

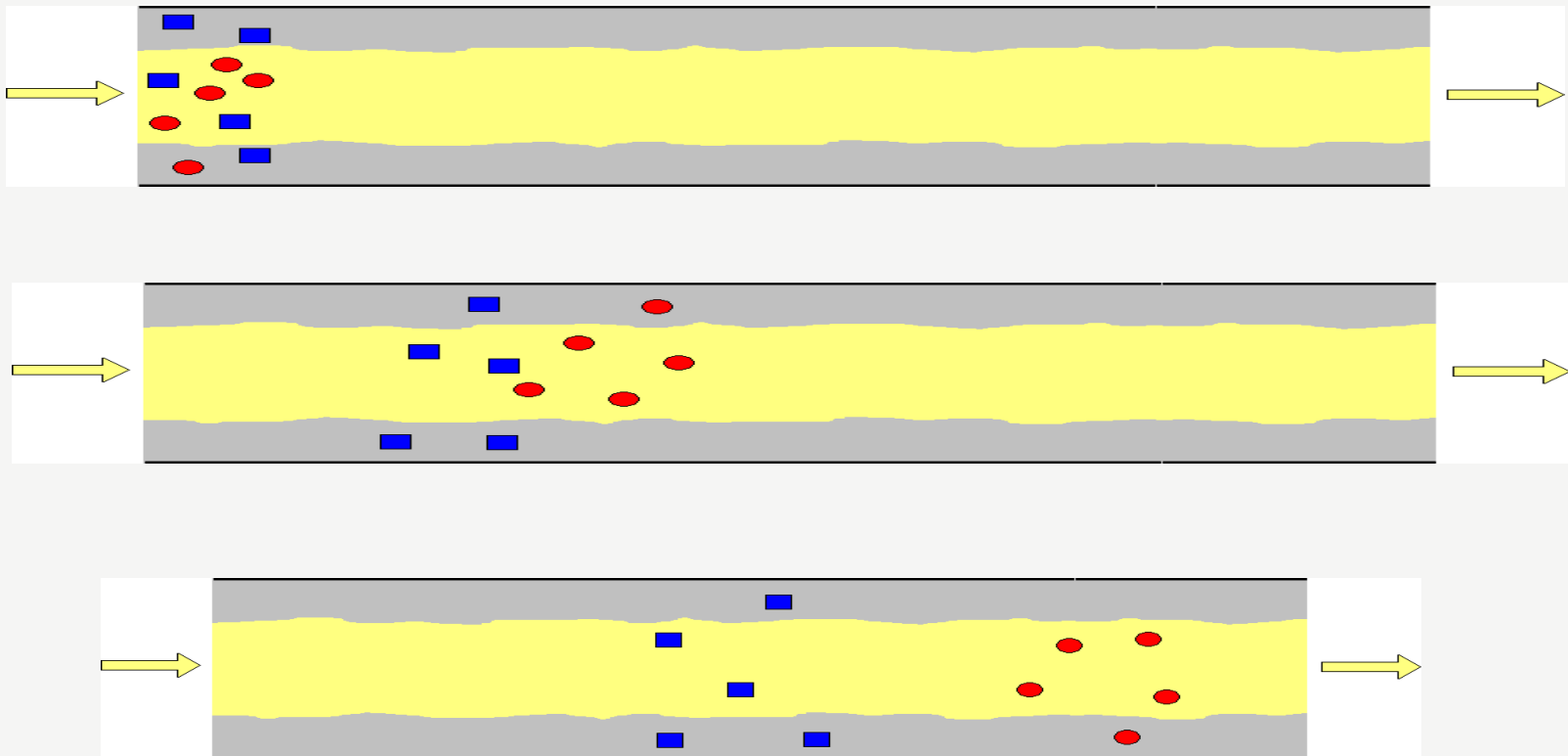
**General Fundamentals of Chromatographic Methods**

**Liquid Chromatography (LC)**

**Gas Chromatography (GC)**

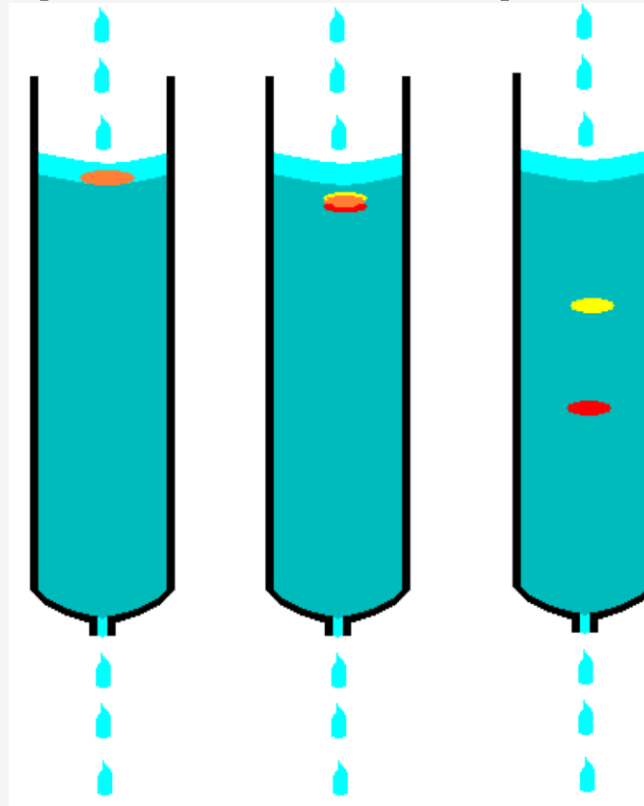
# Chromatographic Methods

Separation of a mixture by differential interaction of its components between a **STATIONARY PHASE** (liquid or solid) and a **MOBILE PHASE** (liquid or gas).



# Chromatographic Methods

**Column chromatography (most common): the stationary phase is contained in a column through which it is forced to pass the mobile phase)**



Two types of column:

1) Packed columns



2) Capillary columns



## Packed columns

Tube made of a chemically inert material (glass, steel...), with a total volume  $V_t = \pi r^2 L$  ( $L$  is the length of the column and  $r$  its internal radius), filled with finely divided solid particles, occupying fixed positions in the column with a volume  $V_s$ . The mobile phase occupies the interstitial spaces between particles, which defines  $V_m$ .

