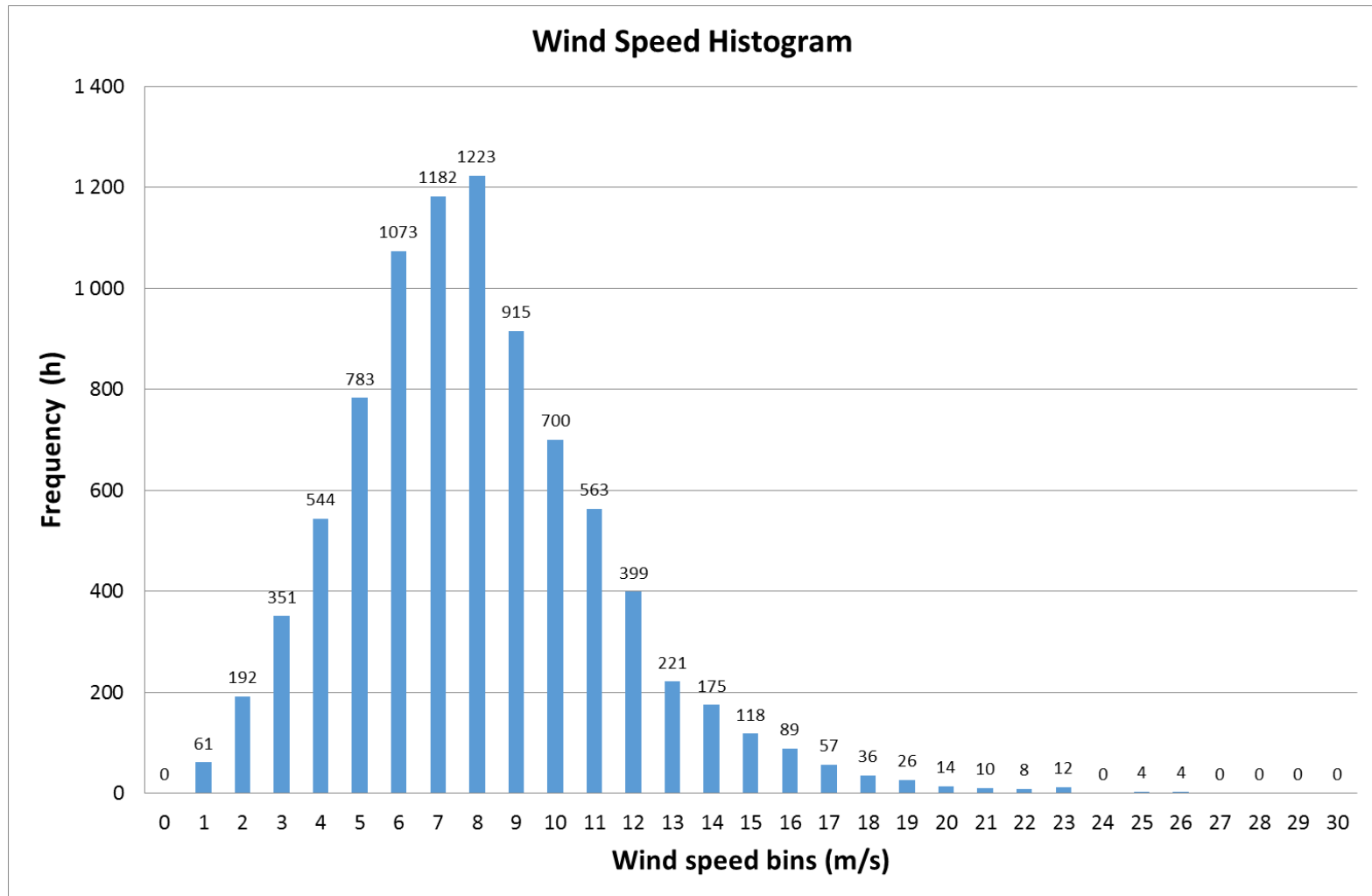
F(u) – cdf

Data: pdf analytical expression and pc discrete values

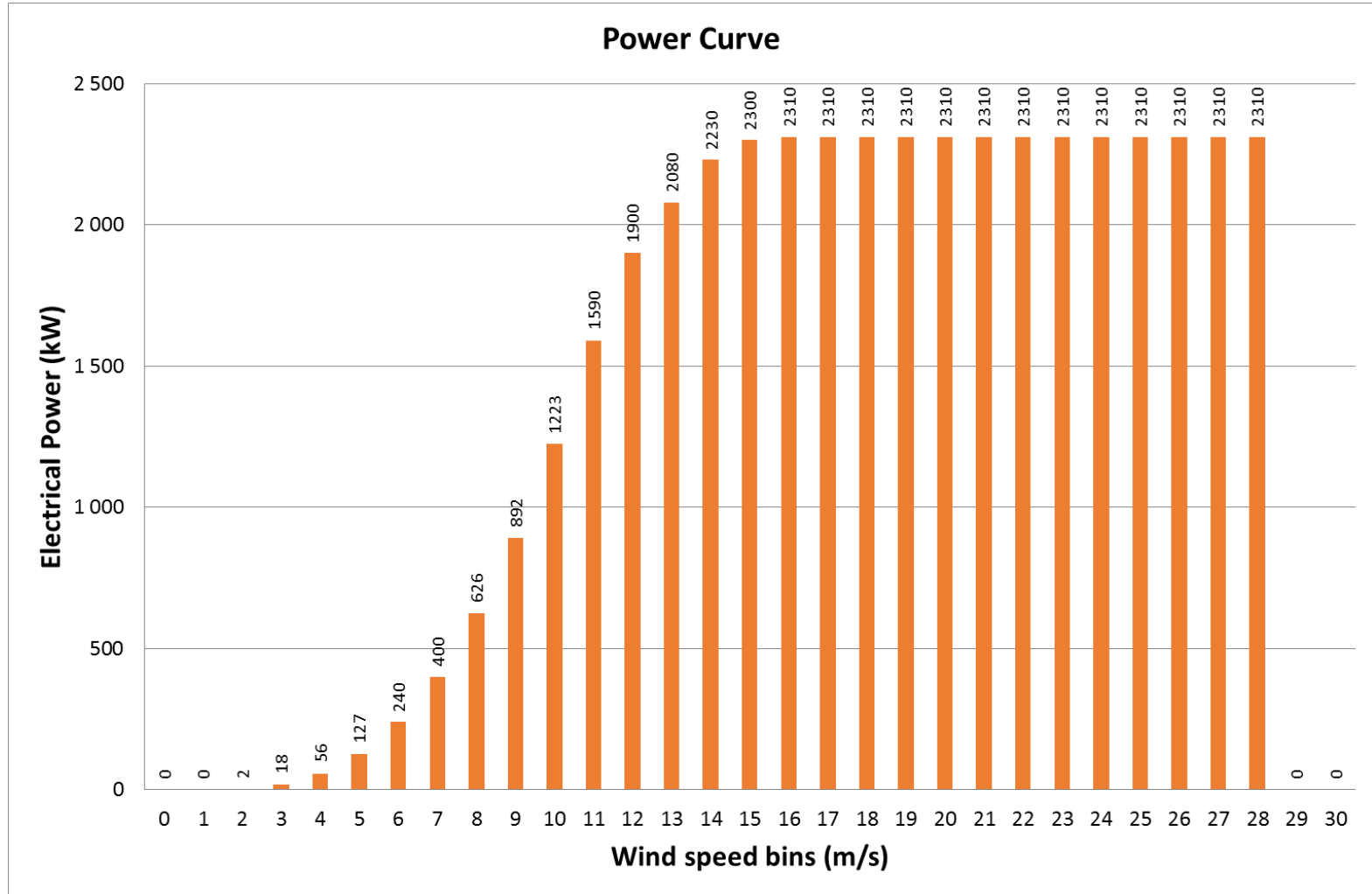
Input data

| | |
|------------------|---------|
| Rated power | 2310kW |
| Rotor diameter | 71m |
| Hub height | 80m |
| Roughness | 0.0300m |
| Measuring height | 20m |