### Packing Variety

#### Sólido



Esféricas (porosas ou não)  
ou polímero irregular (poroso)

#### Líquido



Filme líquido (F) adsorvido  
em torno da partícula sólida

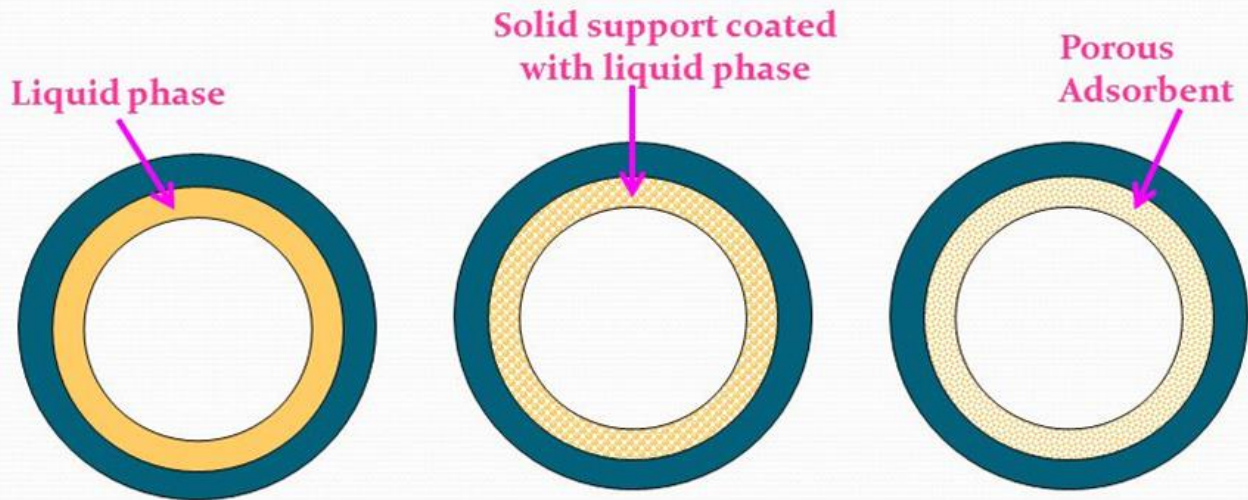
#### Fase Ligada



cadeia ramificada (CR)  
com ligação química à partícula

## Types of Capillary Columns

Capillary tube coated internally and evenly by the stationary phase.



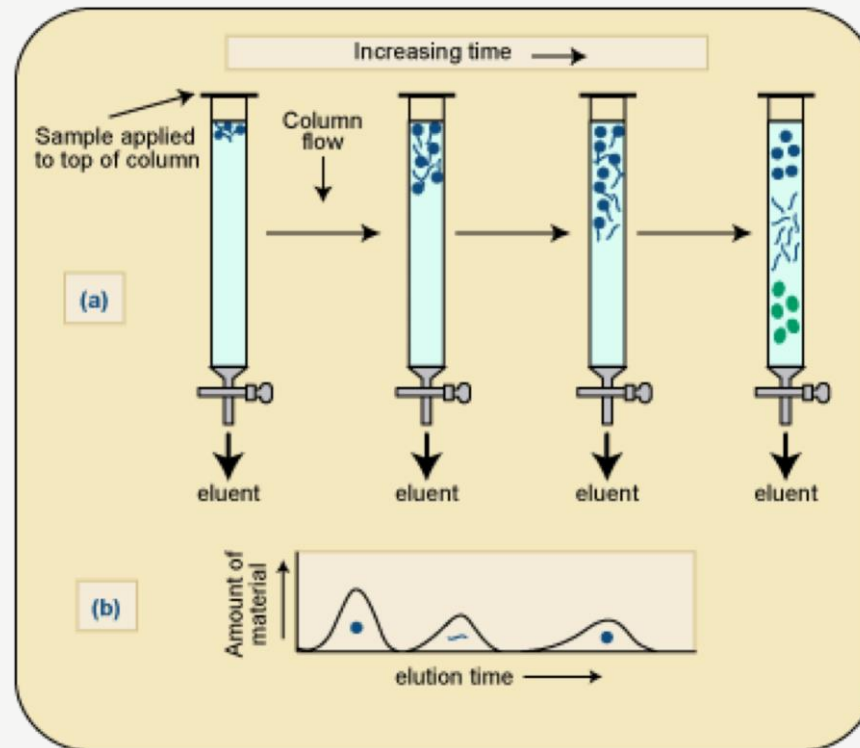
Wall-coated Open Tubular  
(WCOT)

Support-coated Open Tubular  
(SCOT)

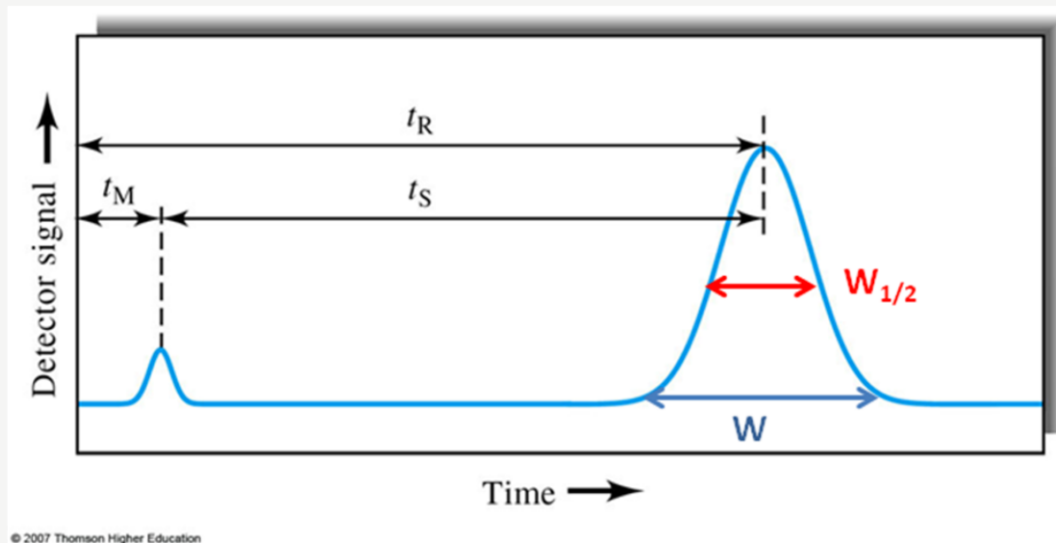
Porous Layer Open Tubular  
(PLOT)

**FSOT: Fused-silica open tubular column**

## Elution on column chromatography



## Chromatogram



**QUALITATIVE ANALYSIS:** Retention Time  $t_r$  (s) or Retention Volume  $V_r$  (mL) ( $V_r = F t_r$ ) where  $F$  is the mobile phase volumetric flow rate.

**QUANTITATIVE ANALYSIS:** Peak Area.



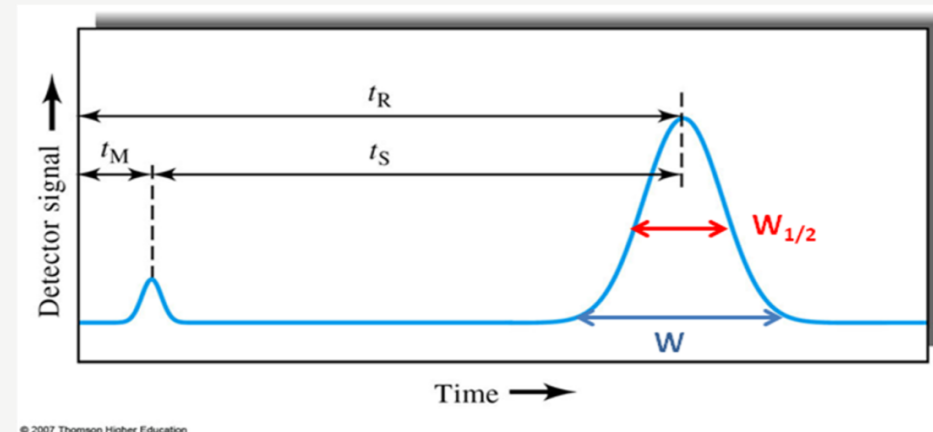
# Column Chromatography

Assuming the chromatographic column as a series of independent stages where the balance between the analyte, the stationary phase (SP) and the mobile phase (MP) occurs:



Each "stage" of equilibrium is called a **THEORETICAL PLATE**

- $t_r$  - retention time (s)
- $W_{1/2}$  - width at half height (units of  $t_r$ )
- $W$  - triangle base width (tr units)
- $t_M$  - retention time (s) of an unretained substance, i.e., elution time of the eluent.



# Column Chromatography

Assuming the chromatographic column as a series of independent stages where the balance between the analyte, the stationary phase (SP) and the mobile phase (MP) occurs:



Each "stage" of equilibrium is called a  
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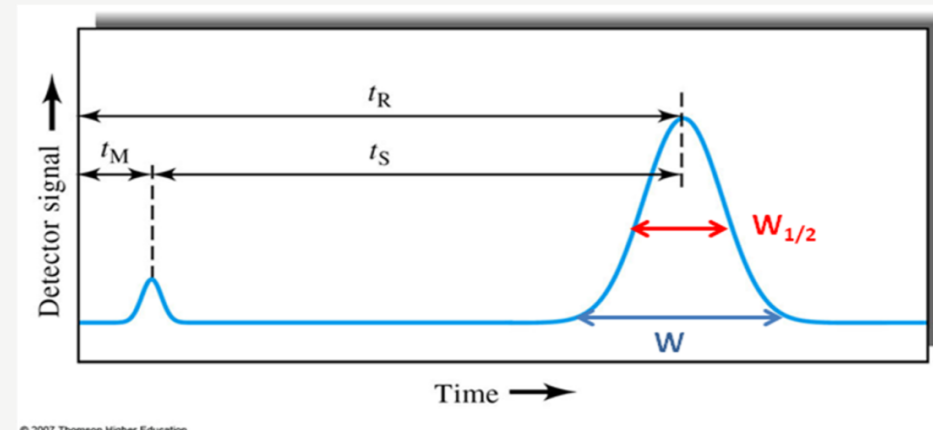
Column of length  $L$  (cm) formed by a number  $N$  of theoretical plates of height  $H$  (height equivalent to a theoretical plate):

$$N = L/H$$

Calculation of  $N$  from the chromatogram (assuming the peaks are Gaussian)