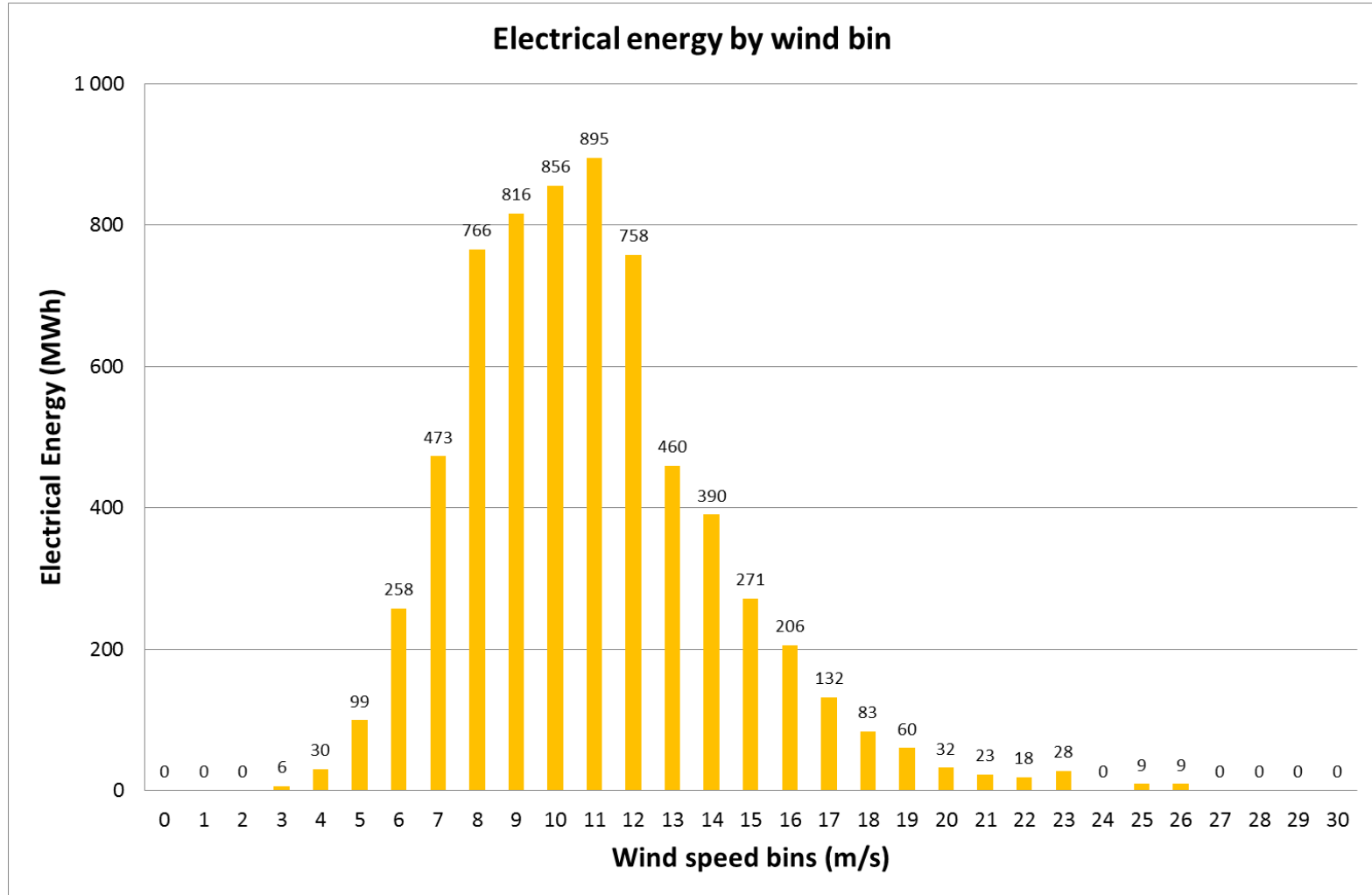
Experimental Computation – Input data



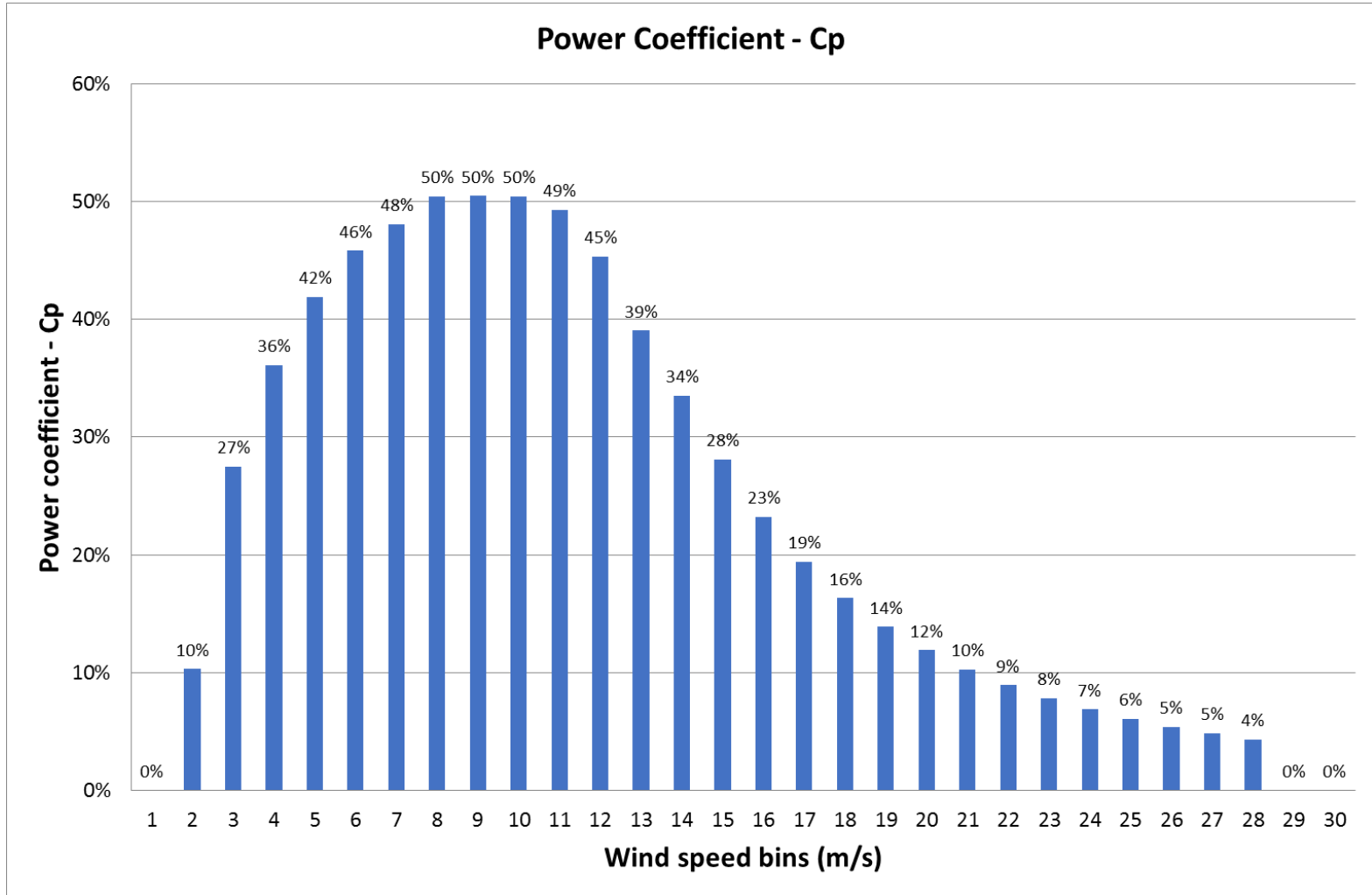
Experimental Computation – Input data



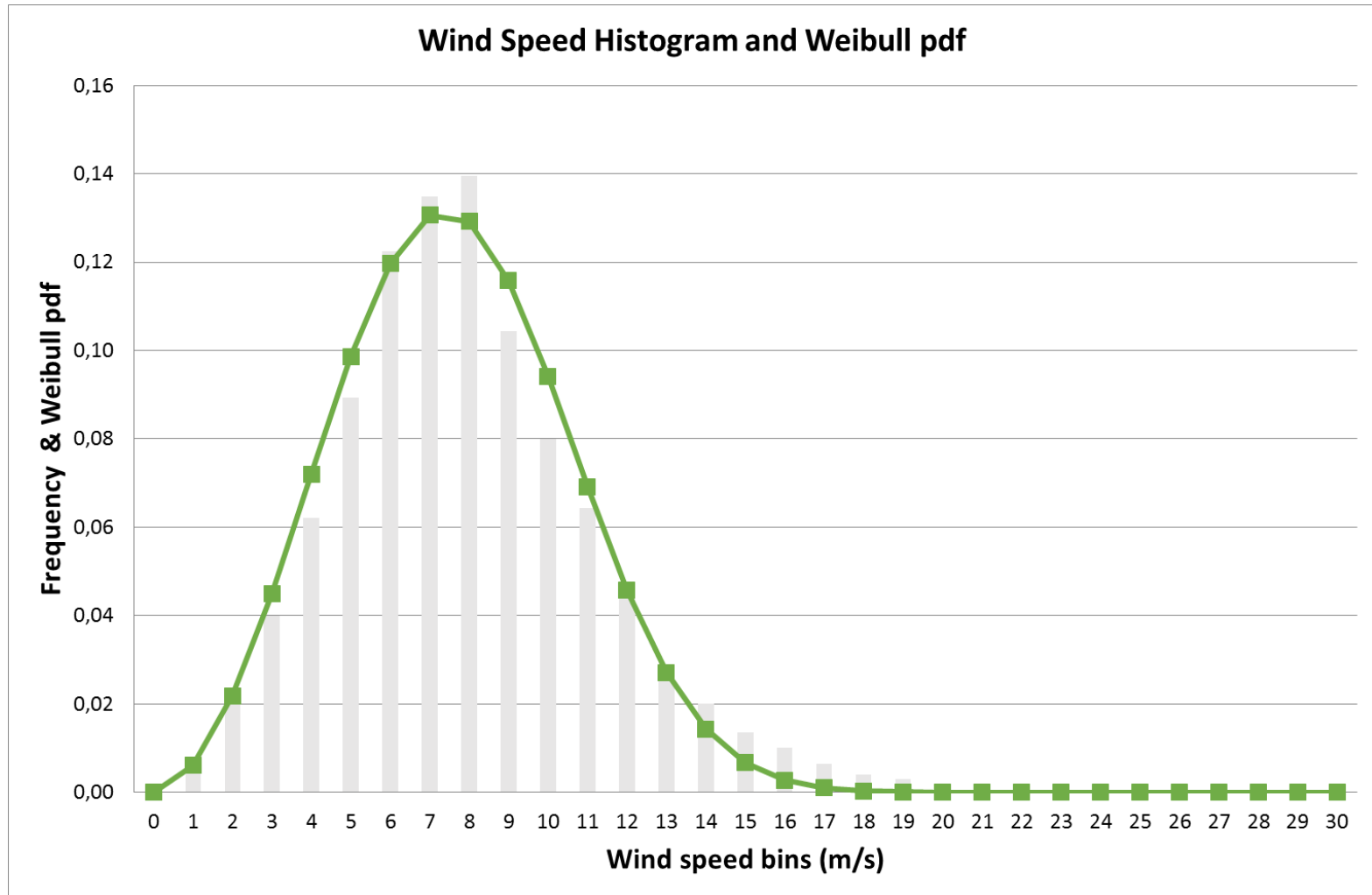
Experimental Computation – Results