$$N = 16 (t_R/W)^2$$

$$N = 5.54 (t_R/W_{1/2})^2$$



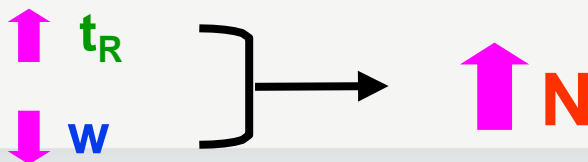
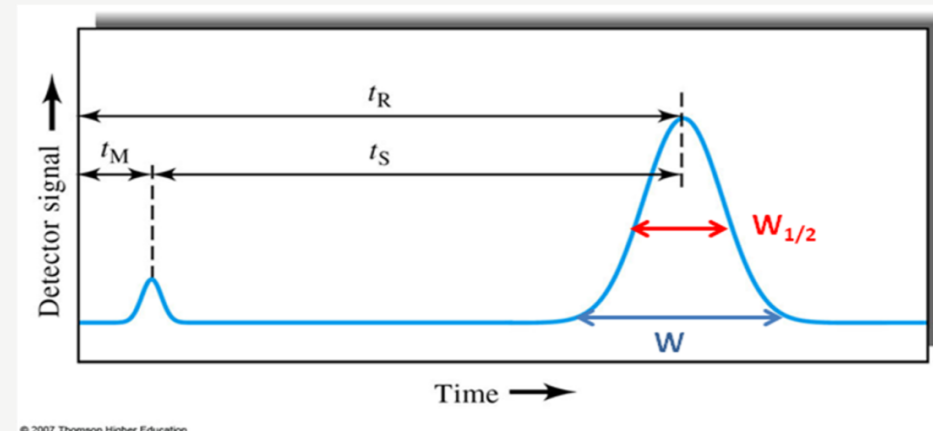
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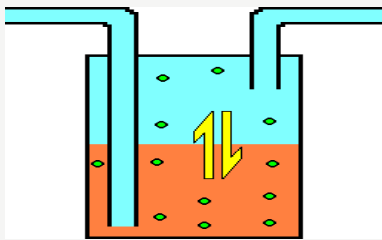
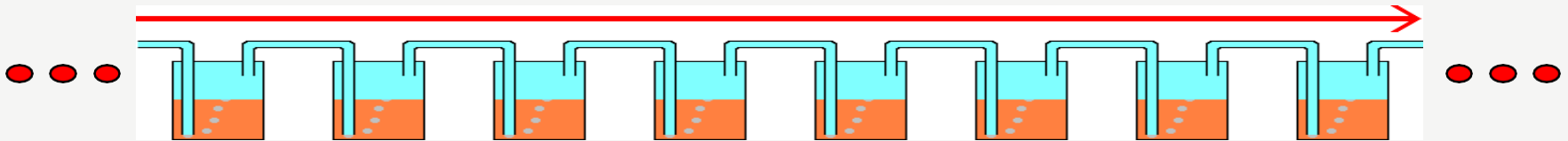
$$N = 16 (t_R/W)^2$$



Column more efficient

# Column Chromatography

An analyte distribution equilibrium between SP and MP occurs.



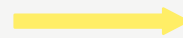
$$K_C = \frac{[A]_s}{[A]_M}$$

**$K_C$  = Distribution Constant**

$[A]_s$  = analyte concentration in SP

$[A]_M$  = analyte concentration in the MP

↓ *Affinity for the SP*



↓  $[A]_s$

**LESS RETENTION!!!**

## Parameters that characterize a chromatographic elution

$A(m) \rightleftharpoons A(s)$

- **Distribution constant:**

$$K_c = [A]_s / [A]_m = (n_s/V_s)/(n_m/V_m)$$

$V_m$ : Volume of the mobile phase ( $V_m = t_m F$ )

$n_s$  e  $n_m$ : moles of A in each of the phases

- **Selectivity factor:**

$$\alpha = k_2/k_1 = (t_2 - t_m)/(t_1 - t_m)$$

for two solutes 1 and 2 where

2 is the most retained

**(ideally  $\alpha > 1$ )**

- **Retention factor:**

Column capacity to retain a component of the sample, i.e., is the measure of retention in the stationary phase.

The more a component is retained by the column, the greater is its k.

$$k = n_s/n_m = K_c V_s / V_m \text{ (Ideally } 1 < k < 10)$$

Relationship between retention factor and retention time

**k = stationary phase time/mobile phase time**

$$k = (t_r - t_m)/t_m = (V_r - V_m)/V_m$$

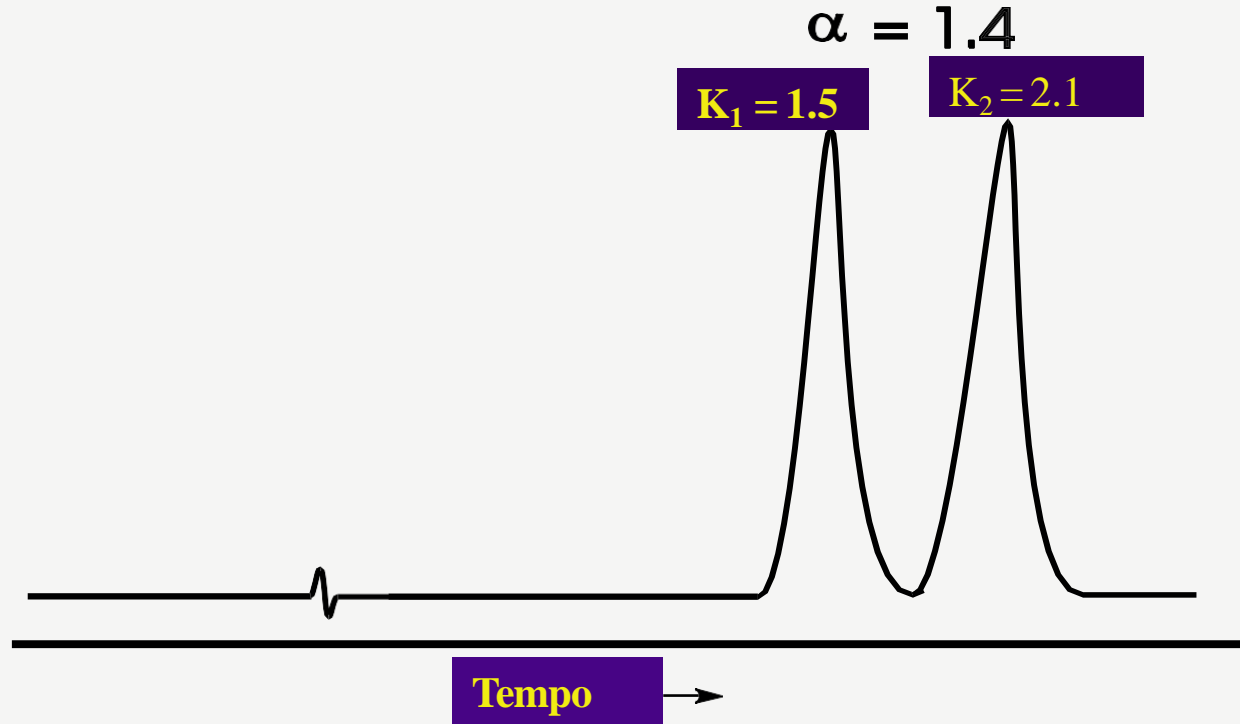
$V_r$  – Retention volume for the solute

## Selectivity ( $\alpha$ )

$$\alpha = k_2/k_1$$

$\alpha$  = relative position of 2 peaks

Ideally:  $\alpha > 1$



# Resolution ( $R_s$ )

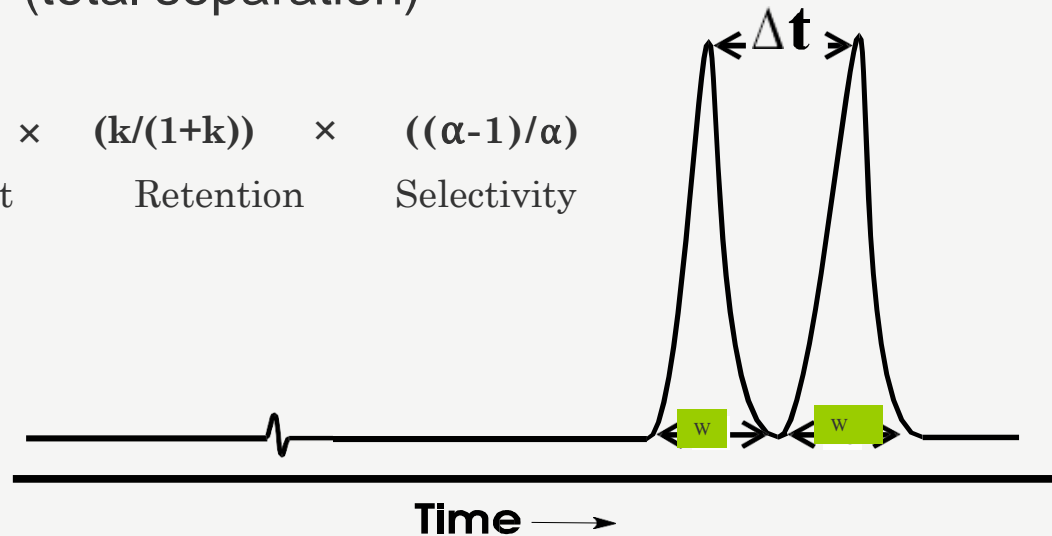
$R_s$  = actual peak separation

$$R_s = 2 (t_{R2} - t_{R1}) / (w_1 + w_2)$$

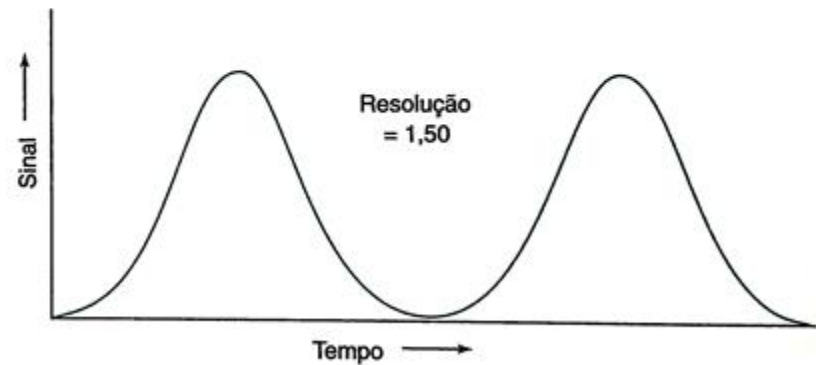
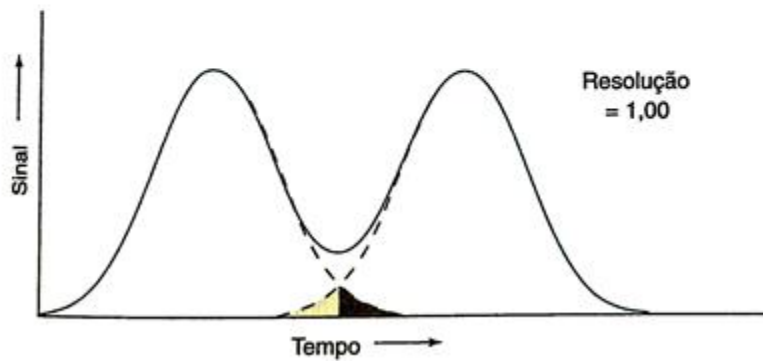
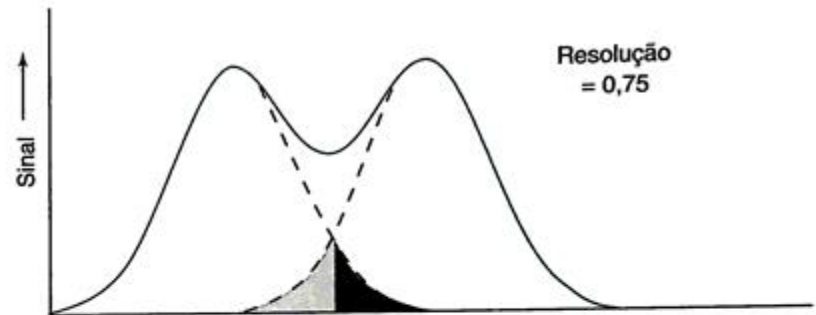
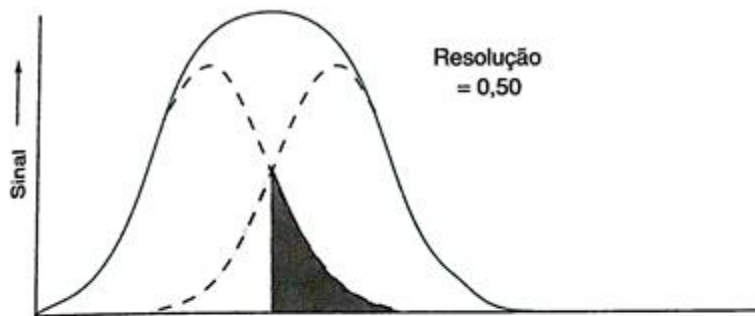
$$R_s = \Delta t_R / W_{\text{average}} = 0.589 \Delta t_R / W_{1/2 \text{ average}}$$