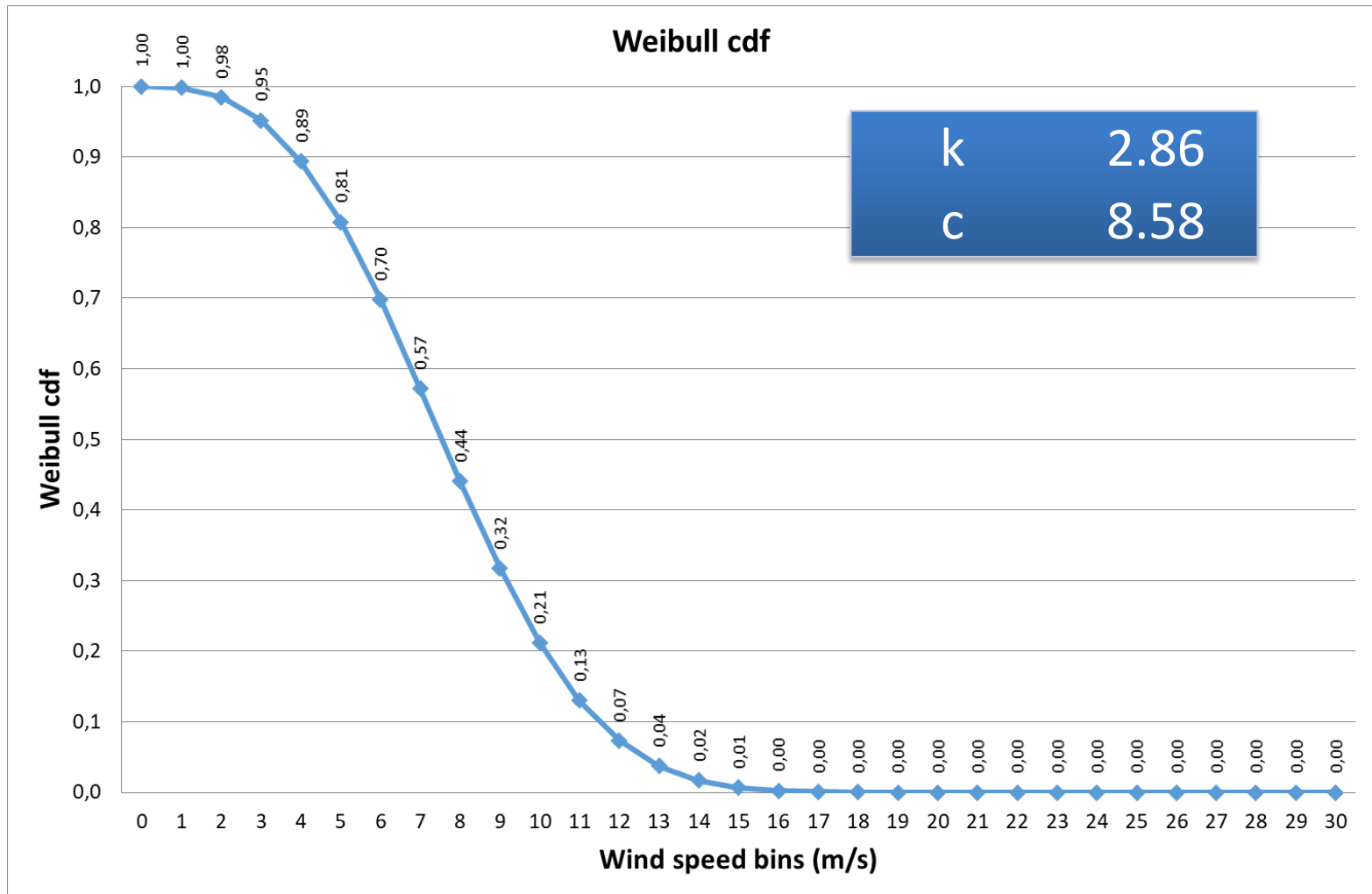
Experimental Computation – Results



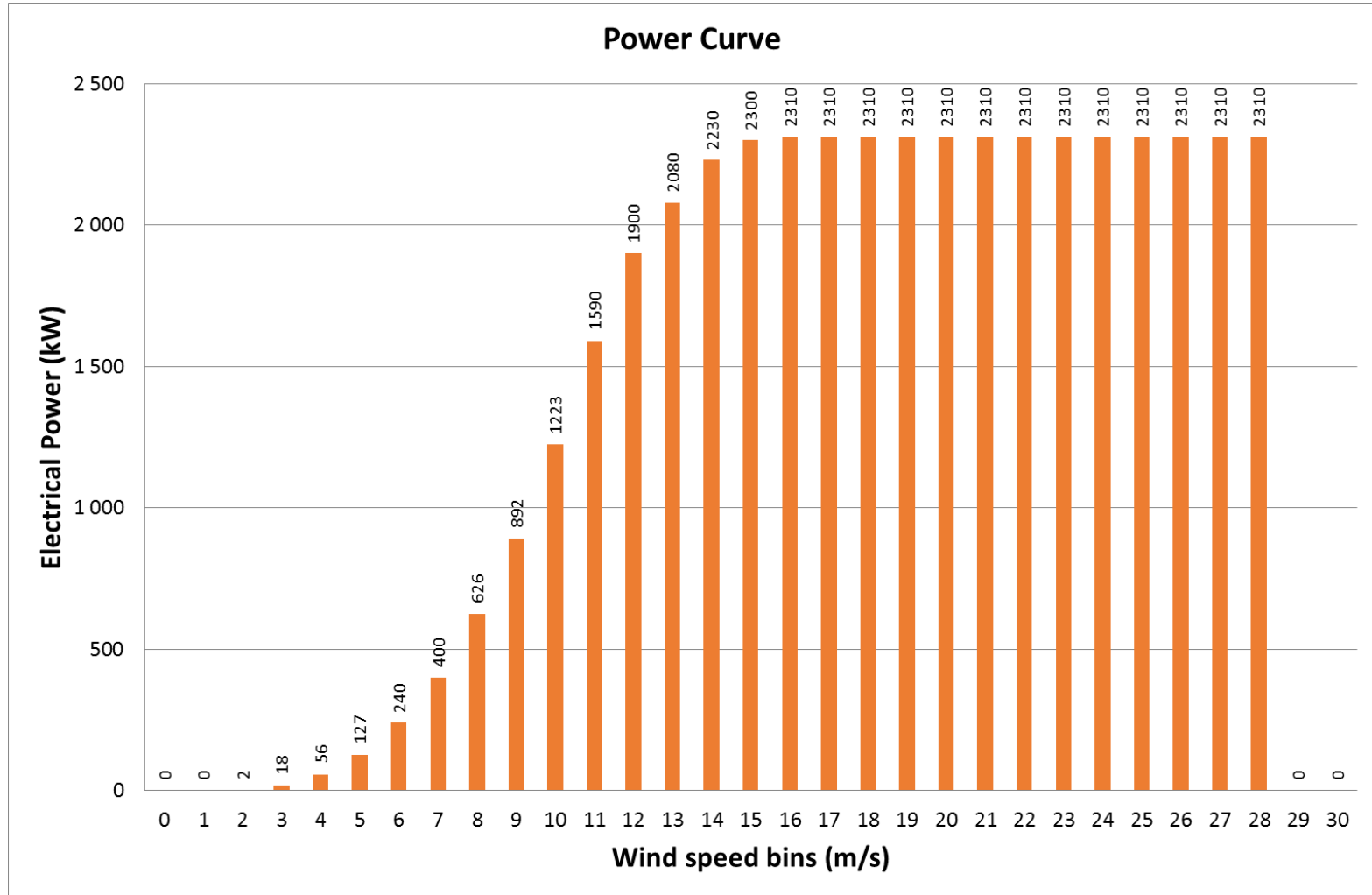
Analytical computation – Input data



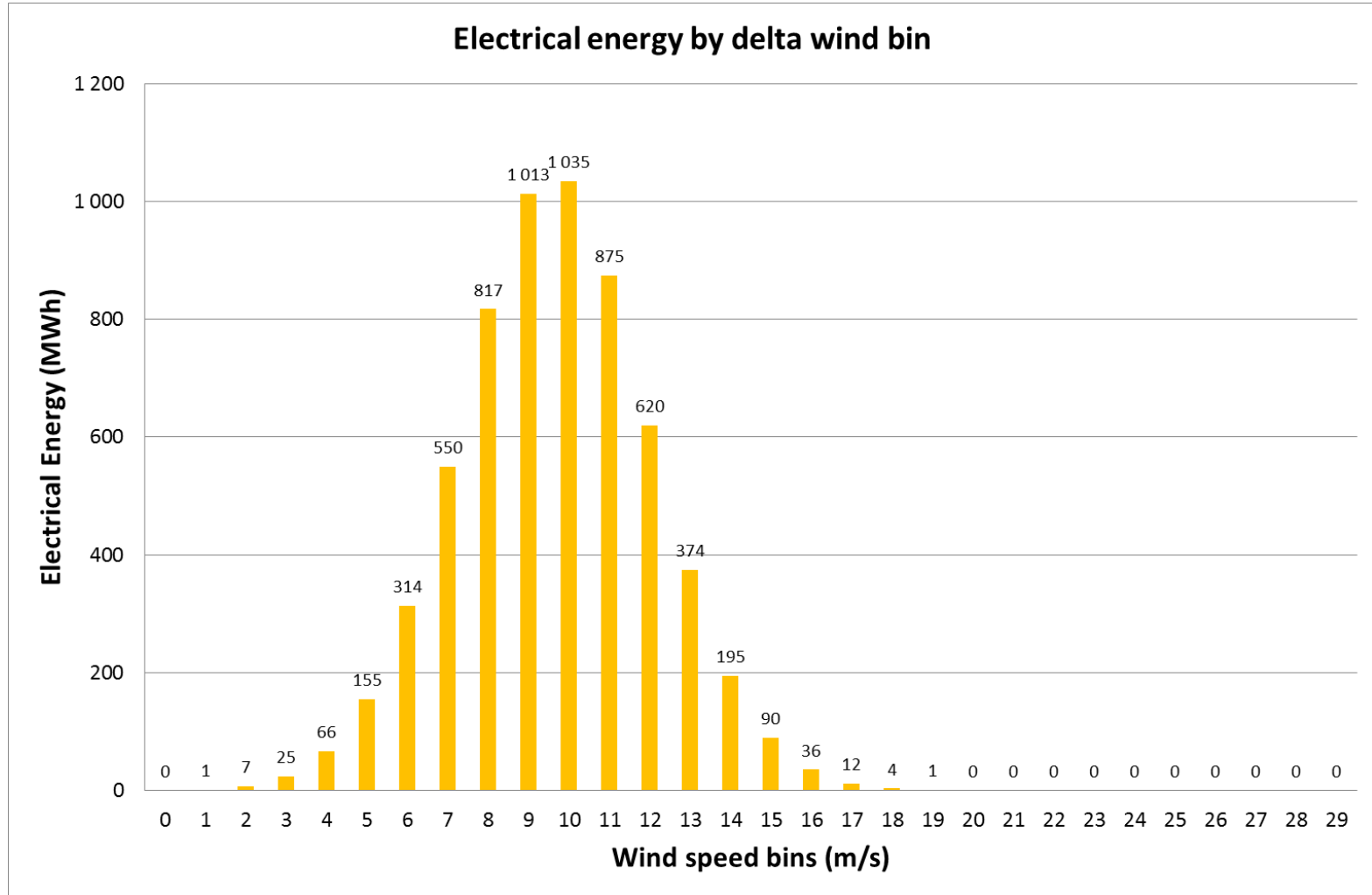
Analytic computation – Input data



Analytic Computation – Input data



Analytical Computation – Results



Results

| | Experimental | Analytic |
|----------------------|--------------|---------------------|
| Swept area | 3 959 | 3 959m ² |
| Max. wind speed @hub | 26.39 | 26.39m/s |
| Mean wind speed @hub | 8.00 | 8.00m/s |
| Min. wind speed @hub | 0.58 | 0.58m/s |
| Annual Energy | 6 680 | 6 239MWh |
| Utilization factor | 2 892 | 2 701h |
| Average power | 763 | 712kW |
| Capacity factor | 33.01% | 30.83% |

ENERGY YIELD FAST ESTIMATE

Fast Estimate

$$(P_{avail})_{avg} = \left(\frac{1}{2} \rho A u^3 \right)_{avg} = \frac{1}{2} \rho A (u^3)_{avg} \quad \longrightarrow \quad (P_{avail})_{avg} = \rho A \frac{3}{\pi} u_{ma}^3$$

$$E_a = P_{avg} 8760 \approx (C_p)_{avg} (P_{avail})_{avg} 8760 \quad (C_p)_{avg} \approx 0.25$$

$$\rho = 1.23 \text{ kg/m}^3$$

$$\frac{3}{\pi} \approx 0.95$$

$$E_a \approx 0.25 \rho A \frac{3}{\pi} u_{ma}^3 8760 \approx 0.3 A u_{ma}^3 8760$$

$$E_a = 2(RD)^2 u_{ma}^3 \text{ kWh}$$

Why $(u^3)_{avg} = \frac{6}{\pi} u_{ma}^3$?

$$(u^3)_{avg} = \int_0^{\infty} u^3 f_{Rayl}(u) du = \int_0^{\infty} u^3 \frac{2u}{c^2} \exp\left[-\left(\frac{u}{c}\right)^2\right] du = \frac{3}{4} c^3 \sqrt{\pi}$$

$$(u^3)_{avg} = \frac{3}{4} \sqrt{\pi} \left(\frac{2u_{ma}}{\sqrt{\pi}}\right)^3 = \frac{3}{4} \frac{8u_{ma}^3}{\pi} = \frac{6}{\pi} u_{ma}^3$$



$$k = 2$$

$$u_{ma} = c \Gamma\left(1 + \frac{1}{k}\right) = c \frac{\sqrt{\pi}}{2}$$



$$f_{Weib}(u) = \frac{k}{c} \left(\frac{u}{c}\right)^{k-1} \exp\left[-\left(\frac{u}{c}\right)^k\right]$$



$$k = 2$$

$$f_{Rayl}(u) = \frac{2}{c} \frac{u}{c} \exp\left[-\left(\frac{u}{c}\right)^2\right]$$

Why $\frac{2}{c^2} \int_0^{\infty} u^4 \exp\left[-\left(\frac{u}{c}\right)^2\right] du = \frac{3}{4} c^3 \sqrt{\pi}$?

$$(u^3)_{\text{avg}} = \int_0^{\infty} u^3 \frac{2u}{c^2} \exp\left[-\left(\frac{u}{c}\right)^2\right] du = \frac{2}{c^2} \int_0^{\infty} u^4 \exp\left[-\left(\frac{u}{c}\right)^2\right] du$$

$$\int_0^{\infty} x^m \exp(-ax^2) dx = \frac{\Gamma\left(\frac{m+1}{2}\right)}{2a^{\frac{m+1}{2}}}$$

From integral tables

$$m = 4; a = \frac{1}{c^2}; \Gamma\left(\frac{5}{2}\right) = \frac{3}{2} \frac{\sqrt{\pi}}{2}; a^{\frac{5}{2}} = \frac{1}{c^5}$$

$$\frac{2}{c^2} \int_0^{\infty} u^4 \exp\left[-\left(\frac{u}{c}\right)^2\right] du = \frac{2}{c^2} \frac{\frac{3}{4} \sqrt{\pi}}{\frac{1}{c^5}} = \frac{3}{4} c^3 \sqrt{\pi}$$

Example

- WTG
 - Capacity = 660 kW; Sigmoid parameters: $c_1=8.76$ & $c_2=1.48$; Rated wind speed: 15 m/s; Rotor diameter = 47 m; Rotor height = 40 m; $u_{ma}(40m) = 8.24$ m/s
- Compute:
 - The electricity produced when the wind speed is comprised between 9 m/s and 11 m/s. Compare different methods.

Solution

$$P(u) = \left(\frac{660}{1 + \exp\left(-\frac{u - 8.76}{1.48}\right)} \right)$$
$$f(u) = \frac{\pi}{2} \frac{u}{8.24^2} \exp\left[-\frac{\pi}{4} \left(\frac{u}{8.24}\right)^2\right]$$
$$F(u) = \exp\left[-\frac{\pi}{4} \left(\frac{u}{8.24}\right)^2\right]$$

Method#1

$$E(9 < u < 11) = 8760 \int_9^{11} P(u)f(u)du = 578.20\text{MWh} \quad (\text{step} = 0.01\text{m/s})$$

Method#2: error=-0.7%

$$E(9 < u < 11) = 8760 \left[(F(9) - F(10)) \left(\frac{P(9) + P(10)}{2} \right) + (F(10) - F(11)) \left(\frac{P(10) + P(11)}{2} \right) \right] = 574.34\text{MWh}$$