$R_s = 0$  (no separation),  $R_s = 1$  (partial separation),  $R_s = 1.5$  (total separation)

$$R_s = \underbrace{((\sqrt{N})/4)}_{\text{Efficient}} \times \underbrace{(k/(1+k))}_{\text{Retention}} \times \underbrace{((\alpha-1)/\alpha)}_{\text{Selectivity}}$$



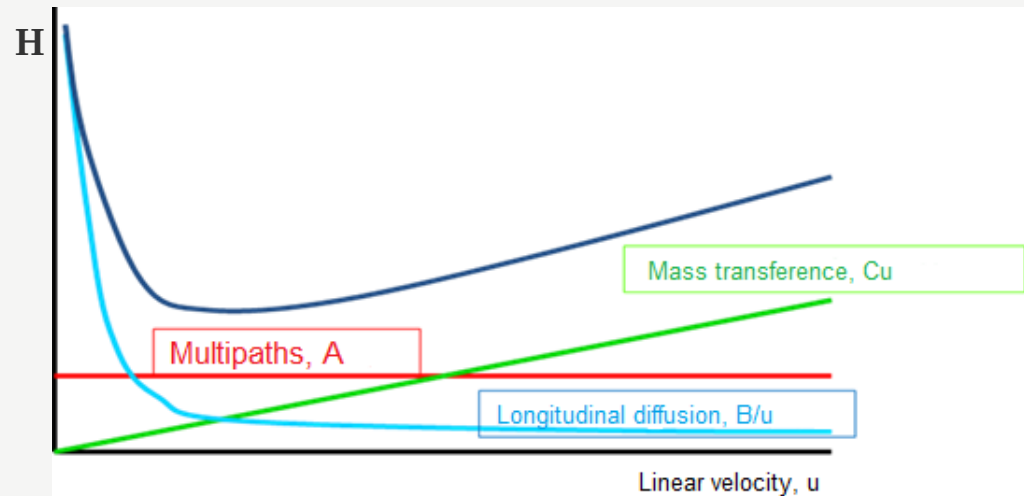
# Resolution ( $R_s$ )





# Optimizing the efficiency of a column

Kinetic Theory - The equivalent height of a theoretical plate  $H$  is a function of the average linear velocity  $u$ .



**Algebraic relations between  $H$  and  $u$ :**

- Packed Columns: van Deemter equation

$$H = A + \frac{B}{u} + C \cdot \bar{u}$$

(A, B, C = constants)

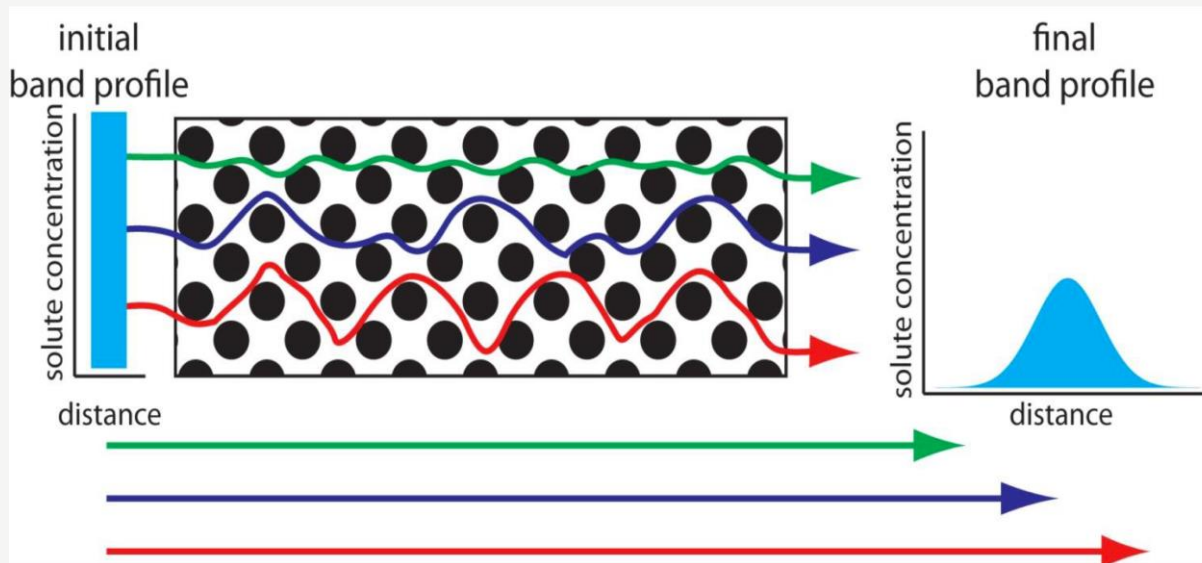
- Capillary Columns: Golay equation

$$H = \frac{B}{u} + (C_M + C_S) \cdot \bar{u}$$

(B,  $C_M$ ,  $C_S$  = constants)

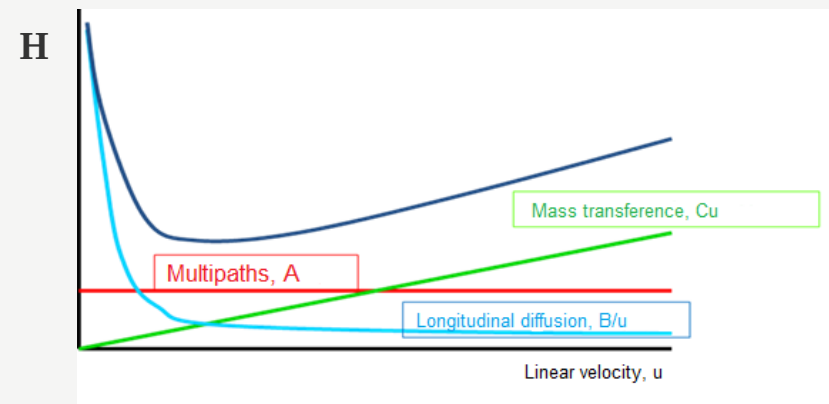
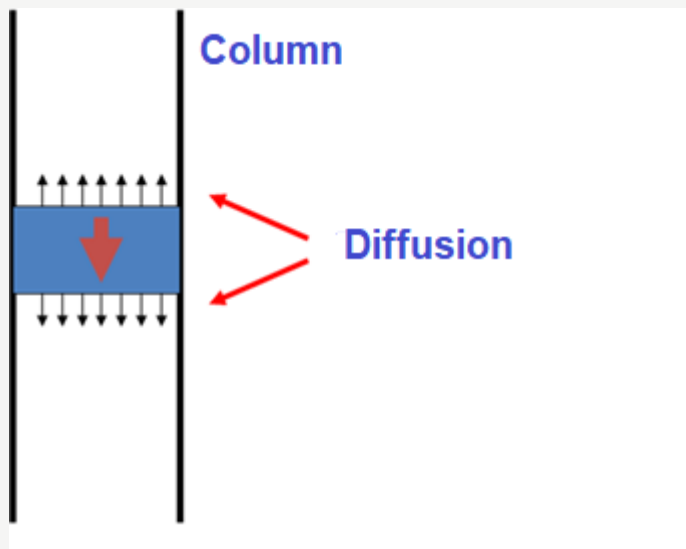
## Kinetic Theory - Multipath Terms(A)