Method#3: error=-1.4%

$$g(u) = P(u)f(u)$$

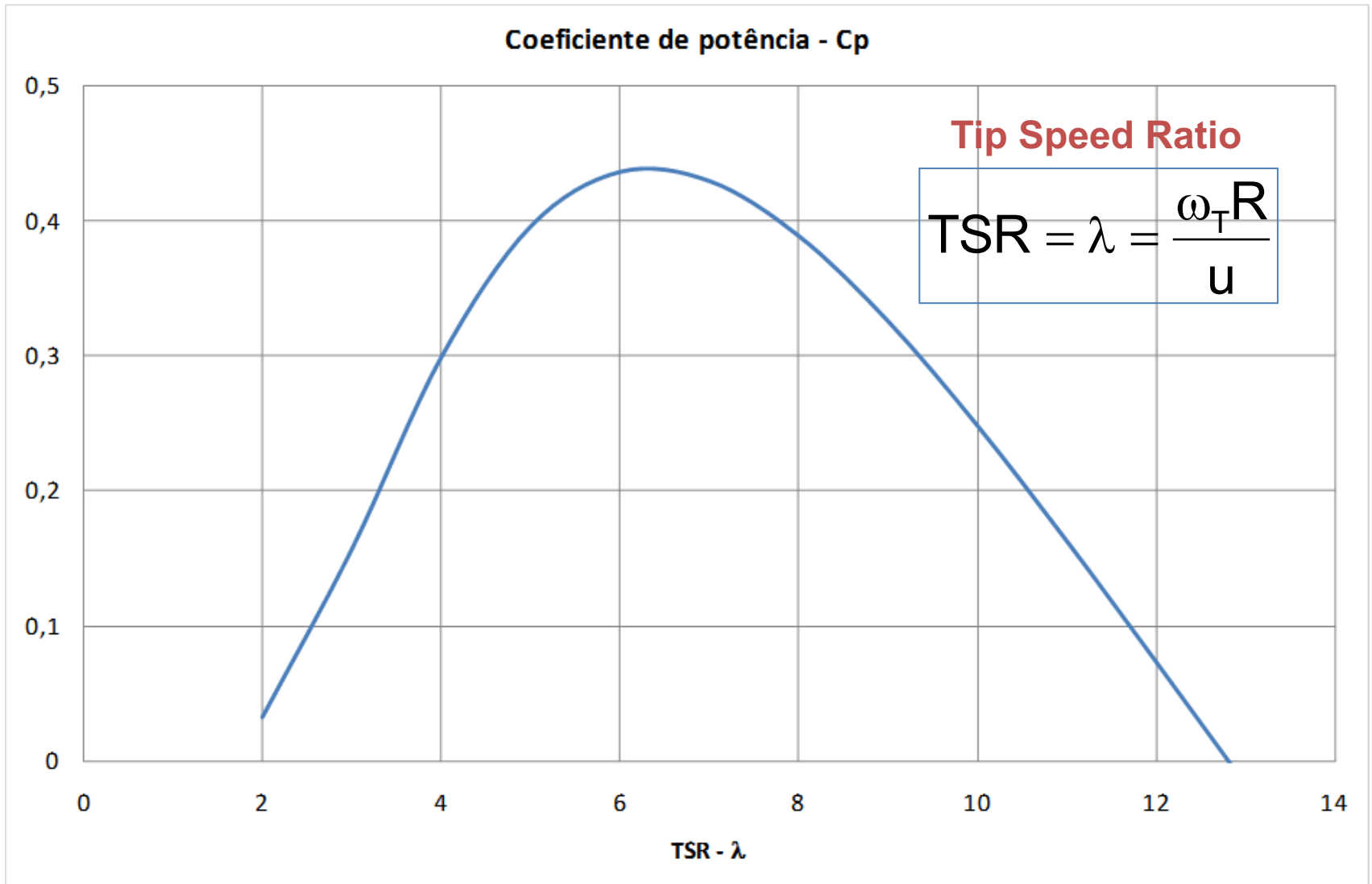
$$E(9 < u < 11) = 8760 \left[\left(\frac{g(9) + g(10)}{2} \right) + \left(\frac{g(10) + g(11)}{2} \right) \right] = 569.83\text{MWh}$$

Method#4: error=46%

$$E(9 < u < 11) = 8760(g(9) + g(10) + g(11)) = 8760(P(9)f(9) + P(10)f(10) + P(11)f(11)) = 846.02\text{MWh}$$

THE NEED FOR VARIABLE SPEED

Tip Speed Ratio



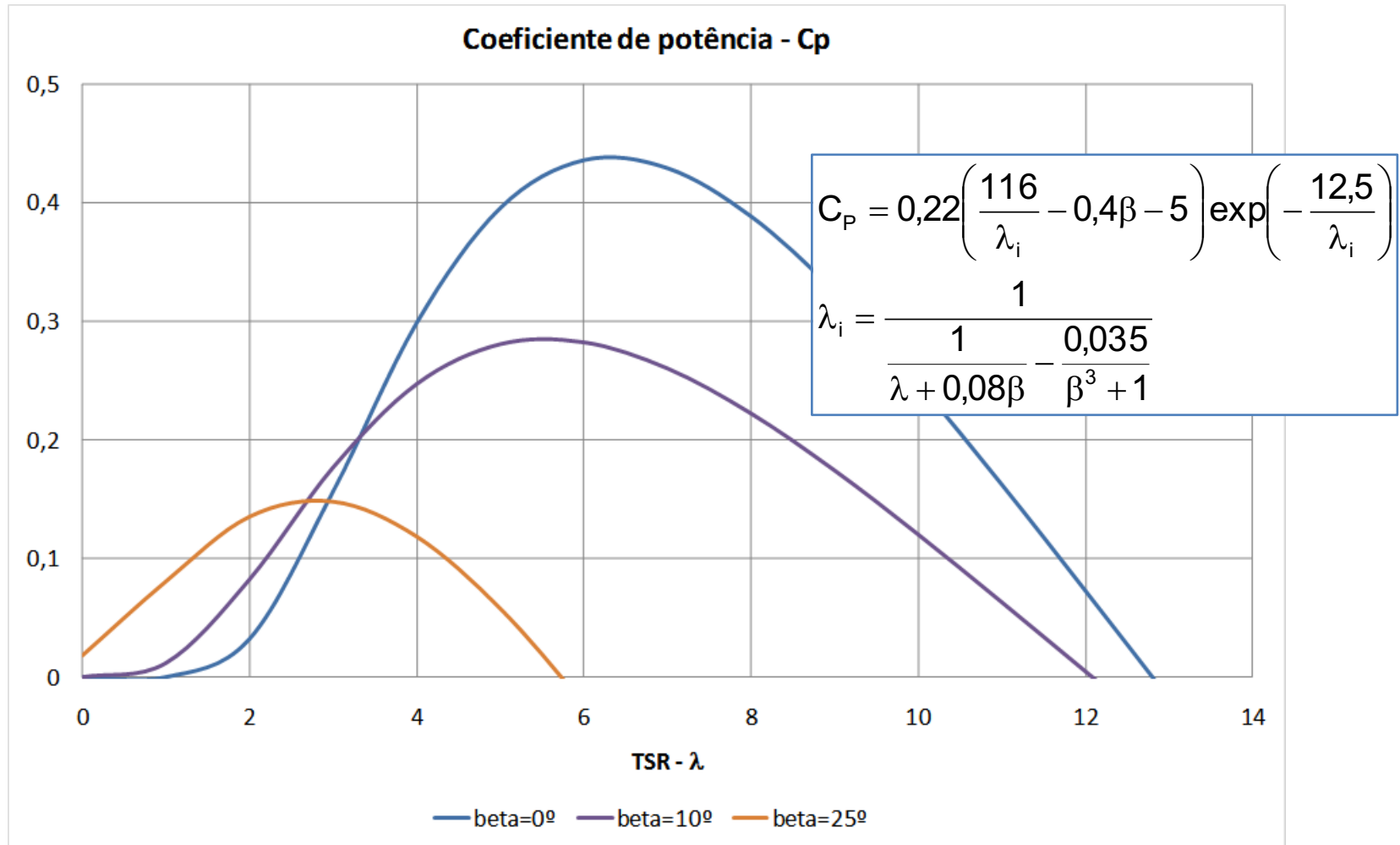
POWER CONTROL

Pitch control



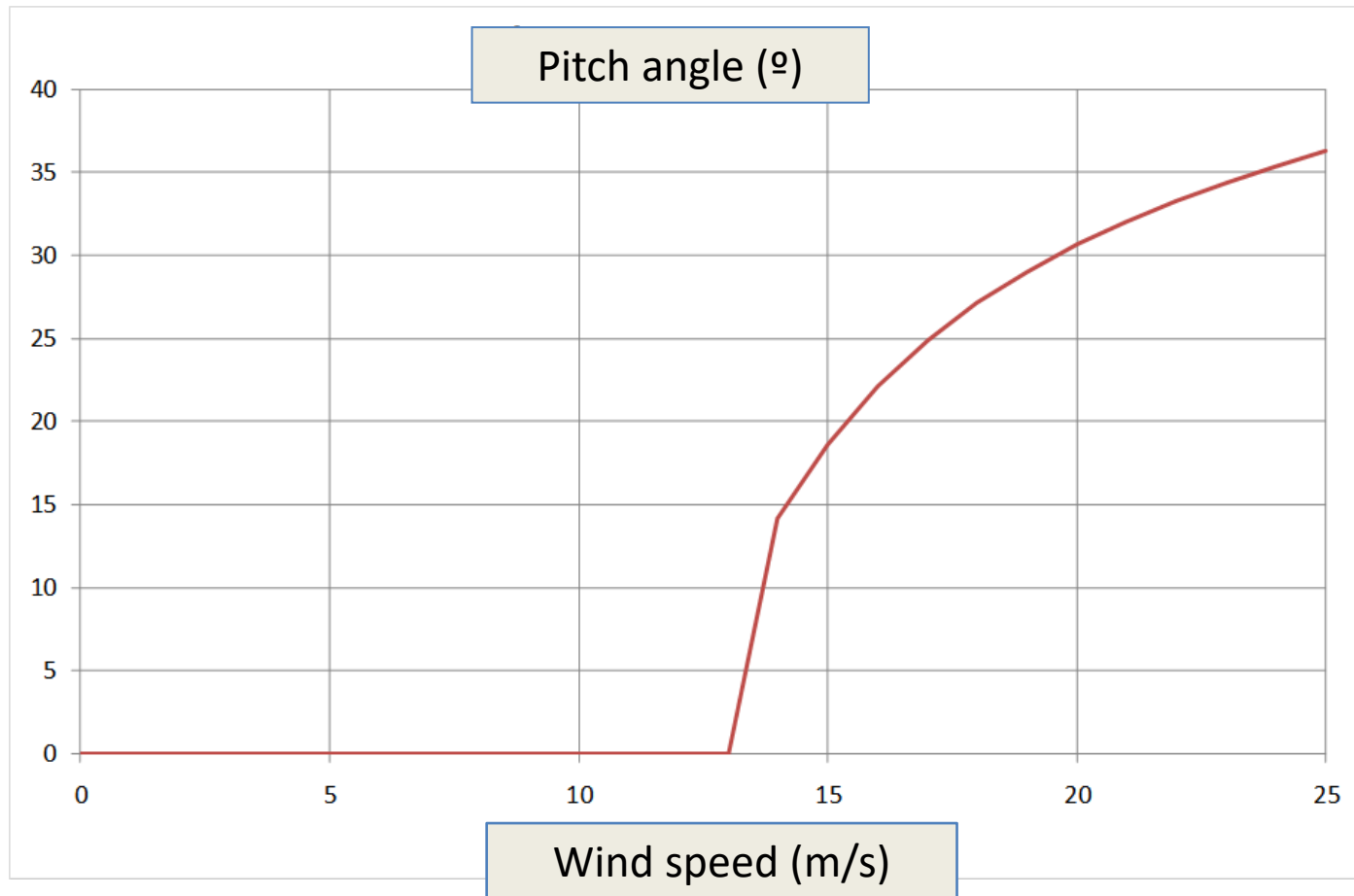
Pitching changes the angle of attack α and hence the power coefficient C_p

Pitch control



Cp reduces with pitch angle increase

Pitch control



Between cut in wind speed and nominal wind speed, the pitch is regulated (normally at zero value) in order to maximize C_p
Between nominal wind speed and cut off wind speed is increased in order to control (limit) power

WIND ENERGY CONVERSION EQUIPMENT

Electrical generators – Type#1 and #2

- **Squirrel-Cage Induction Generators (SCIG) – Type#1**
 - Used in the first WTG to keep costs down and reliability high
 - Very narrow rotor speed variation (slip) -> poor efficiency
 - Need capacitors to compensate the reactive power
 - Not used anymore
- **Wound-Rotor Induction Generator – Type#2**
 - Higher rotor speed variation -> increase efficiency
 - Wound-rotor induction generator connected through slip rings to thyristor-controlled variable resistances
 - Need capacitors to compensate the reactive power
 - Not used anymore

Electrical generators – Type#3

- **Double Fed Induction Generator (DFIG) – Type#3**
 - AKA Double Output Induction Generator (DOIG)
 - Take the Type#2 design to the next level, by adding variable frequency ac excitation (instead of simply resistance) to the rotor
 - Wound rotor with double output (rotor and stator) and electronic interface in the rotor with 2 converters
 - The 2 converters allow a bi-directional power flow in the rotor and a much wider speed range, above and below synchronous speed
 - The set of converters are typically only 30% of the rating of the machine
 - Can control voltage by consuming or generating reactive power
 - It is the most popular technology around the world

Electrical generators – Type#4

- **Direct Driven DC-Link Synchronous Generator (DDSG) – Type#4**
 - Synchronous generator (alternator) with rectifier and inverter
 - The output of the generator is sent to the grid through a full-scale back-to-back frequency converter
 - No gearbox -> much wider speed range
 - Electrically Excited Synchronous Generators (EESG), or self-excited Permanent Magnet Synchronous Generators (PMSG)
 - Can control voltage by consuming or generating reactive power
 - Highly efficient WTG