**Multipath term A (independent of  $u$ ):**  $W$  increases with  $t_R$  and/or  $L$  due to the different paths the species can take inside the column.



## Kinetic Theory - Longitudinal Diffusion Terms ( $B/u$ )

**Longitudinal Diffusion Term ( $B/u$ )** refers to the diffusion of a solute into the mobile phase.  $B = f(D)$  due to the passage of each of the species in the mixture from the more concentrated zone to the more diluted ones, and therefore proportional to the diffusion coefficient  $D$ .



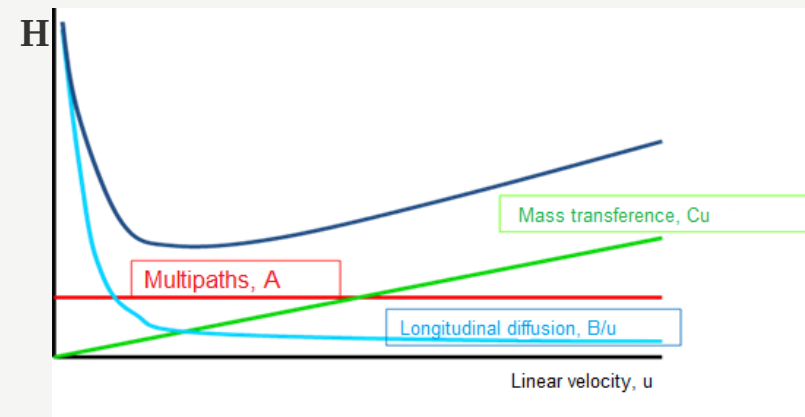
## Kinetic Theory - Mass Transfer Term ( $C \cdot u$ )

$$(C \cdot u = C_S u + C_M u)$$

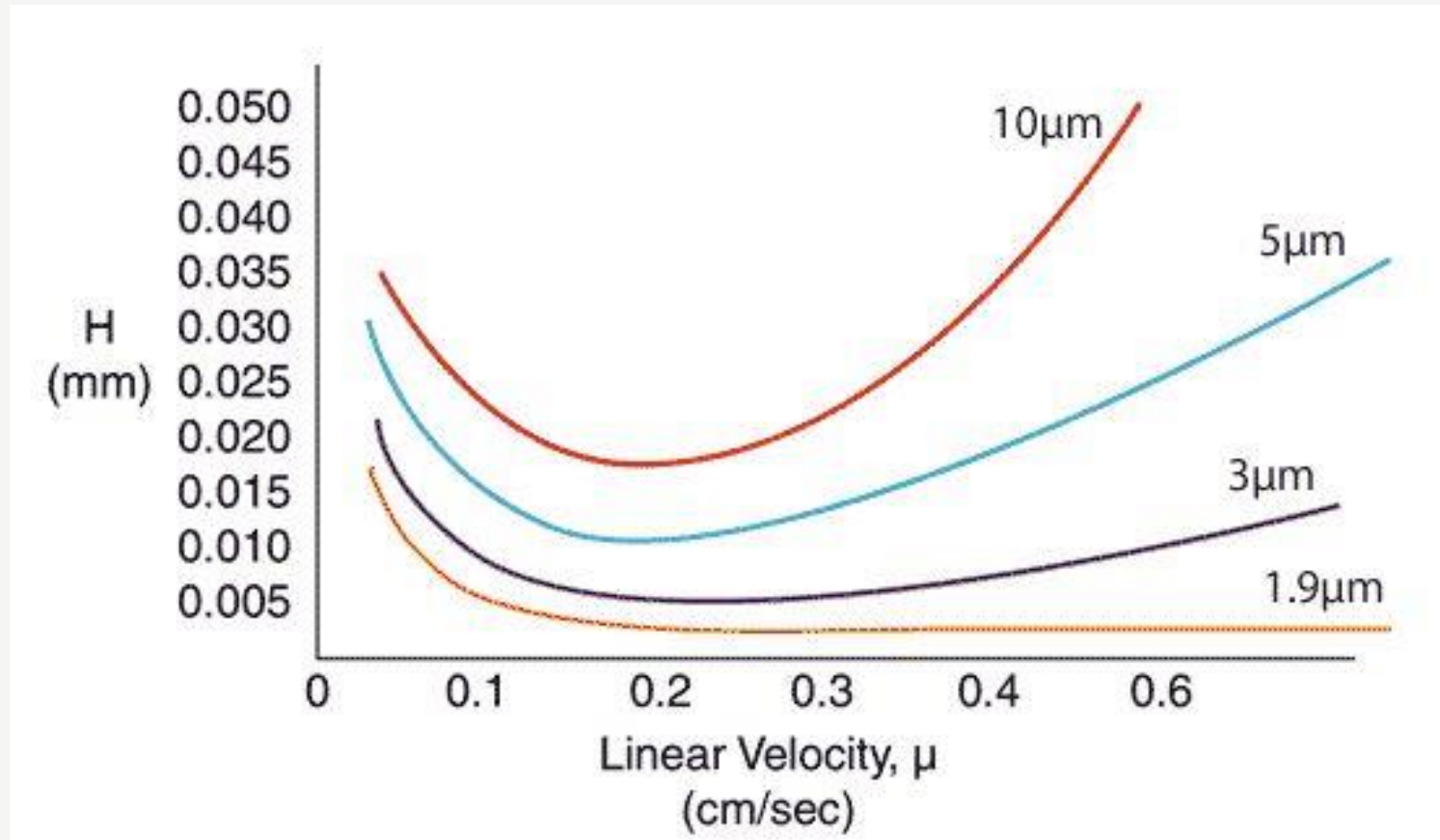
The higher  $u$ , the shorter the time for mass transfer to take place, the lower the efficiency.

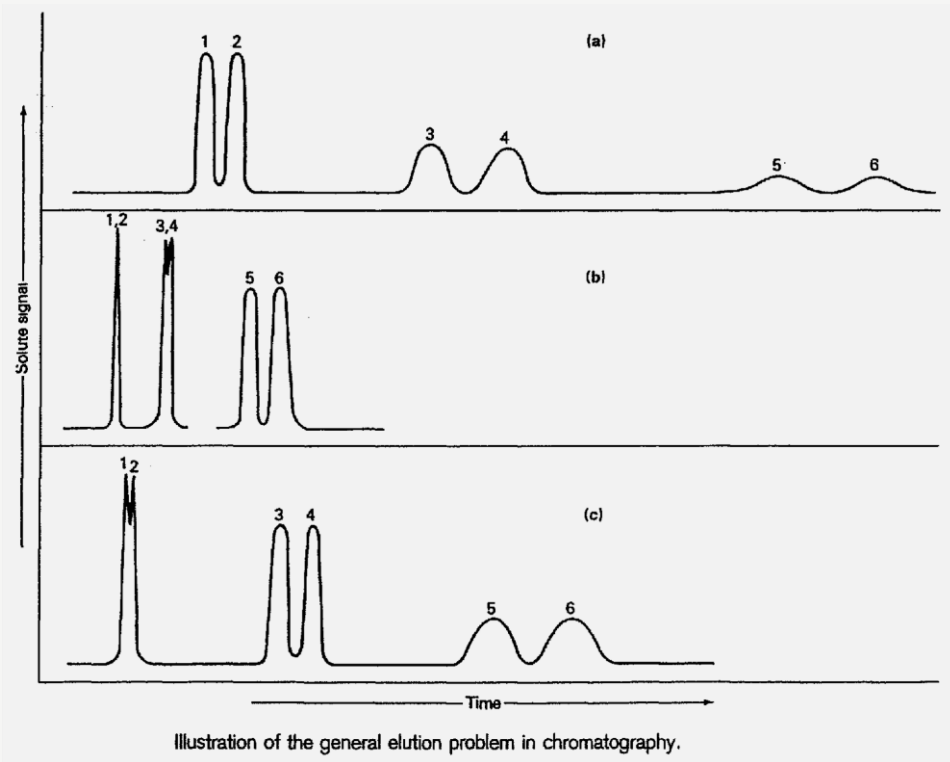
**In the case of liquid chromatography**, the term of mass transfer is the most important, whereby  $H$  is minimized by decreasing particle size, using low flow rates.

**In the case of gas chromatography**, the term of longitudinal diffusion is the most important, so  $H$  is minimized by using high flow rates.



# Optimizing the efficiency of a column





## WHAT CAN VARY:

- Column length (varies  $N$ )
- Mobile phase flow (varies  $H$ )
- Packing particle size (varies  $H$ )
- Mobile phase composition (varies  $k$ )



The determination of the concentration of the species is based on the peak area measurements,  $A$ , proportional to the number of injected moles

$$\text{Area (A)} = \text{constant} \times \text{number of moles injected} = \text{constant} \times V_{\text{inj}} \times C = \text{constant}' \times C$$

where the constant is a parameter that depends on experimental conditions, such as speed  $u$  and type of detector used,  $C$  is the concentration of the species with peak area  $A$ , and  $V_{\text{inj}}$  is the injected volume (in the order of  $\mu\text{L}$ ).

## Exercise 1

A mixture of benzene, toluene and methane was injected into a gas chromatograph (GC). Methane produced a peak after 42s, while benzene required 251s and toluene eluted in 333s. Determine:

- the retention factor ( $k$ ) for each solute.
- the selectivity factor ( $\alpha$ ).

$$k = \frac{t_r - t_m}{t_m}$$

$$\alpha = \frac{k_2}{k_1}$$



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## PROBLEM SOLVING

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- The retention factors are:

$$\text{Benzeno: } k = \frac{t_r - t_m}{t_m} = \frac{251 - 42}{42} = 5,0$$

$$\text{Tolueno: } k = \frac{t_r - t_m}{t_m} = \frac{333 - 42}{42} = 6,9$$

- The selectivity factor ( $\alpha$ ) is:

$$\alpha = \frac{k(\text{tolueno})}{k(\text{benzeno})} = \frac{333 - 42}{251 - 42} = 1,39$$

## Exercise 2

A peak with a retention time of 407s has a width at half height of 7.6s. A neighboring peak is eluted 17s later with  $w_{1/2} = 9.4$  s.

- (a) Determine the resolution for these two components.
- (b) What retention time difference is required for an adequate resolution of 1.5 s?

### PROBLEM SOLVING

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(a) Determine the resolution for these two components.

(b) What retention time difference is required for an adequate resolution of 1.5 s?

$$(a) \quad \text{Resolution} = \frac{0,589\Delta t_r}{w_{1/2_{méd}}} = \frac{0,589 \times 17 \text{ s}}{\frac{7,6 \text{ s} + 9,4 \text{ s}}{2}} = 1,18$$

$$(b) \quad 1,5 = \frac{0,589\Delta t_r}{\frac{7,6 \text{ s} + 9,4 \text{ s}}{2}} \rightarrow \Delta t_r = 21,6$$